

# Noise Shaping Techniques for Analog and Time to Digital Converters Using Voltage Controlled Oscillators

by

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Submitted to the Department of Electrical Engineering and Computer Science

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## Abstract

Advanced CMOS processes offer very fast switching speed and high transistor density that can be utilized to implement analog signal processing functions in interesting and unconventional ways, for example by leveraging time as a signal domain. In this context, voltage controlled ring oscillators are circuit elements that are not only very attractive due to their highly digital implementation which takes advantage of scaling, but also due to their ability to amplify or integrate conventional voltage signals into the time domain. In this work, we take advantage of voltage controlled oscillators to implement analog- and time-to-digital converters with first-order quantization and mismatch noise-shaping.

To implement a time-to-digital converter (TDC) with noise-shaping, we present a oscillator that is enabled during the measurement of an input, and then disabled in between measurements. By holding the state of the oscillator in between samples, the quantization error is saved and transferred to the following sample, which can be seen as first-order noise-shaping in the frequency domain. In order to achieve good noise-shaping performance, we also present key details of a multi-path oscillator topology that is able to reduce the effective delay per stage by a factor of 5 and accurately preserve the quantization error from measurement to measurement.

An 11-bit, 50Msps prototype time-to-digital converter (TDC) using a multi-path gated ring oscillator with 6ps of delay per stage demonstrates over 20dB of 1st-order noise shaping. At frequencies below 1MHz, the TDC error integrates to  $80f_{s,rms}$  for a dynamic range of 95dB with no calibration of differential non-linearity required. The  $157 \times 258 \mu\text{m}$  TDC is realized in  $0.13 \mu\text{m}$  CMOS and operates from a 1.5V supply.

The use of VCO-based quantization within continuous-time (CT)  $\Sigma\Delta$  ADC structures is also explored, with a custom prototype in  $0.13 \mu\text{m}$  CMOS showing measured performance of 86/72dB SNR/SNDR with 10MHz bandwidth while consuming 40mW from a 1.2V supply and occupying an active area of  $640 \mu\text{m} \times 660 \mu\text{m}$ . A key element of the ADC structure is a 5-bit VCO-based quantizer clocked at 950 MHz which we show achieves first-order noise-shaping of its quantization noise. The quantizer structure allows the second order CT  $\Sigma\Delta$  ADC topology to achieve third order noise

shaping, and direct connection of the VCO-based quantizer to the internal DACs of the ADC provides intrinsic dynamic element matching (DEM) of the DAC elements.

Thesis Supervisor: Michael H. Perrott

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# Chapter 1

## Introduction

### 1.1 Area of focus

As device characteristics for analog applications are expected to steadily degrade in future CMOS processes, there is increasing interest in developing new mixed-signal circuit architectures that better leverage digital circuits to improve analog processing of signals. While this trend has been occurring for some time in the form of digital calibration of analog circuits, it is worthwhile to consider alternate paths toward this goal. One such path is the use of time as a signal domain to perform mixed-signal operations such as digitization of analog signals.

In this context, voltage controlled ring oscillators are circuit elements that are not only very attractive due to their highly digital implementation which takes advantage of scaling, but also due to their ability to amplify or integrate conventional voltage signals into the time domain. In this work, we take advantage of voltage controlled oscillators (VCO) to implement analog- and time-to-digital converters with first-order quantization and mismatch noise-shaping.

Figure 1-1 depicts the VCO as an element that transforms an analog input voltage into an output signal with binary levels that can be interpreted *either* as frequency or phase. To explain, we first notice that the instantaneous VCO output frequency is directly proportional to the voltage applied to its tuning node. An example of the VCO voltage-to-frequency transfer characteristic is shown on the right side of Figure 1-1,

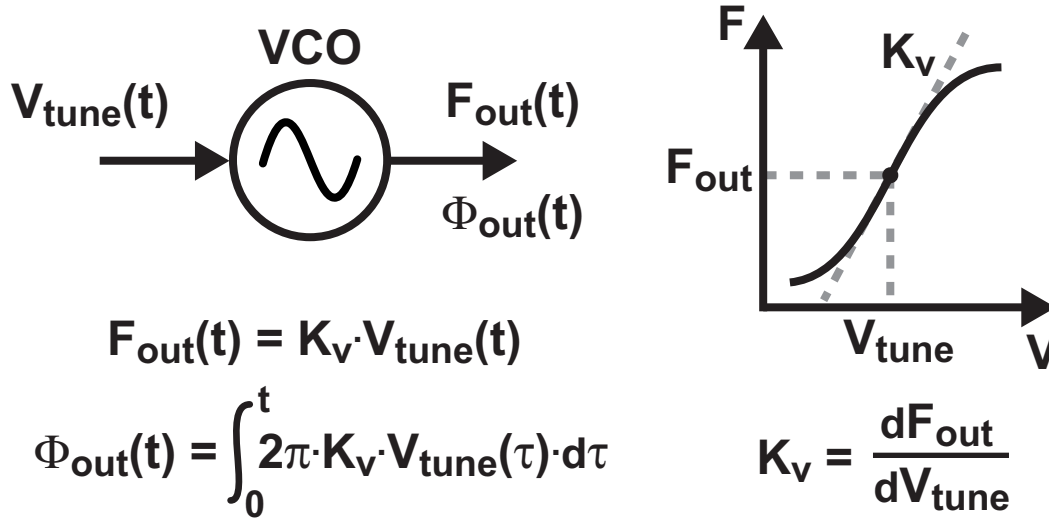


Figure 1-1 VCO voltage-to-frequency and voltage-to-phase relationships

and defines the slope of the curve,  $K_v$  [Hz/V], as the small-signal voltage-to-frequency gain. Second, we also see that the VCO effectively behaves as a continuous-time (CT) voltage-to-phase integrator. Since the output phase of an oscillating VCO accumulates without end, the VCO voltage-to-phase integration is then ideal in the sense that there is infinite DC gain. Finally, while the phase of the VCO output signal changes continuously, its voltage output toggles between two discrete output levels: high voltage and low voltage. Consequently, the VCO can seamlessly drive other digital blocks with little additional signal conditioning or amplification.

It is well-known that a simple ADC can be formed with a VCO structure by simply adding a frequency measurement capability as depicted in Figure 1-2(a). As we will see, the measurement circuits can be implemented a number of ways, however we can conceptualize this circuit for now as simply counting the number of VCO periods in each sampling clock period. The digital output of the measurement circuit will then correspond proportionally to the input voltage through the  $K_v$  gain factor.

To implement a time-to-digital converter (TDC) with noise-shaping using the VCO structure, we present an oscillator that is enabled during the measurement of an input, and then disabled in between measurements as shown in Figure 1-2(b). Note that in this case the frequency is discrete and ideally toggles between fixed

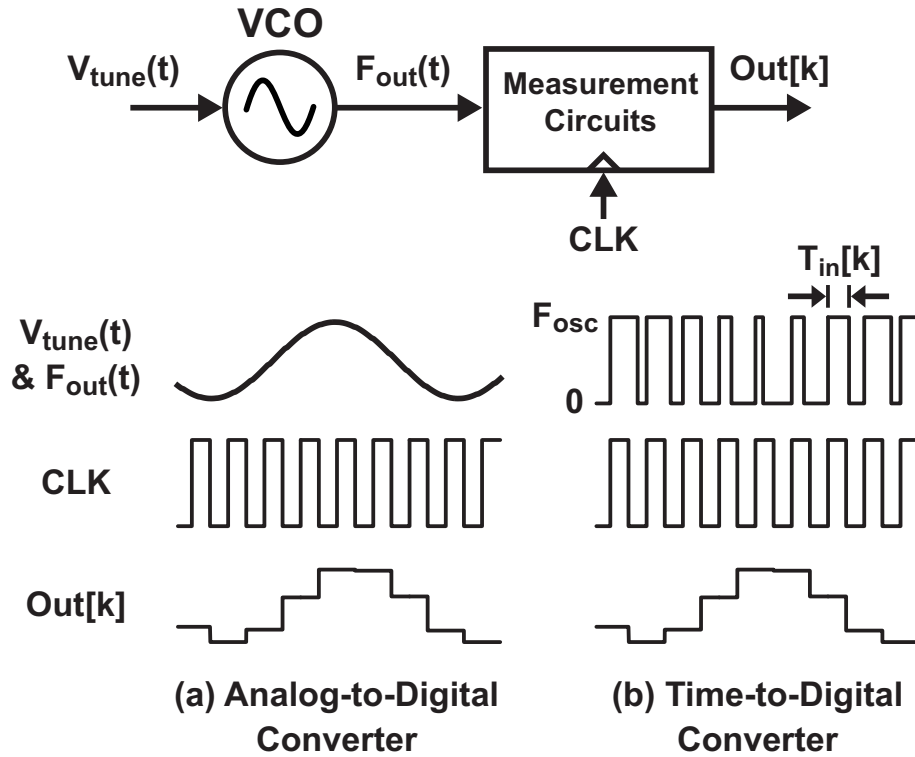


Figure 1-2 The concept of VCO-based converters: (a) a simple analog-to-digital converter, (b) a gated ring oscillator time-to-digital converter

binary values, 0 and the nominal oscillation frequency, and the analog input  $T_{in}$  is now the length of time that the oscillator is enabled. The measurement circuit again monitors the number of VCO periods or transitions that occur during the sample clock period such that the converter output linearly corresponds with the width of the input signal.

A very interesting aspect to both of these converter architectures is that, despite a digital implementation, the analog quantization error for each sample can actually be saved and passed along to the following measurement. If each sample corrects for the error from the previous sample, then the average quantization error will improve significantly by sampling the same input multiple times. In fact, we can say that properly preserving and accounting for this error will result in first-order noise-shaping in the frequency domain.

Although first-order noise-shaping is well-known and can be achieved in a relatively straight-forward manner for the ADC of Figure 1-2(a), to our knowledge

noise-shaping for a TDC has not been previously demonstrated. In order to practically achieve good noise-shaping performance for the TDC of Figure 1-2(b), the quantization error must be preserved during the time that the oscillator is disabled. In fact, holding the phase state of a VCO represents a new concept outside of the typical operating conditions for an oscillator. We therefore explore the key issues in transferring this error, and present key details of a multi-path oscillator topology that is able to significantly improve raw resolution and at the same time accurately preserve the quantization error from measurement to measurement.

An 11-bit, 50Msps prototype time-to-digital converter (TDC) using a multi-path gated ring oscillator with 6ps of delay per stage demonstrates over 20dB of 1st-order noise shaping. At frequencies below 1MHz, the TDC error integrates to  $80\text{fs}_{\text{rms}}$  for a dynamic range of 95dB with no calibration of differential non-linearity required. The  $157\times 258\mu\text{m}$  TDC is realized in  $0.13\mu\text{m}$  CMOS and operates from a 1.5V supply.

The use of VCO-based quantization within continuous-time (CT)  $\Sigma\Delta$  ADC structures is also demonstrated, with a custom prototype in  $0.13\mu\text{m}$  CMOS showing measured performance of 86/72dB SNR/SNDR with 10MHz bandwidth while consuming 40mW from a 1.2V supply and occupying an active area of  $640\mu\text{m} \times 660\mu\text{m}$ . A key element of the ADC structure is a 5-bit VCO-based quantizer clocked at 950 MHz which we show achieves first-order noise-shaping of its quantization noise. The quantizer structure allows the second order CT  $\Sigma\Delta$  ADC topology to achieve third order noise shaping, and direct connection of the VCO-based quantizer to the internal DACs of the ADC provides intrinsic dynamic element matching (DEM) of the DAC elements.

## 1.2 Primary contributions

In regard to a VCO-based time-to-digital converter, the primary contributions of this thesis are:

- The introduction of a gated ring oscillator topology that, when used in a time-to-digital converter, can achieve first-order noise-shaping of quantization and

mismatch error

- The analysis of errors due to gating an oscillator that can fundamentally limit noise-shaping performance
- The mitigation of these errors with a multi-path ring oscillator topology that linearizes the gating operation and reduces the effective delay per stage to a small fraction of an inverter delay
- The presentation of techniques to efficiently and accurately measure the phase of a multi-path ring oscillator
- The verification of first-order noise-shaping with measured results of a prototype gated ring oscillator TDC

To our knowledge, the gated ring oscillator time-to-digital converter presented in this work is the first TDC to demonstrate noise-shaping of analog quantization and mismatch error for non-adjacent measurement intervals. Further, compared with other reported TDC, the prototype described in this work is very competitive in regard to important metrics such as dynamic range, power, and area.

Another contribution of this work is the analysis of the performance advantages, limitations, and tradeoffs for an oversampled VCO-based quantizer, along with the demonstration of these considerations within a high-speed continuous time  $\Sigma\Delta$  ADC. The idea of using a VCO for voltage quantization within a  $\Sigma\Delta$  ADC has been presented multiple times [28, 39], and in fact the architecture chosen independently for this work was originally disclosed in [39]. However, while the ideas for using VCO in a  $\Sigma\Delta$  ADC have been known for many years, this work provides measurement results that justify the consideration of VCO-based quantizers in  $\Sigma\Delta$  ADC. Improvements are also discussed that may significantly improve these results, although the achieved performance is at present competitive with other state-of-the-art ADC architectures.

Together, these contributions demonstrate the utility of ring oscillator-based quantizers in achieving or advancing state-of-the-art performance for the time- and analog-to-digital converters.

## 1.3 Thesis overview

The thesis is divided into two main parts; the first half focuses on the gated ring oscillator time-to-digital converter in Chapters 2-6, and the second half addresses VCO-based analog-to-digital conversion in Chapters 7-10. For both sections, we will summarize previous work in the area, analyze and discuss the various issues that must be addressed to achieve high resolution, and present prototype implementations along with measurement results. Chapter 11 concludes the thesis with a few general remarks.

The first half of the thesis begins with Chapter 2, where we provide a background on time-to-digital converters and motivate the gated ring oscillator topology of this work. To accomplish this, we discuss historical TDC trends, describe a number of modern TDC architectures, and consider the benefits of oversampling before explaining the fundamental concept of the GRO-TDC. In Chapter 3, we examine the accuracy with which a digital GRO implementation can preserve analog signals from one measurement to the next, and present the multi-path oscillator topology that addresses these concerns. The measurement of the GRO with precise, efficient circuitry is discussed in Chapter 4, and measurement results are shown in Chapter 5. To conclude the first half of the thesis, we briefly outline methods to utilize the GRO-TDC in a number of system applications.

Chapter 7 initiates the second half of the thesis by looking at the advantages and shortcomings of a simple VCO-quantizer. The quantizer is then placed within a  $\Sigma\Delta$  ADC in Chapter 8 to improve its linearity performance, and where a few unique properties of the VCO-quantizer can be leveraged at the architectural level. System and circuit-level details of the prototype  $\Sigma\Delta$  ADC are described in Chapter 9, and the presentation of measurement results along with a discussion are included in Chapter 10.



# Chapter 2

## Background on Time-to-Digital Converters

### 2.1 Introduction

Accurate measurement of time has had a critical role in the development of science throughout history, starting with the earliest examples of analog clocks based on solar motion and water flow, and including the most accurate caesium resonators available today. As a subset of time-keeping technology, time-to-digital converters (TDC), or time-interval meters (TIM), allow for precise measurement of the time between two events. Historically, TDC have had significant application in experimental physics. For example, in the nuclear physics community, measurements of mean lifetime, particle identification, and time-of-flight require precise TDC, and many of the early integrated circuit TDC addressed such needs [53]. Today, TDC continue to serve an important role not only in experimental applications, but also in commercial time-of-flight applications such as laser rangefinding and positron emission tomography (PET) medical imaging technology [70].

A relatively new application for TDC that has emerged is closed-loop timing systems that are fully integrated in silicon technology. Since advanced CMOS processes have begun to offer extremely compact, robust, and flexible processing power, many applications have begun to replace traditional analog signal processing blocks with

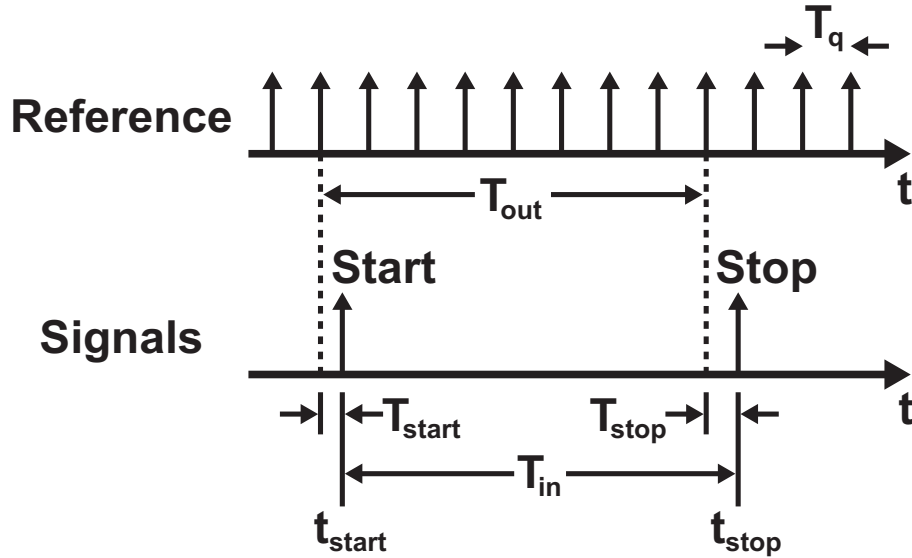


Figure 2-1 Reference and signal pulses vs. time

digital signal processing. Such a shift in architectural design places a relatively increased burden on the mixed-signal interface, especially in terms of converter performance. For systems that require precise control or alignment of timing signals, such as phase-locked loops (PLL), delay-locked loops (DLL), and clock and data recovery (CDR) circuits, the TDC is a fundamental element that can bridge the gap between the continuous-time analog domain and the discrete-time digital domain.

Considering that there is an extensive history of TDC prior to the development of digital PLL, it is useful to understand how today's state-of-the-art TDC technology relates to older ideas that have been around for some time. In fact, a review of the historical developments of TDC over the past 50 years or more reveals that, while technology has seen a tremendous change from vacuum tubes and ferrite pot-core transformers to present-day advanced CMOS, the concepts and techniques for dividing time into measurable intervals have remained remarkably the same. Given this context, although it is possible to think of TDC architectures in terms of implementation details, it is also instructive to think of the architectures in a conceptual manner. In this way, we can both understand current practice and, at the same time, shape the future efforts in TDC development by considering how these simple but powerful ideas best can be used within a new, yet undefined, component technology.

We then examine Figure 2-1, which is a picture describing the general operation of a TDC that can serve as an entry point into the discussion of many different TDC architectures and ideas. The figure, while modified slightly for our purposes, is basically equivalent to Figure 1 from Baron's 1957 original manuscript on the Vernier technique [4].<sup>1</sup> From the figure we see that the input time interval,  $T_{in} = t_{stop} - t_{start}$ , can be divided up into a number of smaller reference time intervals of nominal length  $T_q$ . An estimate of  $T_{in}$  can be trivially calculated by counting the number of intermediate reference pulses or events (i.e.  $T_{out}[k] = Out[k]T_q$ ), although there is an error to this method at both the beginning and end of the measurement,

$$T_{error}[k] = T_{stop}[k] - T_{start}[k]. \quad (2.1)$$

Given these definitions, we can express the input and output relationship for a TDC as

$$T_{out}[k] = T_{in}[k] - T_{error}[k], \quad (2.2)$$

or equivalently in terms of the TDC integer output as

$$Out[k] = \frac{T_{in}[k] - T_{error}[k]}{T_q}. \quad (2.3)$$

Since the raw TDC resolution is limited by  $T_q$ , it is not surprising that a great deal of effort over the years has been made in reducing this value, either *directly* through technology advancement, or *effectively* by using design techniques, a few examples of which will be covered later in the following section. While these efforts have made significant progress in improving TDC resolution, applications continue to demand the best resolution and/or range than can be achieved in a practical fashion.

For many early TDC applications, and especially for experimental applications, the form factor of the TDC was less important than achieving high-resolution and accuracy. As a result, many of the best TDC solutions in terms of resolution are large,

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<sup>1</sup>We should note that within this manuscript we find that Baron "recognizes the fact that the Hughes Research and Development Laboratories, prior to the work described in this report, had fabricated a similar vernier measuring system."

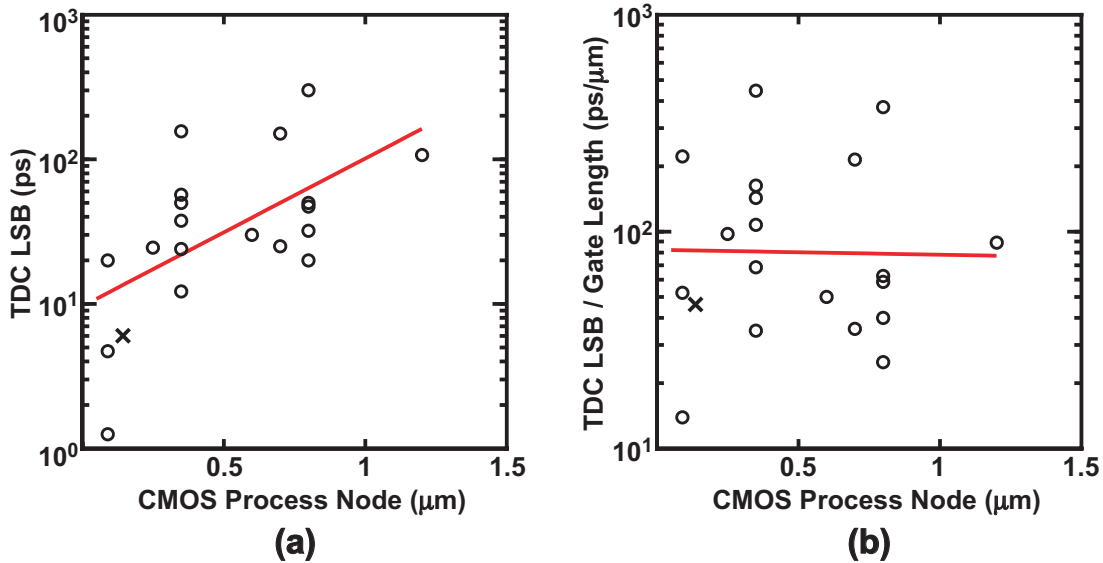


Figure 2-2 Trends of reported time-to-digital converter LSB resolution versus CMOS process technology. (a) depicts the improved resolution (decreased LSB steps) as gate lengths scale, and (b) demonstrates the relatively flat performance of TDC resolution when normalized to gate length

consume significant power, and require complex tuning or calibration. For example, in the dual-conversion approach, classic voltage-domain analog-to-digital converters can be utilized for a TDC by integrating current onto a reference capacitor for each input sample [68], which converts time into voltage before digitization. Although this approach may result in excellent resolution for a particular technology, the architecture is analog-intensive, is not power efficient, and does not take advantage of the ability to resolve digital edges in modern CMOS.

In contrast, TDC constructed with digital CMOS technology have benefited greatly from process feature scaling, since a more advanced process results in not only compact and fully-integrated solutions, but also smaller CMOS gate delays and the accompanying improvement in resolution. Figure 2-2(a) plots reported LSB size for TDC implemented in CMOS over the last decade versus the CMOS technology node (this work is shown with a  $\times$ ), and a best-fit line to the data is also shown [8–10, 13, 18, 19, 27, 29, 30, 34, 37, 43, 44, 46, 48, 56, 66, 71]. We can clearly see from this data evidence that CMOS scaling has indeed resulted in better TDC resolution, and assuming that at least some new process developments are made in the

future, TDC resolution should continue to improve.

On the other hand, Figure 2-2(b) demonstrates that when the LSB size of various TDC are normalized to the minimum transistor gate length in the process<sup>2</sup>, the performance of TDC has been relatively flat. While advancements have certainly been made in adapting TDC architectures for modern CMOS, improvements to the fundamental relationship between gate delay and LSB step size have been difficult to realize.

Certainly one way to interpret this data is to say that the best way to achieve an optimal TDC resolution performance is to wait, i.e. to follow Moore's law until scaling enables better performance with known TDC techniques. While this may be a valid approach for some applications, it does not aid the TDC designer in optimizing resolution performance *for a given technology*. Given the difficulty in improving the raw resolution in a standard CMOS process, it then becomes important to fully explore techniques such as oversampling to improve effective resolution performance, which is a primary focus of this work.

Moreover, when considering future CMOS TDC and process scaling, it is well known that transistor and parasitic mismatch has become a very real and significant problem for the most advanced technologies [54]. Therefore, while intrinsic delay may continue to decrease in the future, for traditional TDC architectures to benefit from this we also require the accuracy of the delay to improve as well. We will later see that mismatch can be a bottleneck for many TDC architectures. Therefore, achieving high performance in the presence of large delay mismatch is a critical requirement for future TDC that has so far seen little attention at the architectural level compared with the relative efforts to improve raw resolution.

Since we have described some of the basic challenges facing TDC, in the next section we will review some of the state-of-the-art TDC architectures along with their associated performance tradeoffs. This review will lead into the focus of this work, which is a CMOS gated ring oscillator (GRO) TDC. The GRO-TDC makes full

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<sup>2</sup>Gate propagation delay is often approximated to be proportional to transistor length [81, 82], and therefore normalizing to transistor gate length is a reasonable way to normalize fundamental resolution.

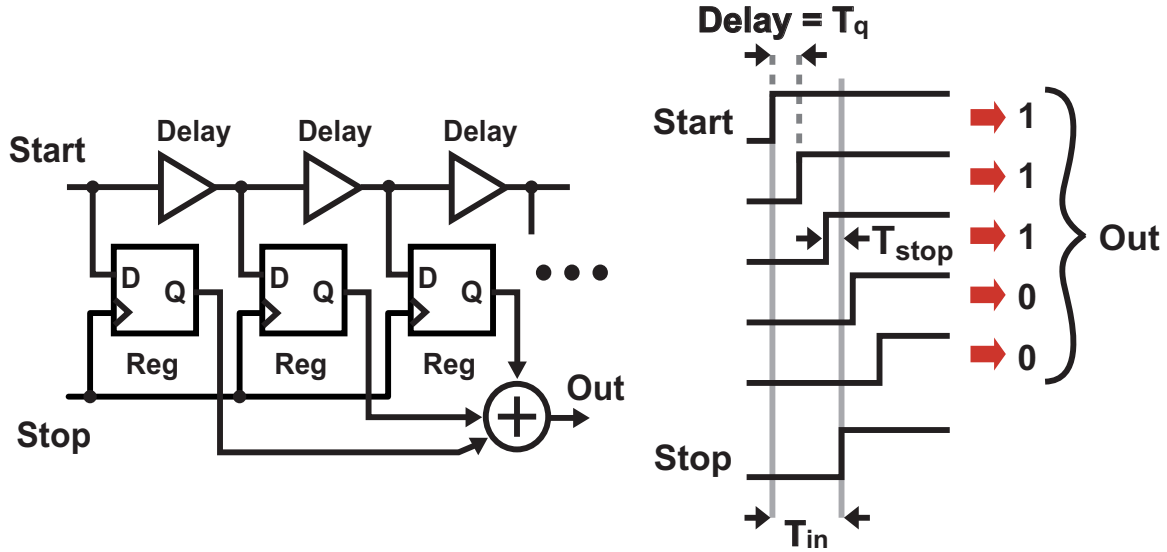


Figure 2-3 Classical delay-chain TDC

use of oversampling to address the issues of limited TDC resolution in the presence of large mismatch, while at the same time achieving a large dynamic range, compact area, and low power consumption.

## 2.2 TDC with gate-delay resolution

A classic TDC architecture comprised of a chain of delay elements is shown in Figure 2-3 [2, 32], and effectively works by counting the number of sequential inverter delays that occur between two rising signal edges. One very attractive feature of this architecture can be seen immediately in that the TDC can be constructed entirely from standard digital gates, as evidenced by its adoption into the FPGA community [65, 78]. The compact and digital architecture offers a moderate performance, and has been proved to be commercially viable for some digital PLL applications in the wireless industry [66].

To explain its operation, the rising edge of the start signal, which represents the first event, is successively delayed by a series of inverter gates (polarity is ignored throughout for simplicity), each with delay  $T_q$ . The outputs from each of these inverters are input to a register, which is clocked with the rising edge of the stop signal

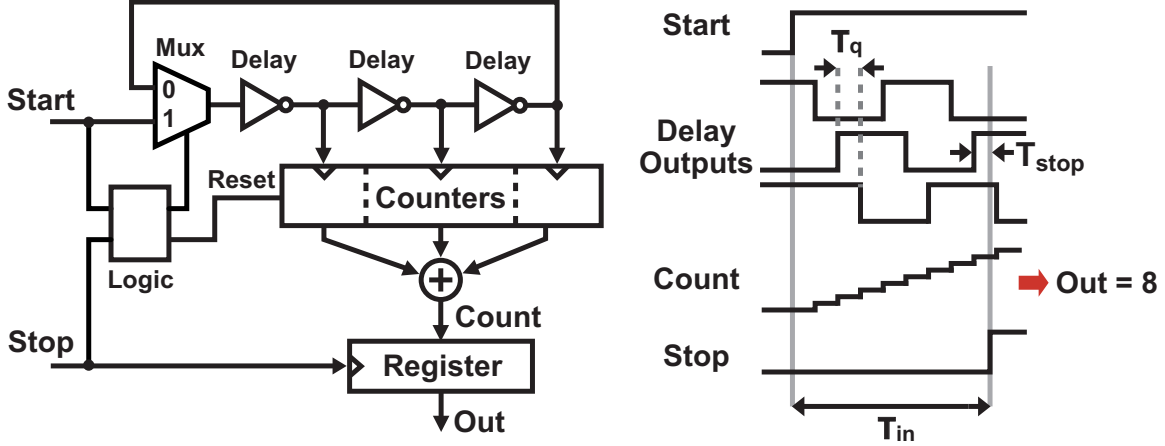


Figure 2-4 A cyclic TDC based on re-using delay elements

representing the second event. A thermometer code is then generated at the register output, which corresponds to the number of delay elements that have transitioned within the measurement interval  $T_{in}[k]$ . The TDC output  $Out[k]$  is then simply calculated as the sum of the thermometer code, and is related to the input by Equation 2.3, where the overall error can be described in this case as

$$T_{error}[k] = T_{stop}[k]. \quad (2.4)$$

Although the delay-chain architecture offers a simple TDC with moderate performance, an important limitation to consider is the high cost for increasing its range. Increasing the dynamic range of the delay-chain TDC requires a *linear* increase in the number of delay elements, which similarly increases the power consumption and decreases the maximum sampling rate.

A simple solution to the limited range of the delay-chain TDC is to wrap or fold the end of the chain back to the beginning through a multiplexer that is controlled by digital logic, as shown in Figure 2-4. The multiplexer selects the start signal during the beginning of each time interval, and after this start signal has occurred then quickly switches to select the end of the delay-chain so that the subsequent edge transitions rotate around the ring. This technique allows each of the delay elements to be used multiple times per measurement, and the TDC output is simply found

by counting and summing all of the delay element transitions that occur during  $T_{in}$ . Compared to the delay-chain TDC, the cyclic TDC core does not scale up at all with larger range, and the counters will only scale with the logarithm of range.

Asymmetry in the delay-chain structure due to the multiplexer increases the mismatch for that particular element, which degrades the differential non-linearity performance. Techniques to match the multiplexer delay to that of a delay element can be used, such as incorporating a multiplexer with fixed connections in each of the delay elements [23]. In terms of integral non-linearity, the cyclic TDC has better performance than the delay-chain TDC for large input signals due to the periodic use of delay elements.

While the TDC range can be improved with the simple cyclic TDC, a more problematic issue that has not been addressed is the coarse resolution, which is limited to a minimum inverter delay in the process. Although over time technology scaling will improve the intrinsic delay, the mismatch of delay elements is expected to get worse. Additionally, as mentioned in the preceding section, physical limitations due to TDC thermal and 1/f noise will continue to be out-of-reach for resolutions limited by a gate-delay. Therefore, an important problem to consider is how  $T_q$  of the simple delay-chain architecture can be divided into smaller intervals in order to significantly improve TDC resolution.

## 2.3 TDC with sub-gate-delay resolution

The Vernier delay technique [4] is one of the older techniques for time digitization that has been adapted for improving the resolution of digital CMOS TDC [13, 55, 57], and has been widely documented in the literature. As shown in Figure 2-5, the concept is to effectively stretch the input time interval  $T_{in}$  by delaying *both* the start and stop signals with delay-chains. What defines the resolution in this case is not the *absolute* rate of transitions (gate-delay being equal to the number of transitions per second), but the *relative* rate of transitions. As a result, the effective resolution of the Vernier TDC is found to be the difference of the two delays, or more specifically,



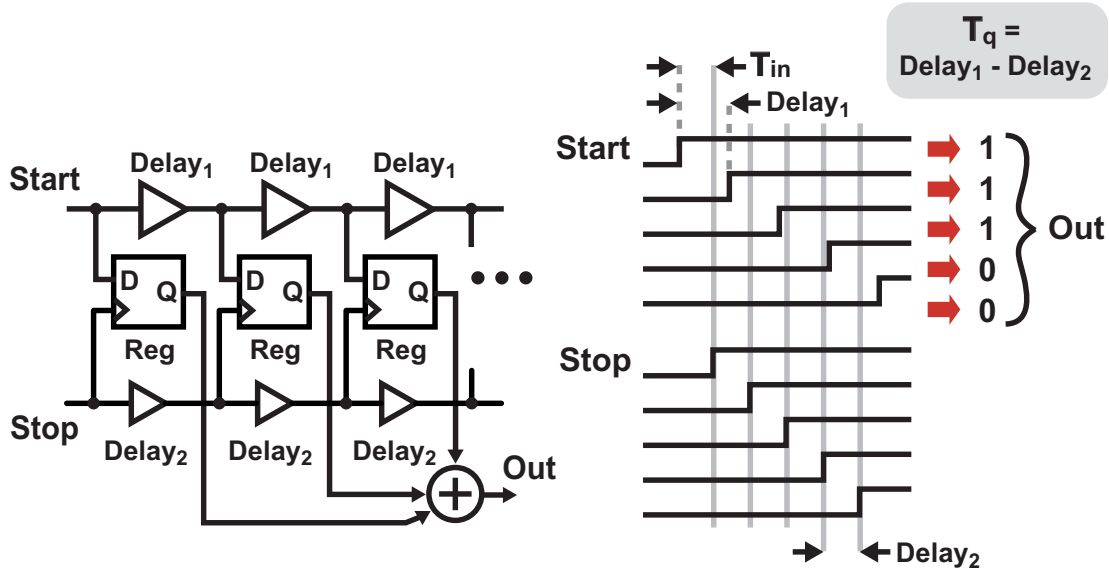


Figure 2-5 An Vernier TDC that effectively amplifies the input time interval

$$T_q = \text{Delay}_1 - \text{Delay}_2.$$

Given this result, the Vernier technique may appear to be able to substantially improve a TDC resolution. However, there are a number of issues to consider that practically limit the resolution improvement to a factor of 4-10. Specifically, the same issues that are found in the simple delay-chain TDC (e.g. range, sensitivity to mismatch) are present in the Vernier TDC, except that, along with the resolution, the magnitude of the problems have also been amplified. Although the Vernier delay elements may be tuned to match a fixed offset and calibrated at the system level, such techniques are both cumbersome and dependent on system-level architecture design [76].

To reduce the size of practical Vernier TDC, various dual step architectures based on Vernier techniques have been proposed [27, 56, 57], as shown in Figure 2-6. These architectures often have a simple delay-chain TDC (Figure 2-3) as the first stage, and then further refine the initial measurement by amplifying the residual error and then passing it to a second, higher resolution Vernier TDC. Another dual step technique that amplifies time error using the metastability property of digital gates has also been proposed, and in this case a larger resolution improvement up to a factor of 20 is reported [34].

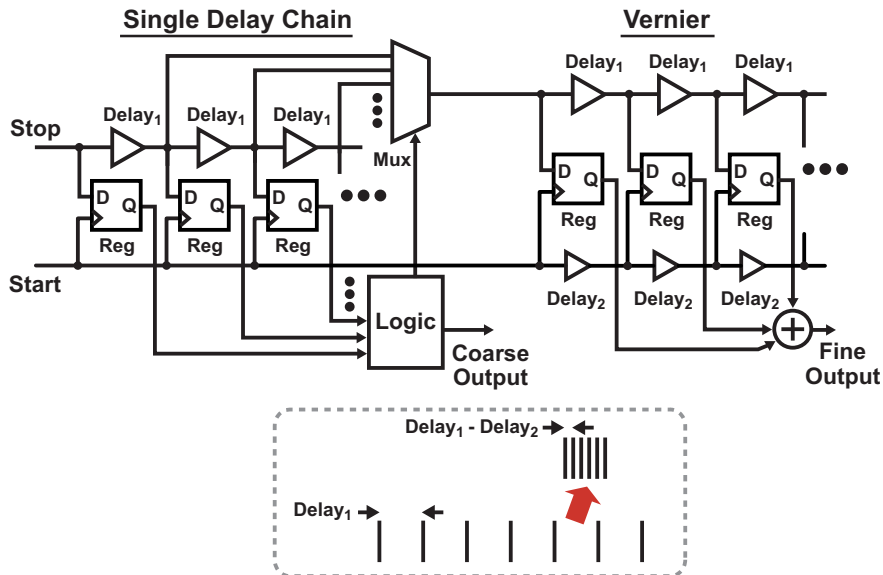


Figure 2-6 A dual-step TDC that incorporates both the delay-chain and Vernier techniques

Although the range for these architectures is larger than what would be achieved for a single-step TDC using the same resolution improvement techniques, the fundamental range versus size tradeoff does not improve compared with the simple delay-chain TDC discussed earlier. Interestingly, a cyclic architecture similar to Figure 2-4 may be used to significantly increase the range of the single or dual-step Vernier TDC [57]. In this case, the decoding logic and calibration become more complicated due to the many logical states that are supported.

Another technique to improve TDC resolution below that of a gate-delay is to interpolate between the input and output signals of a digital gate. Figure 2-7 illustrates this concept using a resistive divider, where the undriven nodes are taken to be the average of the delay element input and output signals. The operation of averaging creates a new intermediate signal with a transition that effectively divides the gate-delay into two smaller intervals. All of the new signals must be registered appropriately, which increases the TDC size, but again a cyclic architecture can be utilized to mitigate this issue [23]. The improvement in resolution for the interpolation architecture over the gate-delay is similar to that of the Vernier architecture, and is practically limited by the non-linear impedances of the delay elements during

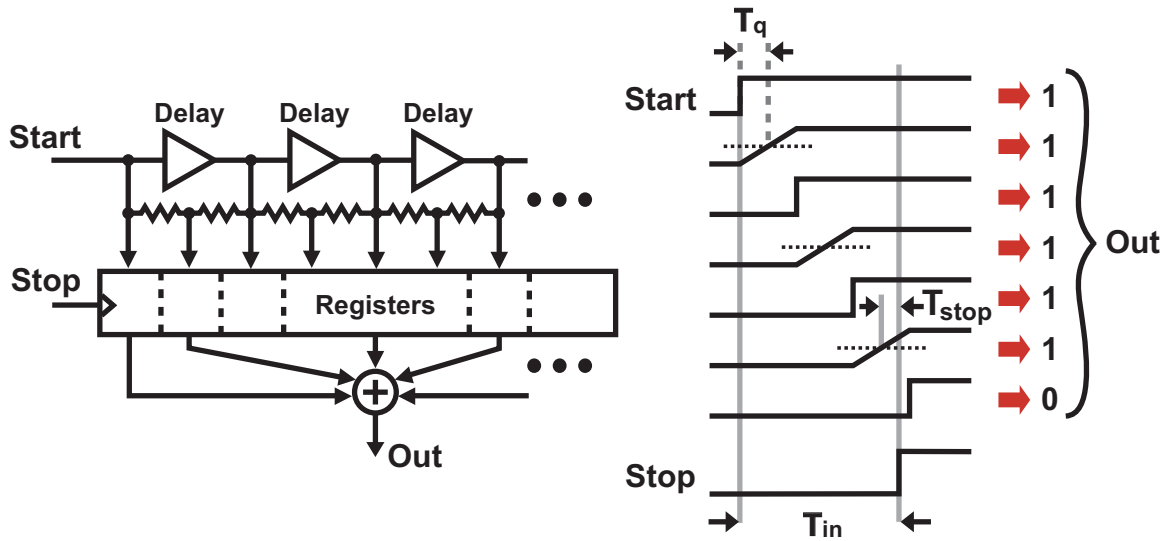


Figure 2-7 An analog interpolating TDC that creates transitions with sub-gate-delay spacing

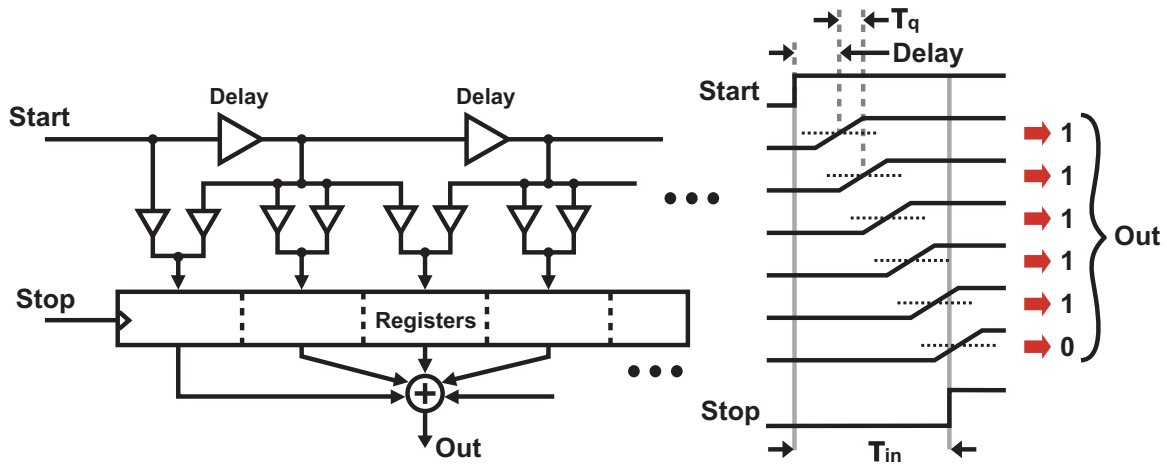


Figure 2-8 A digital technique for creating transitions with sub-gate-delay spacing

the switching transients.

The implementation of the interpolation architecture is not limited to resistive ladders, and can also be efficiently realized with digital gates if the output signals are allowed to be driven by more than one delay element. As shown in Figure 2-8, the same averaging effect can be achieved by connecting the outputs of two delay elements in parallel, while the two delay element inputs are staggered in time. The result from this parallel connection is that the output impedances from both delay elements are averaged together, which then reduces the effective delay per stage. Although this

architecture can also be expanded into a cyclic TDC, achieving a significant improvement in resolution requires more than two delay elements to be connected in parallel, which then increases the complexity of the multiplexer significantly. Nonetheless, we will later see in Chapter 3 that these techniques can be modified when constructing an oscillator-based TDC, and can in fact be quite useful.

For each of the Nyquist TDC architectures described so far, we have seen that significant effort is required to reduce the TDC resolution below that of a gate-delay, and in each case the cost for doing so is increased complexity, area, and/or mismatch. Another common thread to these converters is that there is a deterministic mapping from a given input signal onto a series of delay elements. Since we know that significant element-to-element delay variations due to mismatch cause quantization errors that are non-linear, calibration is very much required for such converters that hope to have resolution far below that of a gate-delay [23, 34, 66]. In a practical implementation, although calibration does generally improve resolution performance in the presence of mismatch, it is an added complexity that can significantly increase TDC area and power consumption. Further, while calibration is quite effective at improving integral non-linearity, it is very difficult to completely remove differential non-linearity errors.

## 2.4 Oversampling TDC considerations

From the examples described in the previous section, we clearly seek TDC implementations not only with excellent resolution, but also with inherently robust sensitivity to issues such as mismatch. It is in this context that we proceed to consider how oversampling may be used to improve TDC performance.

Oversampling describes the quantization of a signal with fixed bandwidth ( $F_b$ ) at a speed  $F_s$  much faster than the Nyquist rate required to reconstruct the original signal without aliasing. Because we often assume that the quantization error,  $T_{error}$ , is random and uniformly distributed over the quantization step, linear system analysis is commonly applied to compute the quantization noise power spectral density (PSD).

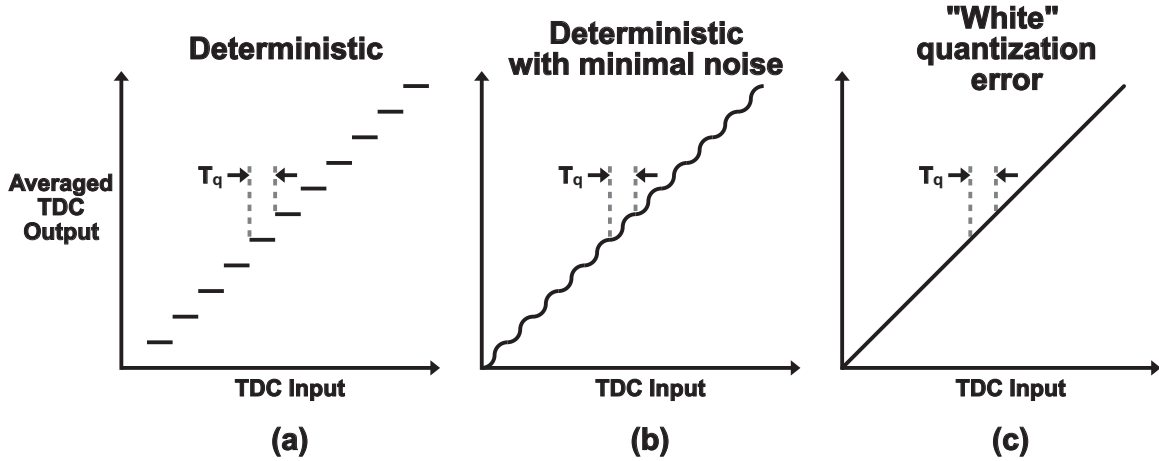


Figure 2-9 The DC transfer characteristics for (a) a completely deterministic TDC, (b) a deterministic TDC with small jitter either due to thermal noise or the input, and (c) a TDC with "white" quantization error due to inherent error scrambling or external dithering

Such standard analysis in the frequency domain assumes that the resulting quantization error is spectrally white and that its PSD in discrete time ideally decreases with sampling rate,

$$PSD_{error} = \frac{T_q^2}{12F_s}. \quad (2.5)$$

It is then expected that filtering of the converter output to remove the undesired bandwidth will also remove a similar proportion of quantization noise, thus realizing the improved signal-to-noise ratio that oversampling can ideally provide.

However, as just mentioned, such analysis depends on the quantization error being random and uniformly distributed over the quantization step, which is not true in general for quantizers with small input signals. As we saw earlier, an important characteristic of the delay-chain TDC is that, since there is no error at the beginning of the measurement (Equation 2.4), the output and error for each measurement are *deterministic* functions of the input. As a result, the DC transfer characteristic of an ideal delay-chain TDC shown in Figure 2-9(a) reveals a non-linear staircase function. For this class of deterministic converters, there is no inherent scrambling of the TDC error that generally can be used to improve effective resolution through oversampling.

In practice, even for deterministic TDC, there is a small amount of noise from both the input signal and the TDC itself that will round off the edges of this staircase

function. As shown in Figure 2-9(b), the resulting DC transfer characteristic is now smoothed somewhat, although the staircase non-linearity can still be evident. In fact, a linear DC transfer characteristic (i.e. a random quantization error) can be achieved in a deterministic quantizer *only* if the input signal is sufficiently large compared to the quantization step size, which includes the situation where the input signal itself is noisy, or if the physical noise internal to the converter is larger than the quantization step size. This condition is illustrated in Figure 2-9(c).

In a closed-loop system such as a PLL, there are certain conditions in which the system may provide such scrambling of the TDC input, for example as it may in a fractional-N  $\Sigma\Delta$  PLL. However, there are many applications to be aware of that do not provide such a dithering. For example, the TDC input for high-performance integer-N PLL limits to a very small range with very little deviation or noise, and a lack of random error in deterministic TDC can be a significant problem. This situation can be compared to the classic dead-zone in an analog phase detector, which is well-known to cause erratic limit-cycle behavior in integer-N PLL.

One solution to this problem is to intentionally modulate the TDC input with a sufficiently noisy signal in order to improve the randomness of the quantization error. Of course, adding unknown noise to a TDC input is a rather poor way to linearize the quantization. Instead, if the “noisy” signal is known and the gain of the TDC is well-characterized, this “noise” can then be subtracted from the TDC output, which ideally would result in a random error that can benefit from oversampling. However, we note that the uncalibrated or residual non-linear quantization error due to mismatch will *not* be corrected with averaging or filtering, since these errors will already have folded in the sampling process to corrupt the bandwidth of interest.

For example, let us consider a high performance Vernier TDC running at 50MSPs that has been optimized at the system level to detect small input signals by modulating  $T_{in}$  with a psuedo-random noise source. We can assume that  $T_q$  has been improved by a factor of 4 from the raw gate-delay of 20ps to reach 5ps resolution. Further, a run-time calibration circuit has been designed that allows for compensation of the psuedo-random input sequence and delay element mismatch. Through

this calibration, the effect of mismatch has been reduced from a delay error standard deviation of 10% to an absolute error standard deviation of only 1%, an improvement of over 20dB. The overall rms TDC quantization error for a fixed 50kHz analog bandwidth (typical bandwidth for a  $\Sigma\Delta$  PLL) can then be estimated by the rms sum of quantization noise and mismatch error as

$$T_{error_{rms}} = \sqrt{\frac{T_q^2(2F_b)}{12F_s} + (T_{mm-rms})^2} \quad (2.6)$$

$$= \sqrt{\frac{(5 \times 10^{-12})^2(1 \times 10^5)}{12(50 \times 10^6)} + (200 \times 10^{-15})^2} \quad (2.7)$$

$$= 210fs \quad (2.8)$$

While this result is relatively impressive, it is important to notice two aspects of this example that may be cause for some concern. First, while the rms error due to mismatch without oversampling is negligible, it becomes a dominant source of error once oversampling is leveraged. Since the level of mismatch is only expected to get worse in future CMOS processes, we can now see that this poses a bottleneck for improving the performance of deterministic TDC in the future. The second issue in this example is the level of complexity that was required to achieve the result, both at the component and system levels. As we will soon see, a much simpler TDC implementation in the form of an oscillator has the benefit of inherently scrambled quantization *and* mismatch error, which makes it well-suited for oversampling applications.

## 2.5 Oscillator-based TDC

Figure 2-10 illustrates the classical ring oscillator-based TDC composed of a ring of delay elements [46,59], which shares a number of characteristics with the cyclic TDC from Figure 2-4. First, we note that for both topologies the oscillator transitions are counted during the input time window  $T_{in}$ , here designated by the *Enable* signal. Next, all counter outputs are summed together and stored as the TDC output before being reset (during *Enable* low) to prepare for the next measurement. Finally, due

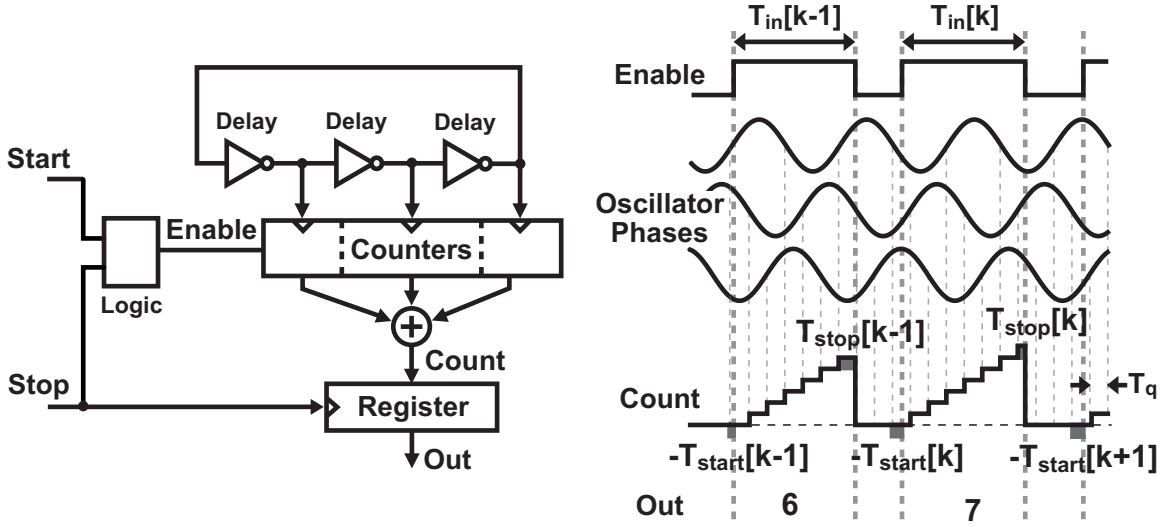


Figure 2-10 Classical oscillator-based TDC

to the logarithmic scaling of the counter range, the oscillator-based TDC also has the attribute of a large dynamic range with reasonable silicon area.

A key difference between the two architectures, however, is found when examining the overall quantization error for the oscillator-based TDC. We find that counting the transitions of a free-running oscillator results in error equivalent to the fundamental expression given earlier by Equation 2.1 and repeated here for convenience,  $T_{error}[k] = T_{stop}[k] - T_{start}[k]$ . Compared with the delay-chain or cyclic TDC error from Equation 2.4, we now include *both*  $T_{start}$  and  $T_{stop}$ , which indicates that each measurement of the oscillator-based TDC will have an *additional* error contribution from  $T_{start}$ . For our purposes, we can assume that the oscillator phase at the beginning of each sample is random, and subsequently  $T_{start}$  is also random having uniform density on the interval  $[0, T_q]$ . By way of contrast, the cyclic TDC "phase" is effectively set to 0 at the beginning of each measurement.

To have benefit from oversampling, we thankfully do not require the overall TDC error  $T_{error}$  to also be a random variable with uniform density, as in fact this criteria is quite difficult to satisfy for small inputs. Rather, we require  $T_{error}$  to be a white random variable with flat power spectral density (PSD) across all frequencies and for all inputs, including zero frequency. In addition, we require  $T_{error}$  to be uncorrelated



with  $T_{in}$ . Discussion of the special cases, for example where  $T_{in}$  is *exactly* equal to an integer multiple of  $T_q$  (i.e.  $T_{error} = 0 \forall T_{in} = kT_q$ ), will be postponed until later, using the justification for now that this special case ideally occurs with zero probability and can therefore be ignored.

Due to the random properties of  $T_{start}$ , the oscillator-based TDC satisfies the above criteria for  $T_{error}$ . We can expect that the small penalty of larger error for the inclusion of  $T_{start}$  can be easily offset by the resolution improvement by oversampling. Interestingly, the oversampling benefit in the oscillator-based TDC is not constrained to simply improving the quantization error, but also extends to improving errors from mismatch as well.

To further explain how mismatch is also improved by oversampling, we first consider an input  $T_{in}$  that is less than an oscillator period. As mentioned earlier, the oscillator starting phase is random with uniform density, which implies that the delay elements that transition during the *Enable* window are chosen with a white random process that is independent of the input. Therefore, input intervals that are a fraction of the oscillation period will have mismatch error with flat power spectral density.

Next, we can consider intervals of  $T_{in}$  that are longer than an oscillation period. In this case,  $T_{in}$  can be seen as an interval composed of two parts: an integer number of periods, which *does not* contribute mismatch error, and the residual fraction of a period that *does* have mismatch contribution. The argument from the first case can again be used on the residual part of the input with length of less than a period. As a result, we can conclude that for inputs of any length, mismatch error is reduced through oversampling and has *no contribution* towards integral non-linearity for the oscillator-based TDC.

At this point another example is helpful to quantitatively compare a simple oscillator-based TDC with raw resolution of a gate-delay resolution with the sub-gate-delay approaches discussed earlier. For this example, let us consider the same sample rate of 50Msps, analog bandwidth of 50kHz, gate-delay of 20ps, and mismatch of 10%. Since we will rely on oversampling to reduce mismatch, we can also assume that there is no calibration. With these parameters set, the overall rms TDC

quantization error is found to be

$$T_{error_{rms}} = \sqrt{\frac{2F_b}{F_s} \left( \frac{2(T_q^2)}{12} + 2(T_{mm-rms})^2 \right)} \quad (2.9)$$

$$= \sqrt{\frac{1 \times 10^5}{50 \times 10^6} \left( \frac{2(20 \times 10^{-12})^2}{12} + 2(2 \times 10^{-12})^2 \right)} \quad (2.10)$$

$$= 367 fs. \quad (2.11)$$

By comparing the two examples so far, while the simple oscillator TDC achieves resolution performance that is on the same order of the Vernier TDC, the result is achieved with *much simpler* implementation and without input dithering *or* calibration. This demonstrates the benefits of oversampling, not only for improving raw resolution, but also for mitigating the effect of mismatch. The error for the oscillator TDC has raw delay and mismatch components that decrease *together* with oversampling, while the Vernier error has a floor set by the ability to calibrate the mismatch error.

Although the oversampling with the oscillator-based TDC does offer improved resolution, it comes at a fairly expensive penalty in terms of bandwidth and power. In terms of bandwidth, to effectively decrease  $T_q$  by a factor of 2, the oversampling rate would need to be increased by a factor of 4 times the rate. Equivalently, a doubling of the sample rate results in decreasing the quantization error by 3dB, which is a small though helpful improvement. When it comes to power efficiency, in many applications the input signal  $T_{in}$  is quite small compared to the measurement period,  $T_s$ , yet the ring oscillator continues to run freely regardless of the measurement state. This results in wasted power that could otherwise be spent on improving the raw delay resolution of the oscillator.

## 2.6 Gated ring oscillator TDC

Figure 2-11 illustrates the concept of a gated ring oscillator (GRO) TDC [21, 25], which is again similar to the previous cyclic and oscillator TDC in that it measures

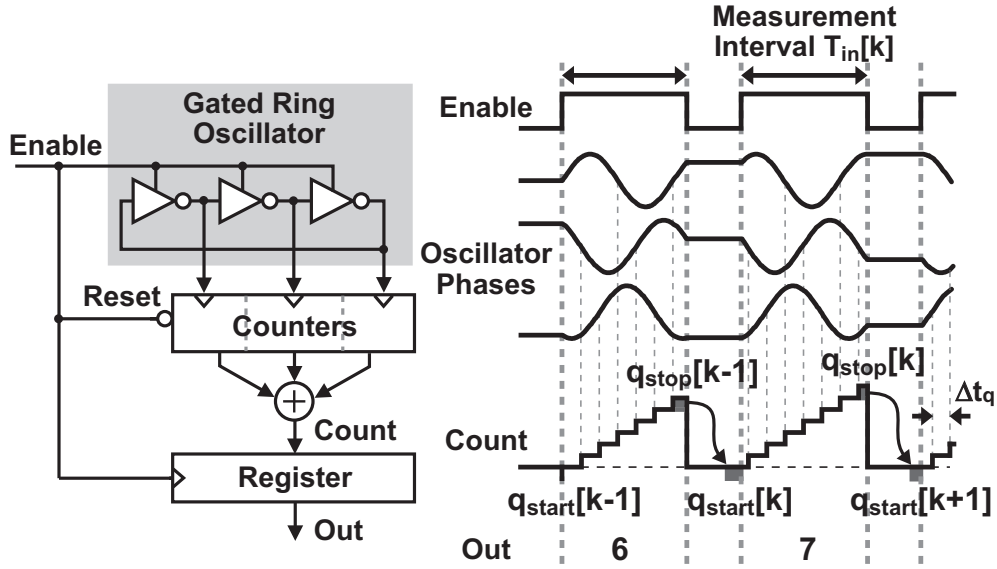


Figure 2-11 Concept of the gated ring oscillator TDC

the number of delay element transitions during a measurement interval. Also similar is the ability of the GRO-TDC to achieve large range with a small number of delay elements. However, the key innovation in the gated ring oscillator is that instead of enabling the *counters* during the measurement window, the *ring oscillator* itself is gated with the *Enable* signal, with the state of the oscillator preserved in between measurements.

By preserving the oscillator state at the end of the measurement interval  $T_{in}[k-1]$ , the quantization error  $T_{stop}[k-1]$  from that measurement is also preserved. In fact, when the following measurement of  $T_{in}[k]$  is initiated, the previous quantization error is carried over as  $T_{start}[k] = T_{stop}[k-1]$ . This results in first-order noise shaping of the quantization error in the frequency domain, as evidenced by the first-order difference operation on  $T_{stop}$  since the measurement error is given by

$$T_{error}[k] = T_{stop}[k] - T_{stop}[k-1]. \quad (2.12)$$

A subtle aspect to the GRO-TDC is that, along with the quantization noise, the delay element mismatch is also first-order shaped. To see this more clearly, let us examine the sequencing of delay elements for successive TDC conversions, as

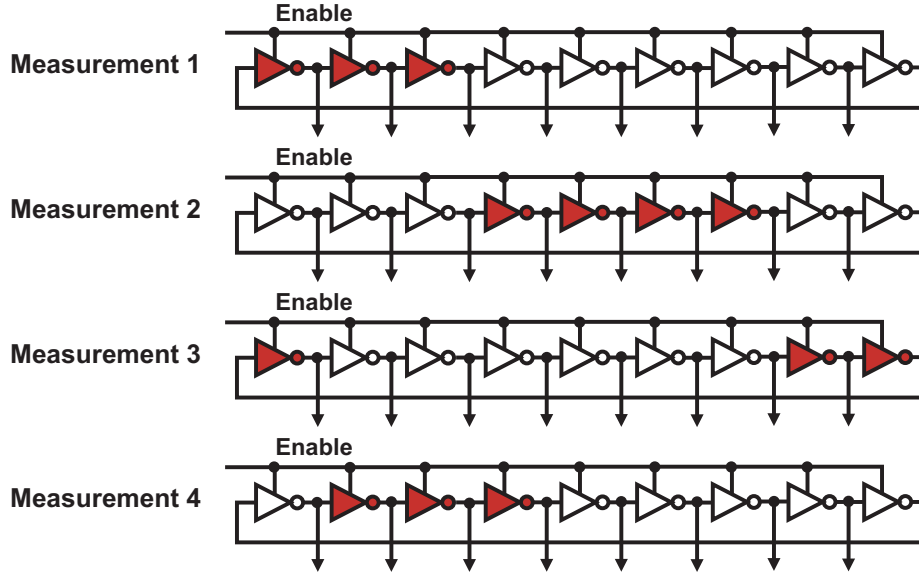


Figure 2-12 Barrel-shifting of GRO delay elements to achieve first-order shaping of mismatch error

shown in Figure 2-12. What is clearly evident in this figure is that the selection of delay elements for a given input is equivalent to the well-known barrel-shift algorithm for dynamic element matching. Similar to the transfer of quantization error, the mismatch errors for one sample are also passed along to and subtracted from the following sample. Therefore, we can expect that in the case of oversampling, the GRO-TDC architecture ideally achieves high resolution without the need for calibration, even in the presence of large mismatch.

Now comparing the GRO-TDC to the oscillator-based TDC for a single-shot measurement, the GRO-TDC will have the same additional quantization error penalty found in Equation 2.1. However, when considering again the benefits from oversampling, the GRO-TDC quantization error will ideally decrease by 9dB for a doubling of the sample rate, which is a significant improvement compared to the 3dB possible for the oscillator TDC. This relationship can be clearly seen in the expression for rms TDC quantization error

$$T_{error_{rms}} = \sqrt{\left(\frac{T_q}{2}\right)^2 \frac{1}{9\pi} \left(\frac{2\pi F_b}{F_s}\right)^3} \quad (2.13)$$

An example GRO-TDC using the same parameters as the previous oscillator example will then ideally have rms TDC quantization error of only

$$T_{error_{rms}} = \sqrt{\left(\frac{20 \times 10^{-12}}{2}\right)^2 \frac{1}{9\pi} \left(\frac{2\pi 5 \times 10^4}{50 \times 10^6}\right)^3} \quad (2.14)$$

$$= 0.9fs! \quad (2.15)$$

While this ideal performance level is far below typical thermal and 1/f noise levels for digital CMOS, even the *potential* to achieve TDC resolution that is limited by physical processes in a simple architecture is very compelling. The combination of oversampling with first-order quantization noise and mismatch shaping is quite powerful and can result in very high resolution conversion. Moreover, as will be seen in the following sections, the GRO-TDC requires only a modest level of complexity that can be implemented with small area and power consumption.



# Chapter 3

## Detailed GRO operation

### 3.1 Simple Gated Ring Oscillator Implementation

While first-order quantization noise shaping is very appealing for many applications, it is yet unclear that preserving a ring oscillator state through the stop and start operation is possible, and even more unclear is whether a simple circuit topology can yield useful and practical results. Because the noise shaping we desire depends on the accurate transfer of quantization error from one measurement to the next (i.e.  $T_{start}[k] = T_{stop}[k - 1]$ ), it is important to consider how well this can be accomplished with simple circuitry, and also how imprecise error transfer will affect noise-shaping. Towards this end, we now consider a simple circuit topology to illustrate the key design challenges of the gated ring oscillator.

#### 3.1.1 GRO with inverter delay stages

Figure 3-1 illustrates one potential implementation for gating a ring oscillator by using switches [21]. Starting from a classical inverter-based ring oscillator with an odd number of stages, these switches are added in series to the positive and negative power supply connections for each inverter, and all switches share a common state. When the switches are closed, oscillation is enabled and the ring of inverters behaves identically to a classical ring oscillator (Figure 3-1(a)). Conversely, when the switches

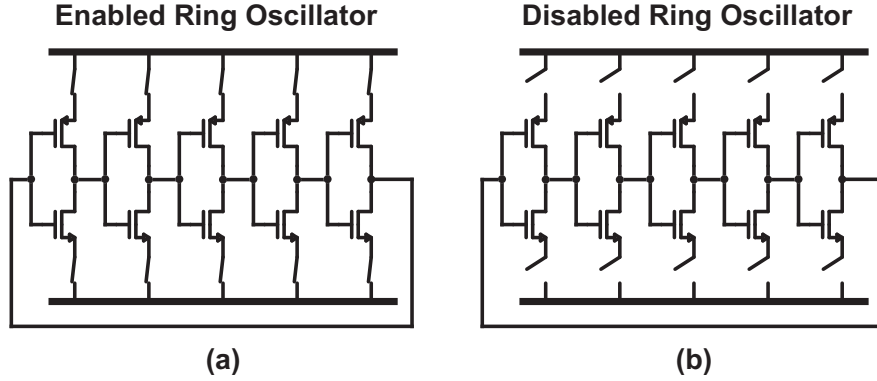


Figure 3-1 Conceptual implementation of gating a ring oscillator

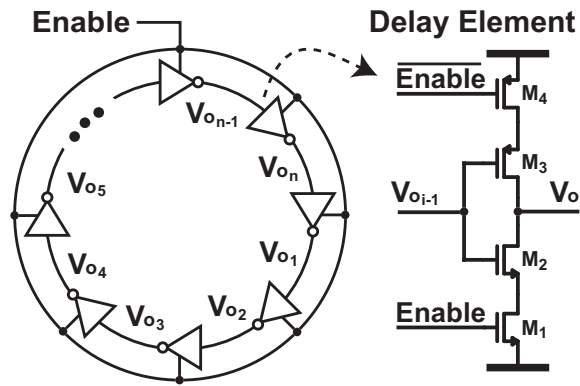


Figure 3-2 Transistor-level schematic of a simple GRO

are open, the inverter delay element is unable to charge or discharge the parasitic output capacitance, and as a result oscillation is suspended (Figure 3-1(b)). The oscillator phase at the end of the enabled state is then held during the disabled state with the charge stored on the parasitic capacitance of the delay elements.

The delay element switches of Figure 3-1 are well-suited for CMOS technology, and can therefore be implemented for each element with complementary transistors M1 and M4 as shown in Figure 3-2. For an odd number of stages, all of the NMOS switches are controlled by an *Enable* signal, and likewise all of the PMOS switches are controlled by an  $\overline{Enable}$  signal (for simplicity, *Enable* will be used in reference to the differential signals).

We should note that there are many ring oscillator configurations that can be gated to hold phase information, including differential implementations. In fact,



differential delay elements are used in most TDC to achieve good differential non-linearity performance, mitigating the mismatch between rising and falling edges. For the GRO, however, the single-ended configuration shown in Figures 3-1 and 3-2 may be preferable to a differential one. As explained earlier in Section 2.6, the error from differential non-linearity is actually first-order shaped, and the single-ended topology has half the power and area.

### 3.1.2 Model for skew due to oscillator gating

As mentioned earlier, perfectly preserving the GRO phase state is equivalent to setting the initial quantization error  $T_{start}[k]$  equal to the final error of the preceding sample,  $T_{stop}[k - 1]$ , and is required to achieve ideal noise-shaping. In a practical implementation, however, we can expect that the analog quantization error is not preserved *perfectly*, and it is therefore important to understand the physical limitations as well as the implications of practical quantization error transfer. With this goal in mind, we begin by describing the issue of quantization error transfer in general terms, which then will provide a context for evaluating specific GRO implementations.

When the output of a delay element is in transition, there are a number of dynamic mechanisms that determine the location and movement of charge within the circuit. In Figure 3-3, for example, when the transition is interrupted by disabling the oscillator, the dynamics of the transition are replaced by an entirely new and distinct set of dynamics. For the interruption of a negative transition in Figure 3-3(a) or its inverted positive transition in (b), the charge will redistribute to satisfy an equipotential condition across the FET resistor that is left on, even in the disabled state. Upon enabling the delay element once again, the transition resumes, however we can see that the charge distribution within the cell is not the same as it was during the original transition. Moreover, it is also clear that the *amount* of charge redistribution depends on the state of the oscillator when *Enable* transitions low.

In addition to the charge redistribution within a delay element for transitioning *outputs*, there is also some charge redistribution during the disable time for delay elements that have an *input* in transition. As shown in Figure 3-4, both the switch

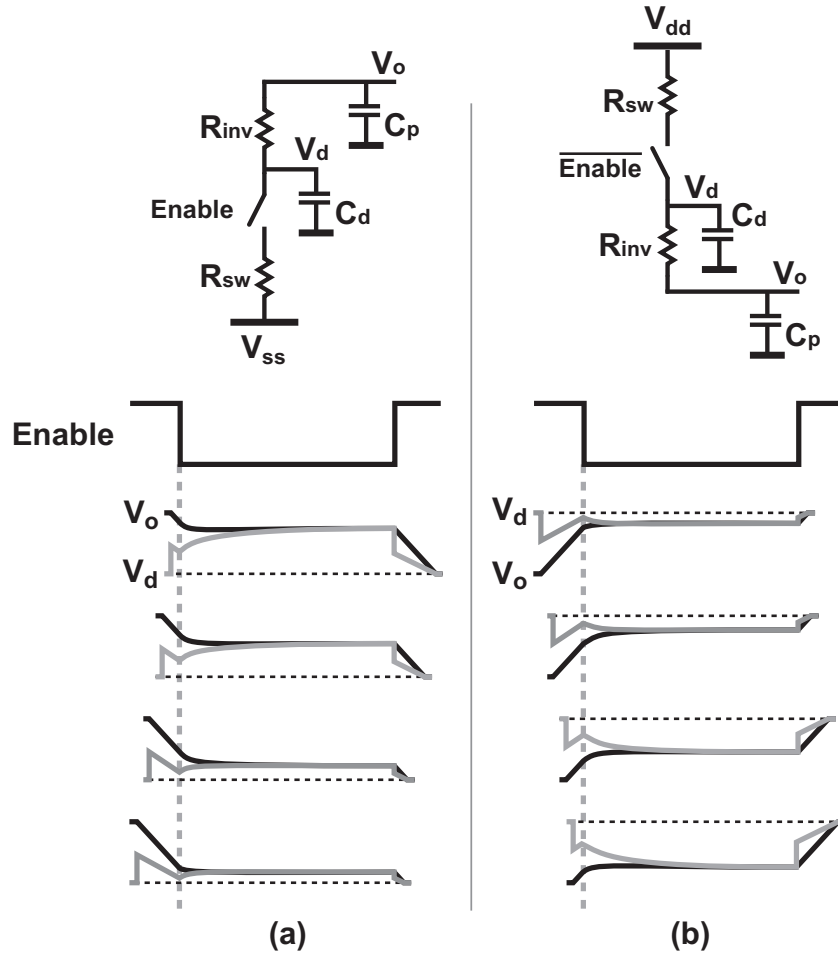


Figure 3-3 Conceptual picture of a transition being interrupted with a disable window. A negative transition is shown in (a), and the approximate inverse is shown in (b) for a positive transition.

drain voltages  $V_{d_p}$  and  $V_{d_n}$  and the output voltage  $V_{o_i}$  will be pulled towards the input voltage  $V_{o_{i-1}}$  until the respective inverter core transistor turns off. Compared to the case where the output is in transition, when the oscillator is enabled again most of the redistributed charge here will quickly move back close to its original distribution before the output begins to transition. While the charge redistribution for this case is seen as secondary, it may also have a small effect on precise quantization error transfer.

Since we now understand that the analog state information at the beginning of a measurement interval is not strictly equal to the final state of the GRO from the previous measurement, we now need to introduce this error in our mathematical

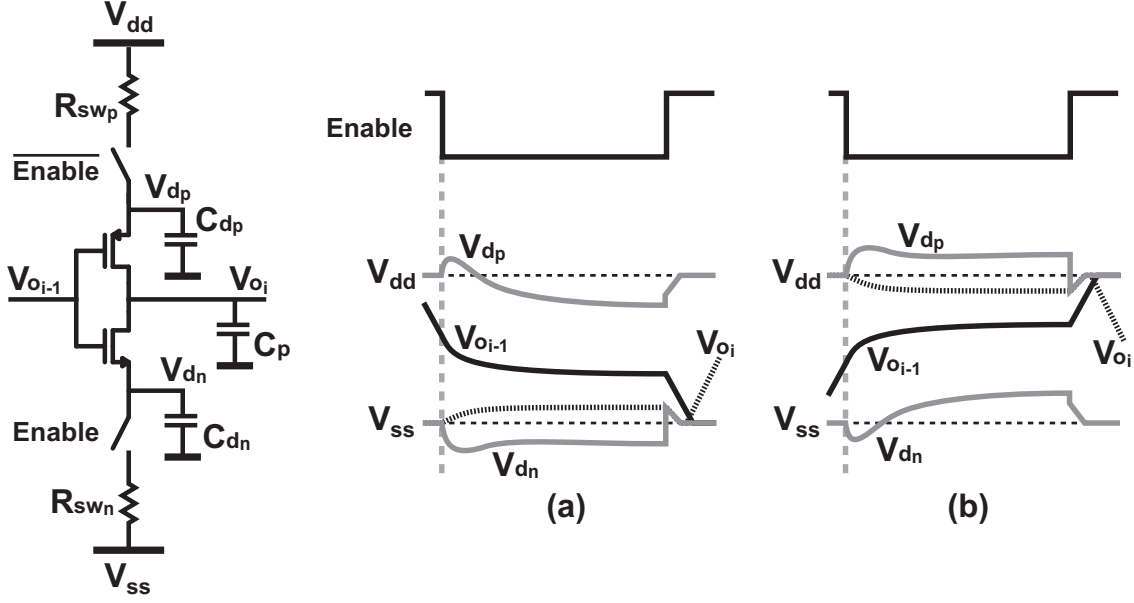


Figure 3-4 Conceptual illustration of how charge redistribution within a delay element depends on the input level

model. To do this, for each measurement  $k$  we first define a variable  $\hat{\theta}_{GRO}[k]$  that is equal to the GRO phase at the time when the negative *Enable* transition crosses mid-supply. Second, we recognize that  $T_{start}[k]$  will no longer be equal the value of  $T_{stop}[k-1]$ , and we define another time error,  $T_{skew}$  that is a function of GRO phase  $\hat{\theta}_{GRO}[k]$ .  $T_{skew}$  now models the corruption of the analog phase state as an unintended consequence of gating the oscillator by the relation

$$T_{start}[k] = T_{stop}[k-1] + T_{skew}(\hat{\theta}_{GRO}[k]). \quad (3.1)$$

As another illustration of this additional error,  $T_{skew}$ , in Figure 3-5 we compare the phase trajectory of an example GRO with its idealized piecewise linear phase trajectory before and after the oscillator is disabled for a length of time,  $T_{disable}$ . Since it is not physically possible to gate an oscillator off and on *instantaneously*, we can therefore expect a small amount of lag time, both when the GRO is disabled and again when oscillation resumes. An equivalent way to define  $T_{skew}$  is to take the difference between these two lag times, seen by extrapolating and subtracting the tangential phase trajectories.

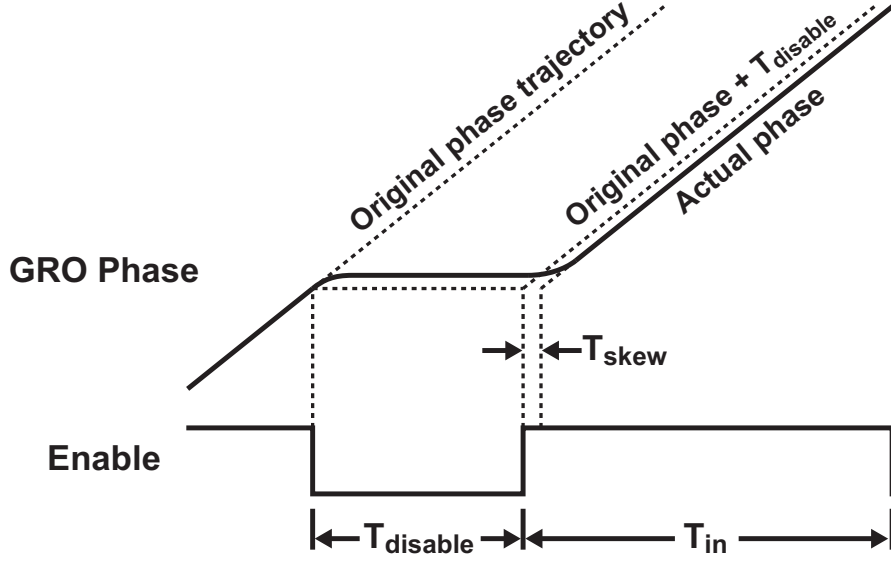


Figure 3-5 Phase trajectory skew (error) due to the physical non-idealities of gating an oscillator

As defined in Figure 3-5, we can see that to account for this,  $T_{skew}$  should be subtracted from the input measurement interval,  $T_{in}$ . On average, a positive value of  $T_{skew}$  will pull the quantized output to be slightly smaller than it should be, and similarly a negative value of  $T_{skew}$  will result in a slightly larger output. Mathematically, this can be seen when the measured GRO output time is given by

$$T_{out}[k] = T_{in}[k] - T_{skew}(\hat{\theta}_{GRO}[k]) - T_{stop}[k] + T_{start}[k]. \quad (3.2)$$

We can then continue to use Equation 2.2, stated again for convenience as

$$T_{out}[k] = T_{in}[k] - T_{error}[k], \quad (3.3)$$

where, by comparing with Equation 3.2,  $T_{error}$  is now expressed as

$$T_{error}[k] = T_{stop}[k] - T_{stop}[k-1] + T_{skew}(\hat{\theta}_{GRO}[k]). \quad (3.4)$$

Before we make comments on how the gating skew error affects the overall GRO output, first let us recall the discussion on oversampling considerations for classical

quantizers from the previous chapter in Section 2.4. The applicable part of this discussion is that the non-linear DC transfer characteristic of a classical quantizer can be made to *appear* linear only if the quantization error is adequately scrambled. Without scrambling, the output of the classical quantizer should be *expected* to be non-linear, especially for inputs that are small or that create distinct quantization patterns.

Because the gating skew error is also non-linear, adequately scrambling  $T_{skew}$  by randomizing  $\hat{\theta}_{GRO}$  can also linearize the TDC behavior in the same manner that the classical quantizer can be linearized. In this linear approximation, we can expect that the GRO-TDC will have two non-physical noise profiles, a first-order noise-shaped quantization error in addition to a white noise floor due to the skew error. The required scrambling action can be accomplished by a combination of methods, including random physical processes such as 1/f and thermal noise, intentional randomization of the input signal through dithering, and pseudo-random patterns such as the shuffling of delay element mismatch.

However, a lack of scrambling will leave the non-linearity to cause complex effects in the quantizer output, especially when the converter is placed in a feedback system. One example of these effects is the appearance of a deadzone in the quantizer DC transfer characteristic, which will be discussed in Section 3.1.4. Generally avoiding these effects is a very difficult challenge, and moreover the noise-shaping benefit of the GRO-TDC architecture may be not be realized at all without a scrambled GRO phase. Therefore, it is important to understand the root cause of this gating skew error in more detail so that it may be minimized and appropriately scrambled by design.

### 3.1.3 Gating skew analysis

With the framework for understanding skew already established, we now will turn to identifying the mechanisms and variables that can affect  $T_{skew}$  by altering charge within the delay cell. To this end, we begin with a cartoon of the gating skew for an inverter-based GRO as shown in Figure 3-6. At the top of the figure, we see that the

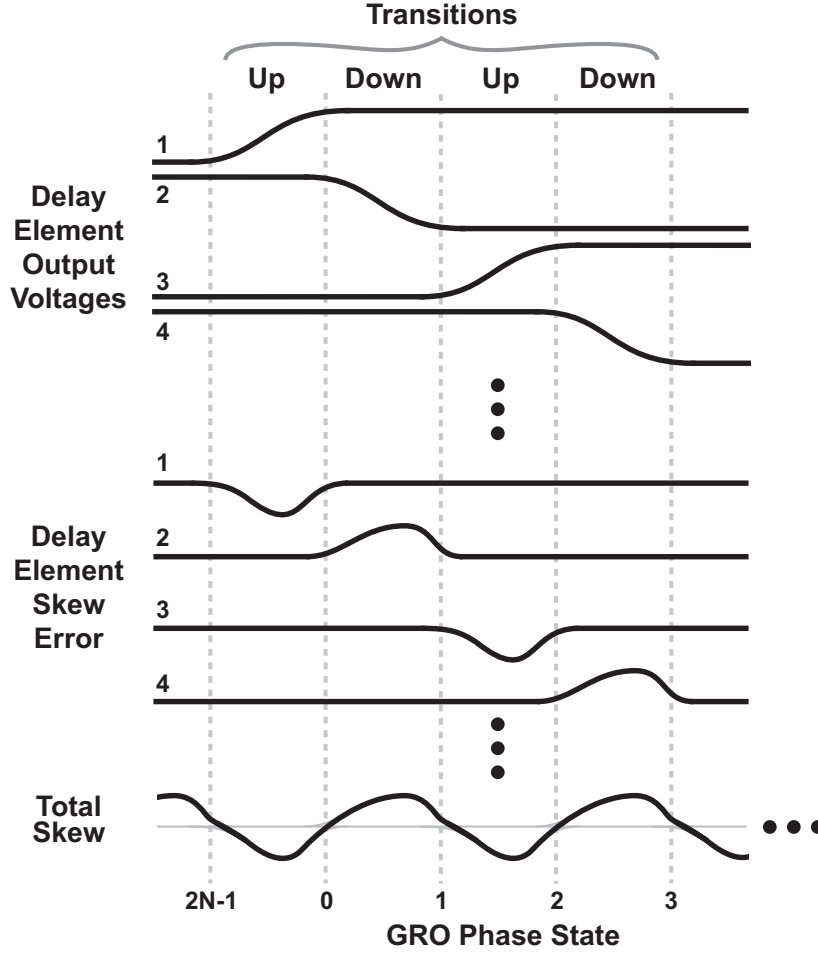


Figure 3-6 Concept of how the gating skew error for an inverter-based GRO is the sum of the skew from the positive and negative transitions

alternating delay element output sequence of positive and negative transitions as a function of the GRO phase state,  $\hat{\theta}_{GRO}$ , which is equivalent to a transient view of the output voltages during normal oscillation.

Next, in the center of Figure 3-6, we depict the contribution from each individual delay element to the gating skew error,  $T_{skew}$ . While the actual shape and magnitude of the error contributions shown here are conceptual, in practice we do know that each delay element only contributes to the overall  $T_{skew}$  while its input or output transitions between logic levels. We also can expect that the contribution from the rising and falling transitions will be somewhat different from each other.

Last, on the bottom of Figure 3-6, we show that the overall skew error is simply the

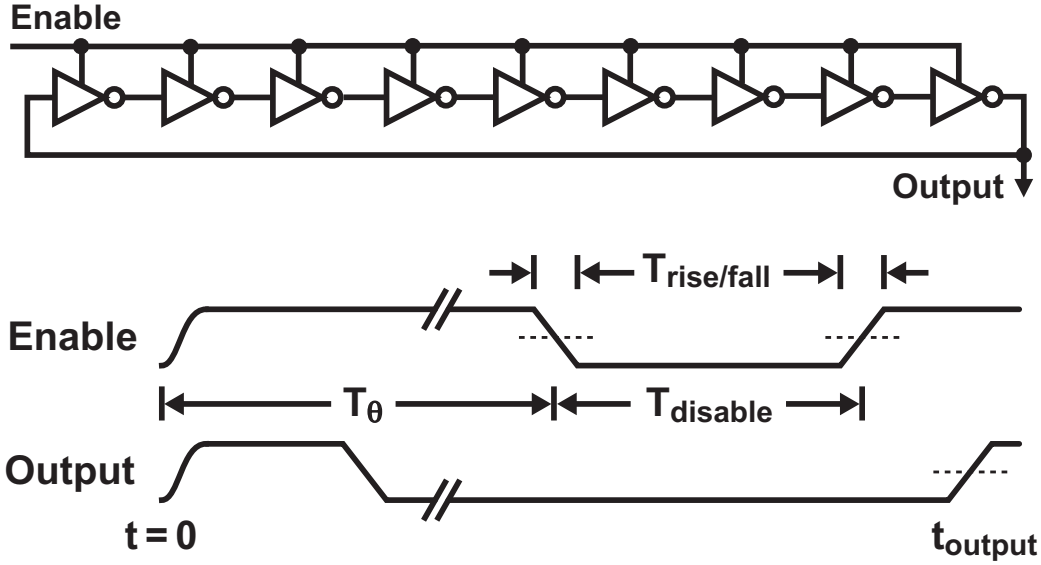


Figure 3-7 Simulation testbench to characterize  $T_{skew}$  as a function of  $\hat{\theta}_{GRO}$

combination of the individual contributions from each delay element, which reveals a periodicity to the skew error of  $2T_q$  due to the difference between the rising and falling transitions, or alternately the difference between the NMOS and PMOS transistors. For example, we can expect that since the PMOS switch transistors are twice as large as the NMOS, the amount of charge injected from the PMOS will similarly be twice the amount of charge injected from the NMOS. While we acknowledge that this simplistic decomposition of GRO skew lacks precision, it does provide a backdrop for understanding the complex features of the error.

To gain a more empirical view of gating skew for the inverter-based GRO, we can simulate  $T_{skew}$  as a function of the GRO phase state  $\hat{\theta}_{GRO}$  at the transistor-level in Spectre (SPICE) for a variety of conditions using the testbench shown in Figure 3-7. For each curve,  $\hat{\theta}_{GRO}$  is swept by stepping  $T_\theta$ , which successively moves the falling edge of *Enable* across the GRO states. After a disable time  $T_{disable}$ , the oscillator is enabled again and allowed to reach steady-state. We then monitor the time  $t_{output}$  at which a GRO delay element output transitions. Finally, the value of  $T_{skew}$  is calculated from  $t_{output}$  by subtracting the disable time, and then comparing to a reference time of  $t_{output}$  that is obtained from a simulation with no disable window.

The primary simulation parameters (excluding  $\hat{\theta}_{GRO}$  or  $T_\theta$ ) are the length of the

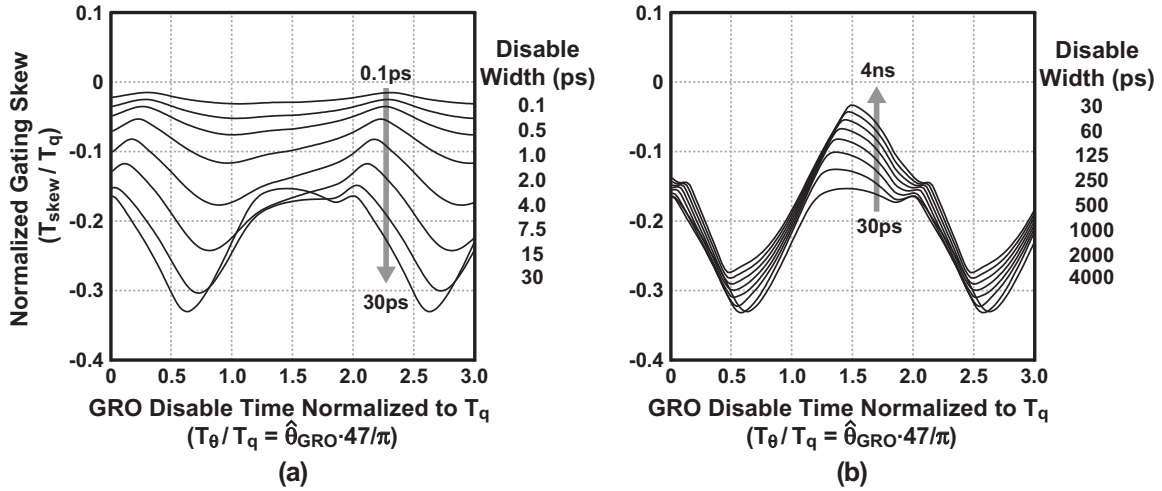


Figure 3-8 Gating skew  $T_{skew}$  as a function of  $\hat{\theta}_{GRO}$  for stepped values of disable width ( $T_{disable}$ ) from (a) 0.1-30ps and (b) 30-4000ps. The *Enable* rise and fall times are held constant at 0.5ps.

disable time and the rise/fall times of the *Enable* signal. As shown in Figure 3-7, *Enable* signals are constructed with piecewise linear voltage sources, and the length of the disable time is taken from the 50% crossings of the supply. SPICE models for a standard  $0.13\mu\text{m}$  CMOS process with ideal matching are used throughout.

A first simulation to examine varies the width of the disable time with a very fast rise/fall time that is held constant at 0.5ps, which is close to the ideal case of zero-width rise and fall times but large enough to avoid convergence issues. Because many charge transfer mechanisms occur with exponential time constants, the disable width is stepped from 0.1 to 4000ps with approximately logarithmic increments. Figure 3-8 plots the results from this simulation, where (a) displays  $T_{skew}$  for short disable widths of 0.1ps to 30ps, and (b) corresponds to the longer values of  $T_{disable}$ , ranging from 30ps to 4,000ps.

By looking at these results, there are a few immediate observations on which to comment. First, we can see in Figure 3-8(a) that as the disable width decreases,  $T_{skew}$  limits to a zero-value, which is the same as the reference simulation with no disable at all. Although this result is what intuition would suggest, it is satisfying to see that the unrealistically fast *Enable* transients do not cause non-physical behavior in the



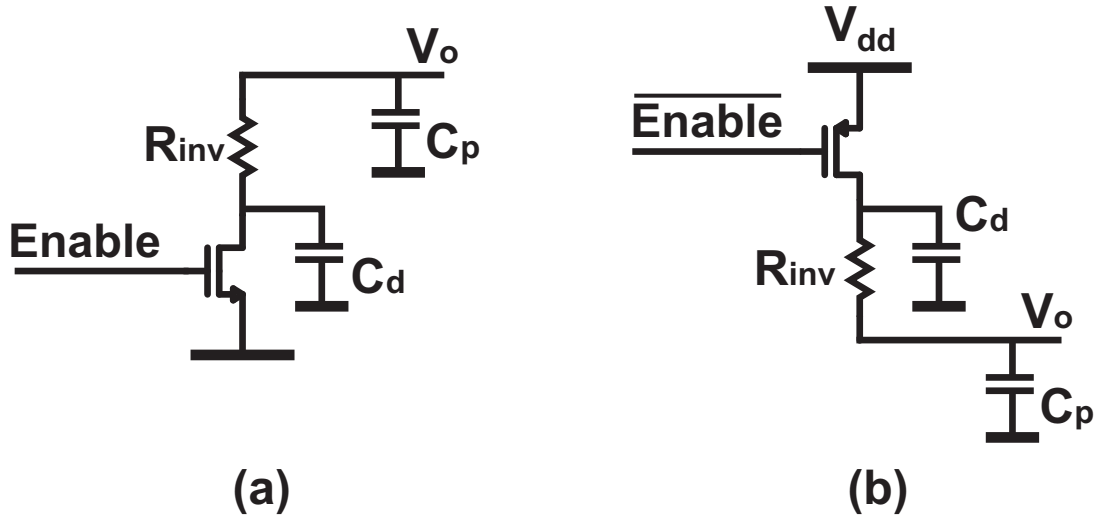


Figure 3-9 Schematic depicting two time constants present in the charge redistribution within a delay element whose output is in transition at the disable time

simulation. Second, we can verify that  $T_{skew}$  is indeed periodic with  $2T_q$ , as predicted by Figure 3-6. Last, as we can see clearly by the separation of Figure 3-8 into (a) and (b), there are at least two time constants that dominate the motion of charge in the inverter cell.

To explain the presence of more than one time constant, consider that when the transition is interrupted, either the top or bottom of the inverter is open, with the schematics for both cases drawn earlier in Figure 3-3, and shown here again for convenience. When a GRO transition is disabled, the switch transistors turn off and the charge in the switch transistor channels quickly diffuses, approximately half moving to the supply and the other half into the inverter core. The capacitance at the inverter drain,  $C_d$ , will at first absorb this charge injection at a rate determined by the first time constant, and then eventually the voltage across  $R_{inv}$  will settle to zero at a rate determined by the second time constant. Additional error with long time constants may arise from delay elements with interrupted transitions at the input, since these transistors are very weakly on and can have very large impedances.

Next, we know that the rise and fall times of *Enable* are practically much larger than 0.5ps, which means that the turn-on time of transistors will depend on interaction between the voltages within the GRO core and the voltages of *Enable*. We show

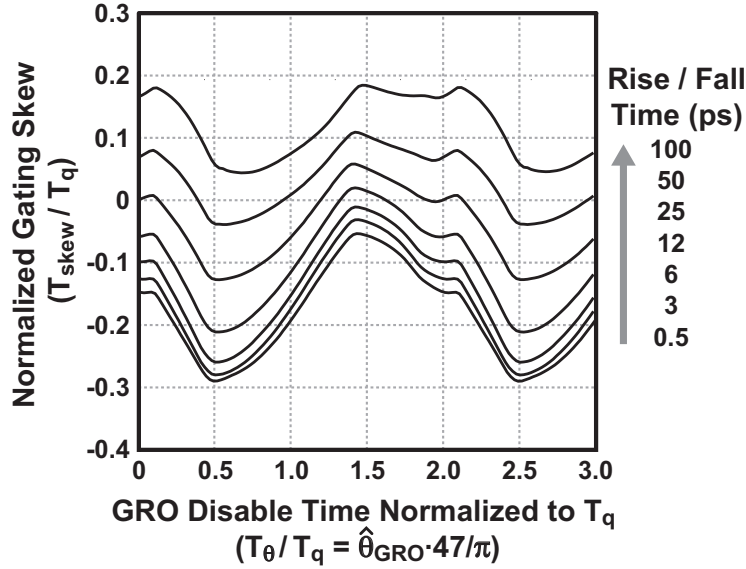


Figure 3-10  $T_{skew}$  as a function of  $\hat{\theta}_{GRO}$  for stepped values of rise and fall time ( $T_{rise/fall}$ ) from 0.5-100ps. The disable width is held constant at 1,000ps.

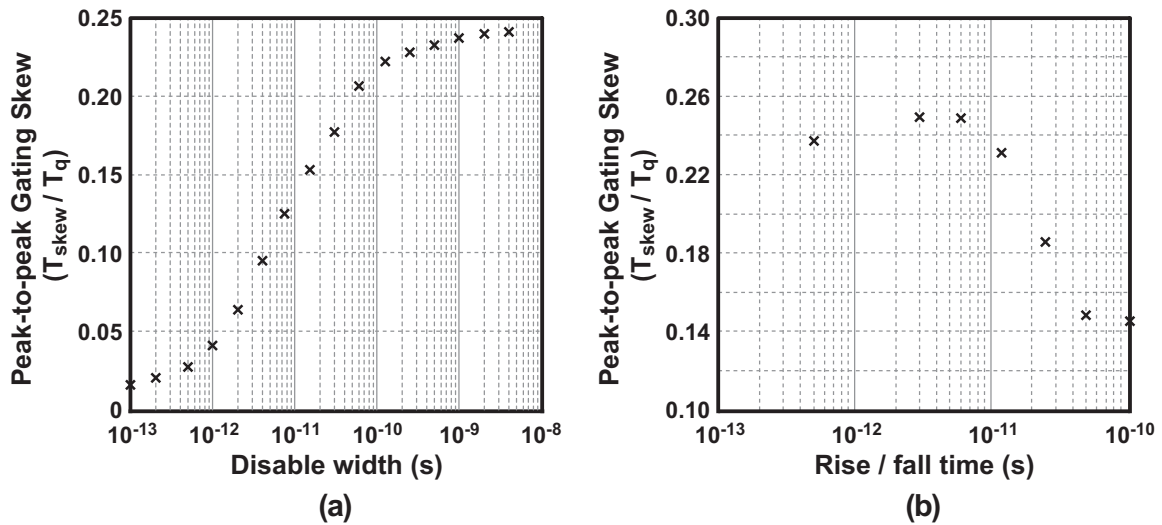


Figure 3-11 Peak-to-peak  $T_{skew}/T_q$  plotted vs. (a) disable width and (b) rise / fall time

in Figure 3-10 the results of another simulation, this time with varied rise and fall time and a constant disable time. An interesting thing to note here is that longer rise and fall times effectively smooth out the peaks of the skew function, yet maintain the same overall shape with surprising consistency.

Another perspective to view these same results is by plotting the peak-to-peak magnitude of  $T_{skew}$  vs. disable width and rise / fall time. Because the detrimental

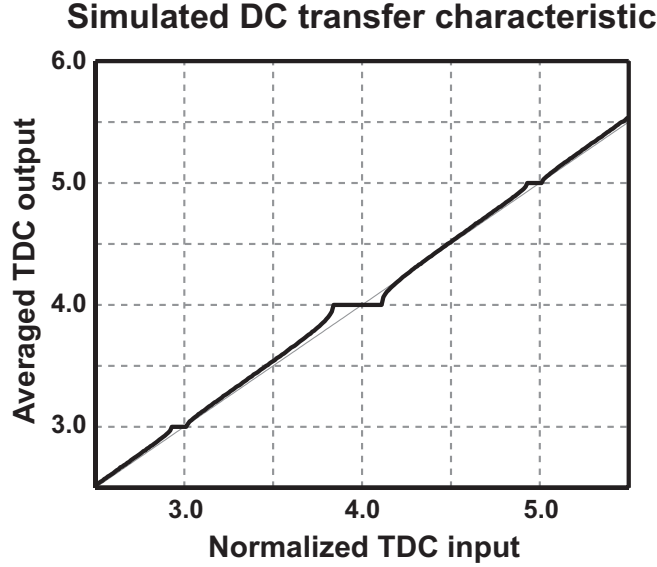


Figure 3-12 Simulated deadzones in the DC GRO-TDC transfer curve caused by gating skew

effects of skew are caused by variation of  $T_{skew}$  with GRO phase, the DC offset is irrelevant and can be removed. In Figure 3-11(a), we again can see the significant changes in error magnitude for small disable widths, which have been explained already by the charge redistribution, and in (b) the slight decrease of  $T_{skew}$  with larger rise / fall times can clearly be seen. Specifically,  $T_{skew}$  starts with a peak-to-peak deviation of about  $0.23T_q$  for fast rise / fall times, and then weakens to about  $0.14T_q$  for 100ps transitions. Thus, while a longer slope to *Enable* may be detrimental in terms of jitter, in this case it actually contributes a small amount of "averaging" that could be seen as helpful in terms of gating skew error.

Due to the shallow slope of  $T_{skew}$  versus disable width for large values of  $T_{disable}$  seen in (a), we can say that in a standard  $0.13\mu\text{m}$  CMOS process there is relatively little charge lost to switch leakage. In deep sub-micron process technologies, however, it is possible that subthreshold and gate leakage will present another source of error that will change the shape and dependence of  $T_{skew}$  as a function of  $\hat{\theta}_{GRO}$  and  $T_{disable}$ .

### 3.1.4 Deadzone effects

As mentioned earlier, many complex and interesting non-linear effects in the TDC output can be caused by the gating skew error if the GRO phase is not scrambled adequately. One important effect of the non-linear quantization error transfer is that deadzones can be found in the GRO-TDC DC transfer characteristic. Since this is a very standard measure for converter accuracy, it is worthwhile to understand this issue in more detail.

As an example of this deadzone effect, Figure 3-12 plots a simulated DC transfer characteristic using a behavioral model for the GRO-TDC. The MATLAB model is based on Equation 3.2, where the value for  $T_{skew}$  comes from the Spectre simulation results described earlier. For each data point, the MATLAB inputs a constant signal, allows the GRO-TDC to reach steady-state, and then averages a large number of repeated conversions.

To explain the deadzone behavior, we first consider that the non-linearity occurs most prominently when the input to the converter is close to an integer multiple of twice the delay  $T_{in}[k] - 2MT_q = \epsilon_T$ , where  $\epsilon_T \ll T_q$ . Notice that in this case, the quantization error at the end of a measurement interval is very close to the error at the beginning of the interval. Mathematically we can see this as

$$T_{stop}[k] - T_{start}[k] = \epsilon_T. \quad (3.5)$$

By substituting this into Equation 3.1, we also have that

$$T_{stop}[k] = T_{stop}[k - 1] + T_{skew} \left( \hat{\theta}_{GRO}[k] \right) - \epsilon_T. \quad (3.6)$$

In this expression, we can again see that the gating skew will push and pull the GRO phase with a magnitude and direction determined by the phase of the previous measurement. However, we can also see here that if the magnitude of  $T_{skew}$  is larger than  $\epsilon_T$ , then the influence of  $T_{skew}$  on the TDC output is also larger than it is for  $\epsilon_T$ . Recall that in the ideal GRO, where  $T_{skew} = 0 \forall \hat{\theta}_{GRO}$ , even very small values of

$\epsilon_T$  will slowly accumulate over time and eventually cause the TDC output to change. With the presence of a large, unwanted error that is a periodic function of the GRO phase, the GRO will be pulled until a steady-state is reached. We can expect that the gating skew error in a steady-state deadzone will be given by

$$T_{skew}(\hat{\theta}_{GRO}[k]) = \epsilon_T. \quad (3.7)$$

With this insight, a few comments can be made on the deadzones. Notice that in Figure 3-12, the *even* integer values exhibit larger deadzones than the *odd* integers, which is consistent with the periodicity of  $T_{skew}$ . However, if mismatch were to be added, we would expect the period of  $T_{skew}$  to be equal to the GRO oscillation period,  $2NT_q$ . Therefore, practical deadzones are likely to be most severe when the GRO is stopped on the exact same delay element transition for each measurement, which is similar to injection-locking the GRO with the TDC sampling frequency. In this case, we need to either provide a large amount of GRO phase scrambling, or reduce the magnitude of  $T_{skew}$  *far* below that of random physical processes internal to the GRO.

### 3.1.5 Improving the gating sensitivity function

In this example GRO-TDC implementation, it is clear that the non-linearity due to stopping and starting the oscillator can prevent the converter from fully realizing the noise shaping that gives the architecture its advantages. Although the effective TDC resolution has some benefit even from non-ideal noise shaping, at this point it is still far from the physical noise limits of the architecture. To significantly improve the effective TDC resolution to 1ps and below, we need a more sophisticated GRO implementation than the example shown in Figure 3-2.

One approach to consider in reducing the *effective* non-linearity error,  $T_{skew}$ , would be to provide random dithering of the TDC input as suggested earlier for deterministic TDC in Section 2.4. Indeed, this technique would rid the TDC of deadzones by scrambling the GRO phase, and also results in a “white” noise floor that is limited by  $T_{skew}$ . Although oversampling could be now be used to filter noise outside the band of

interest, this approach moves away from the strength of the gated ring oscillator TDC, namely the ability to inherently achieve noise-shaping of quantization and mismatch errors with a simple architecture.

As an alternative to intentional dithering, we can consider optimum sizing of transistors within the inverter delay cell to reduce the magnitude of  $T_{skew}$  within the inverter-based GRO architecture of Figure 3-2. However, this approach can improve the raw magnitude of  $T_{skew}$  by only a small amount, and even this small improvement is not robust across processes, power supply voltages, etc.

Finally, let us consider the approach to reduce the magnitude of  $T_{skew}$  through interpolation or averaging. We have seen in Figure 3-6 that the gating skew is composed of contributions from alternating positive and negative transitions. If multiple skew contributions can be averaged together, then it may be possible to scale both the gating skew as well as the effective oscillator delay,  $T_q$ . Therefore, we proceed to consider architectural modifications to the GRO of Figure 3-2 that can achieve sub-gate-delay raw resolution.

## 3.2 Multi-Path Gated Ring Oscillator

In this section, we first explore the suitability of various sub-gate-delay ring oscillator topologies for implementing a gated ring oscillator. We then identify the most promising of these architectures to be the multi-path oscillator, and follow with a detailed analysis, considering especially the critical architectural issues and tradeoffs for use as a gated ring oscillator. Next, we present a design methodology and circuit details for use within a prototype GRO-TDC, and then revisit the issue of quantization error transfer accuracy, or gating skew. We demonstrate through simulations the marked improvements in gating skew error using the proposed multi-path oscillator compared to the simpler inverter topology discussed previously in Section 3.1.3, and provide a physical explanation for the improved skew performance.

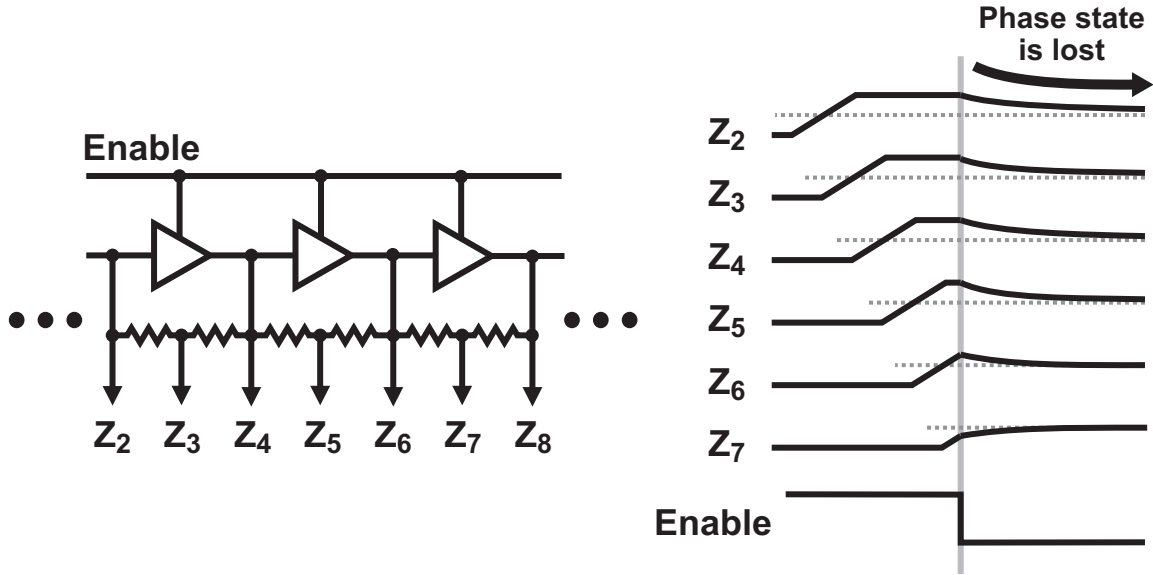


Figure 3-13 Illustration of the problem in using resistive interpolation for the GRO

### 3.2.1 Achieving sub-gate-delay raw resolution

Earlier in Section 2.3, a few techniques for creating sub-gate-delay TDC resolution were discussed. Due to geometric similarities, the approaches commonly used in cyclic TDC are of particular interest for application to the GRO. For example, it is natural to consider the interpolating technique implemented either with rings of resistors or with transistors. In addition to oscillators within the TDC community, research in precisely generating multi-phase signals for fixed-frequency phase and delay-locked loop applications have also investigated similar ideas that can be considered for the GRO [11, 12, 16, 31, 35, 36, 38, 42, 63].

The resistor ring often used in multi-phase oscillator applications is able to generate very high-resolution and low differential non-linearity, however we can quickly see that this particular topology has fundamental problems for the gated ring oscillator. To explain, Figure 3-13 applies the concept of resistive interpolation to the gated ring oscillator, with the assumption that a differential delay element structure would be used in practice. Although the power and area penalty of the differential structure can be tolerated for the GRO (as discussed earlier in Section 3.1.1), the main issue here is that when the GRO is disabled, current will continue to flow in the resistor

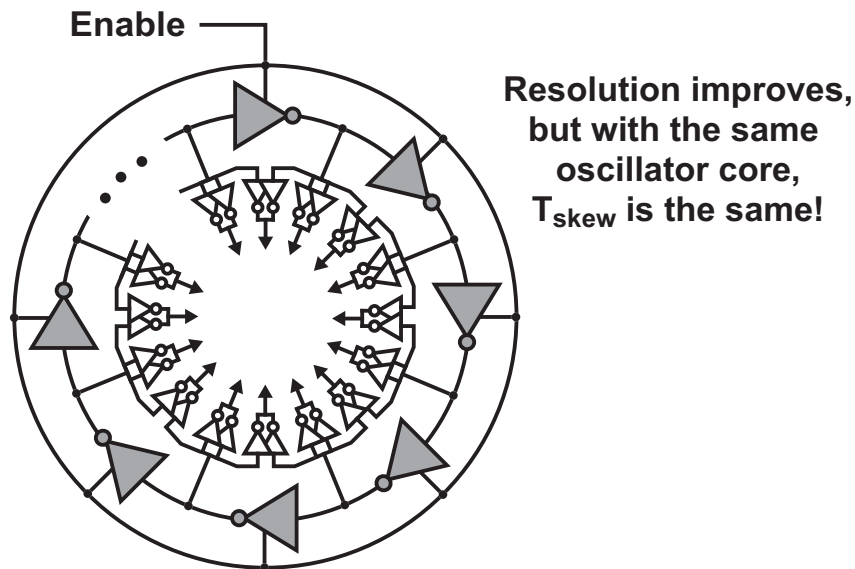


Figure 3-14 A GRO topology with digital interpolation

ring. The effect of resistor averaging which is quite useful for dynamic phase interpolation will actually destroy the analog phase information during the disabled state. We can conclude that for the GRO, at least in the disabled state, each delay element cell should be held in isolation so that charge does not escape.

Since resistors are problematic for the GRO, it may seem logical to replace the resistors with digital gates as the interpolating elements (as in Figure 2-8 [16,63]). In this case, digital gates can be isolated so that charge does not flow between stages. However, this approach is also flawed for application to the GRO, since interpolation's primary advantage of reducing the raw quantization error does not address the fundamental issue of gating skew. Recall that for the GRO, raw quantization and mismatch error is noise-shaped, and therefore not a primary concern. Rather, the problem with the GRO is that the gating skew error,  $T_{skew}$ , arises from the alternating sequence of positive and negative transitions *within* the active core of the oscillator. Therefore, significant improvement of  $T_{skew}$  by means of reducing  $T_q$  will only be possible if the oscillator core itself is modified.

As shown in Figure 3-15, one possibility for modifying the oscillator core is to couple together  $M$  multiple oscillators, each with  $N$  stages. This architecture also creates sub-gate-delay resolution, theoretically reducing the effective delay per stage



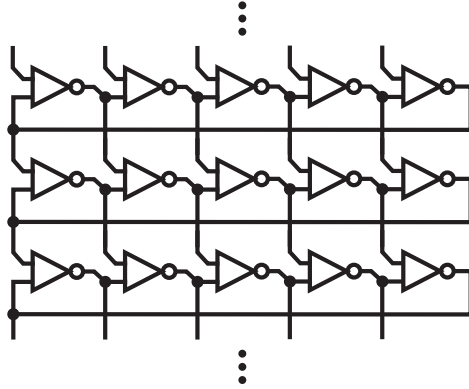


Figure 3-15 Coupled oscillators used to reduce the effective delay per stage

by a factor of  $M$  [36,38]. One issue that must be carefully considered for a system of coupled oscillators is the stability of oscillation within the primary mode, which is defined by adjacent delay elements transitioning in sequence around the ring. A large coupling factor between the  $M$  oscillators can ensure stability in the primary mode, however increased coupling also has the undesired effect of slowing down the transitions.

Oscillators that operate continuously (e.g. for PLL and DLL applications) may well be able to support an initial reset operation that establishes the primary mode. However, the very premise of the GRO is that it will be stopped and started at the same phase state *with no intervention or reset operation*. While we are concerned with reducing the delay of each stage as much as possible, at the same time we need to achieve a well-defined oscillation *through the gating operation*. Therefore, robust oscillation in the primary mode is a critical requirement for the GRO design.

Another possibility for creating sub-gate-delay resolution that is quite suitable for the GRO is shown in Figure 3-16. In this multi-path topology, each delay element uses state information from more than one output stage to determine when to begin its transition. Interestingly, the coupled oscillators we just discussed are a subset within the category of multi-path oscillators, because the coupling requires contribution from more than one element per node. However, we can optimize the multi-path oscillator for the GRO application with more degrees of freedom than the coupled oscillator. For example, the multi-path topology is not restricted to having  $M \cdot N$  stages, and a

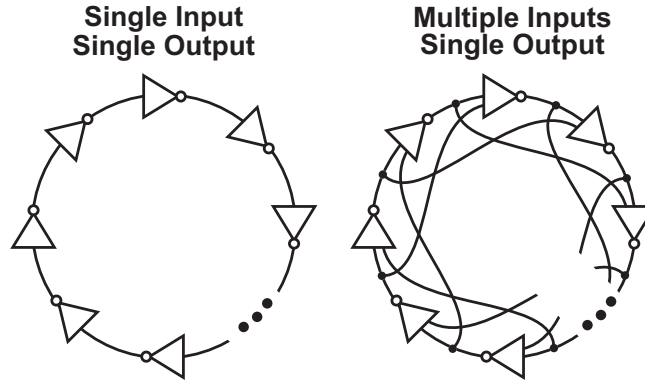


Figure 3-16 Basic concept of using multiple inputs for each delay stage

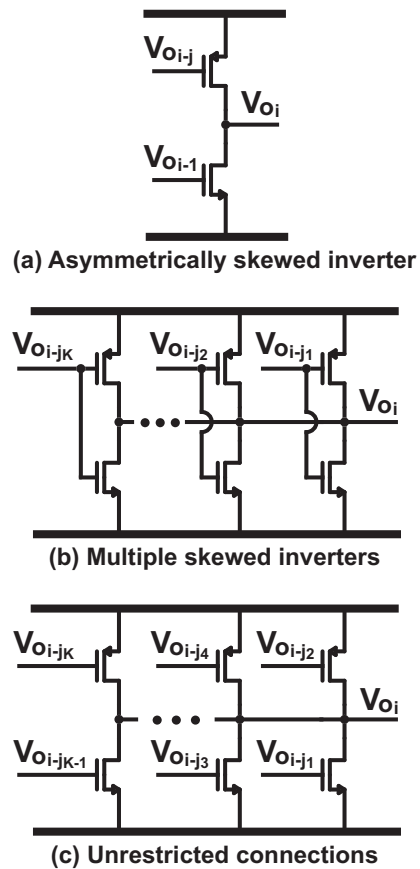


Figure 3-17 Techniques to reduce effective delay by modifying the standard inverter

primary oscillation mode can more easily be established.

One example of this multi-path topology is to modify the standard two-transistor inverter delay cell by asymmetrically connecting the PMOS and NMOS inputs to different delay stage outputs [35]. With the transistor drains both connected to the

output of the stage  $V_{o_i}$ , as shown in Figure 3-17(a), the NMOS gate connects to the output of the immediately preceding stage  $V_{o_{i-1}}$ , and the PMOS gate connects to an output  $V_{o_{i-j}}$  occurring  $j$  stages prior. By skewing the arrival of the input transition to the slower PMOS transistor, the effective delay through the stage is reported to be reduced by a factor of 2 [35].

Another ring oscillator topology has been proposed for differential circuits [41], with a simplified single-ended version shown in Figure 3-17(b). Here,  $K$  multiple symmetric inverter outputs are connected in parallel to  $V_{o_i}$ , however the inverter inputs are skewed by connecting to  $K$  delay stage outputs  $\{V_{o_{i-j_1}}, V_{o_{i-j_2}}, \dots, V_{o_{i-j_K}}\}$ . By optimizing the number, placement, and weight of the connections, each stage begins to transition before the full transition of the immediately preceding stage is completed such that the effective delay through the stage is minimized. Stable oscillation in the primary mode can also be assured through proper design, with a reduction of the gate delay again reported to be a factor of 2.

We now consider that each of these two techniques in Figure 3-17(a) and (b) can be combined together to result in an unrestricted set of transistor connections as shown in Figure 3-17(c). In the proposed topology,  $K$  transistors connect to a set of output stages  $\{V_{o_{i-j_1}}, V_{o_{i-j_2}}, \dots, V_{o_{i-j_K}}\}$ , which gives the designer a much larger optimization space compared with Figures 3-17(a) and (b). Specifically, the connection and size of *each* transistor in the delay cell can be *independently* adjusted, and the overall design can be fully optimized to decrease the effective delay while maintaining a stable, robust oscillation.

To describe a particular oscillator design, let  $J$  be the set of integers  $\{j_1, j_2, \dots, j_K\}$  that describe specific input connections  $\{V_{o_{i-j_1}}, V_{o_{i-j_2}}, \dots, V_{o_{i-j_K}}\}$  corresponding to an output  $V_{o_i}$ . Next, let  $W$  be the collection of normalized drive strengths  $\{w_1, w_2, \dots, w_K\}$  ( $w$  corresponds to transistor width assuming minimum length devices and adjustment for the relative strength of complementary devices), where  $\sum_{k=1}^K w_k = 1$ . We also define  $\bar{J}$  as the *weighted average* of  $J$ , or

$$\bar{J} = \sum_{k=1}^K w_k \cdot j_k \quad (3.8)$$

To make use of these definitions, we first consider a standard ring oscillator with  $\bar{J} = 1$ . Not coincidentally, we find that the oscillation period is equal to  $T_{osc} = 2NT_{inv}/\bar{J}$ . Here  $T_{inv}$  is the delay of a standard inverter, and  $N$  is the number of stages. While this is convenient for the case of the standard inverter ring, to be more general we say that  $\bar{J}_{eff}$  is the *effective* weighted average of  $J$ , defined when the period for *any* ring oscillator is given by

$$T_{osc} = \frac{2NT_{inv}}{\bar{J}_{eff}} \quad (3.9)$$

To continue, we next can consider a multi-path ring oscillator with accelerated transitions that reduces the oscillation period to  $T_{osc} = 2NT_q$ . By combining with Equation 3.9, we have

$$T_q = \frac{T_{inv}}{\bar{J}_{eff}}. \quad (3.10)$$

From this result, the designer may be tempted to reduce  $T_q$  by increasing  $\bar{J}_{eff}$  as much as possible, however, there are a number of practical considerations that limit its attainable value. First, consider that only connections to the previous  $(N - 1)/2$  stages are useful for primary mode oscillation, and a more practical rule is to restrict  $J$  to a maximum of  $N/3$ . Therefore, achieving a large value of  $\bar{J}_{eff}$  requires a large number of stages, which in turn requires larger area.

Second, we need to consider the stability of the oscillator. If  $J$  is large, and/or concentrated heavily at  $N/3$  without a distributed contribution over the entire range of  $J$ , secondary oscillation modes become difficult to suppress, especially in the presence of mismatch. While using a prime number of stages can be helpful in this regard, a conservative design should have at least one input connection with some weight for every 4 stages to ensure that transitions occur in the proper sequence. We will later see that this strategy is also helpful in reducing the gating skew.

Finally, the larger values in  $J$  will typically add more parasitic wiring capacitance to the delay element output, since these elements need to be placed further away. Moreover, the parasitic capacitance will also become more important when multiple connections with small weights are chosen. We then introduce  $\eta$ , an *efficiency* factor

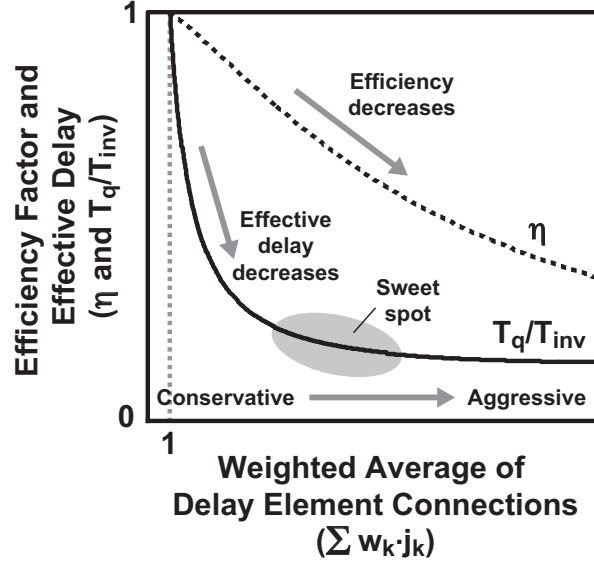


Figure 3-18 Example tradespace for optimizing the resolution of a multi-path oscillator operating in its primary mode by considering the weighted average of  $J$

that takes into consideration switching transients and wiring parasitics to result in

$$\bar{J}_{eff} = \eta \bar{J} = \eta \sum_{k=1}^K w_k \cdot j_k. \quad (3.11)$$

As an example tradespace shows in Figure 3-18, an optimal design in terms of resolution should not just consider the weighted average of  $J$ , but also its product with  $\eta$ . Fortunately, in general this efficiency factor degrades smoothly, and can be estimated by including including crude parasitic wiring capacitance models in the transistor-level simulations.

### 3.2.2 Design of the Proposed Multi-Path GRO

The delay cell from Figure 3-17(c) can be easily modified to accommodate the gating functionality by again placing appropriate switches above and below the inverter core as shown in Figure 3-19. In the same manner as was described earlier in Section 3.1.1, all impedances are high in magnitude during the disabled state, which will approximately preserve the oscillator state in between measurements.

With the delay cell building block now defined, let us consider the number of stages

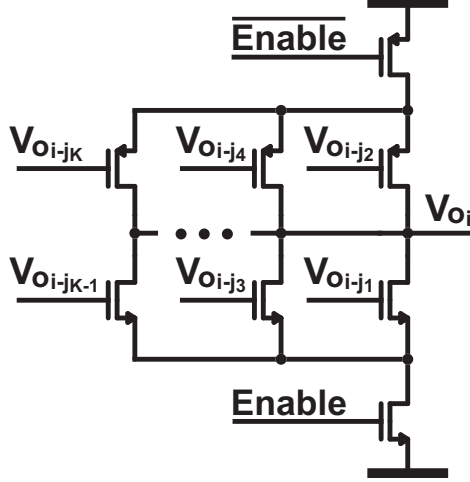


Figure 3-19 Delay cell topology for the proposed gated ring oscillator

$N$  that is appropriate for use in the GRO-TDC application. Counting and measuring the GRO outputs with standard digital logic places an upper bound on the oscillation frequency of 2GHz, which is a period conservatively equal to ten inverter delays in the  $0.13\mu\text{m}$  CMOS process. For a minimum design goal of  $\bar{J}_{eff} \approx 5$ , this implies that the number of stages  $N \approx 50$ . An upper bound on  $N$  is less strict, and is determined primarily by practical limitations such as the number of connections per stage and silicon area (for the same set  $J = \{j_1 \dots j_K\}$ , a larger  $N$  does not reduce  $T_q$ ). Another issue for choosing  $N$  is that a prime value inherently has better rejection of undesirable modes than does a value of  $N$  with large odd factors, such as  $45 = 3 \cdot 15 = 5 \cdot 9$ . As a result of these considerations, we propose here that  $N = 47$ .

To set the delay cell transistor connections and sizes, we use a soft approach based on empirical simulation results in combination with the desire to minimize layout complexity and area. A useful metric for evaluating designs is the power-delay product, which can achieve a local minimum for a well-designed multi-path oscillator. Another useful indicator of stability, albeit somewhat qualitative, is the steady-state start-up time of the oscillator when given a minor charge injection onto one of the oscillator nodes.

Although simulation is used for final assignment of connections and weights, there are a number of guidelines that are also useful to generate a first-pass design that

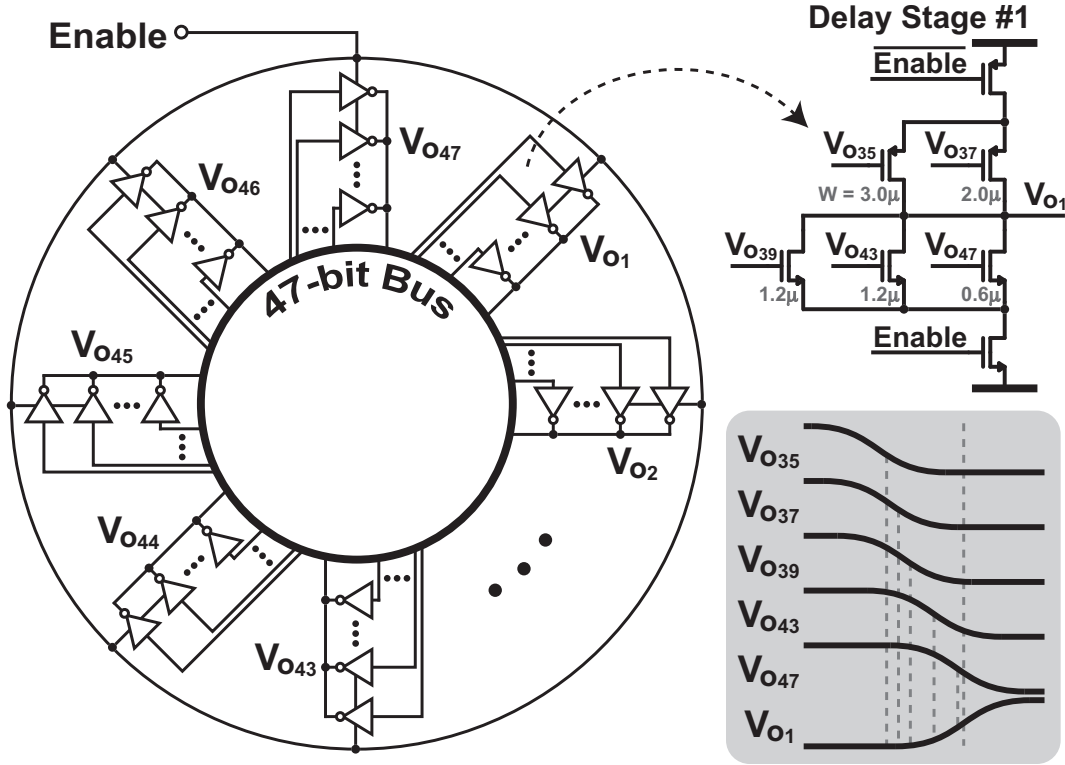


Figure 3-20 Schematic of the proposed multi-path GRO

is relatively close to optimal. As discussed earlier in regard to Figure 3-17(a), connecting the slower PMOS transistors to the largest values in  $J$  results in a better efficiency. Depicted in Figure 3-20, the PMOS connections are then made to the 13th and 11th preceding stages  $\{V_{oi-13}, V_{oi-11}\}$ , while NMOS connections are made to  $\{V_{oi-9}, V_{oi-5}, V_{oi-1}\}$ . Whereas the PMOS connections establish the maximum value of  $J$  close to  $N/3$ , the NMOS connections are distributed to efficiently establish the fundamental oscillation mode with minimal penalty in speed.

In terms of sizing, a larger weight is assigned to the connections with longest distance, with only a small drive from the immediately preceding stage. To facilitate a compact and simple layout as shown in Figure 3-21, the same number of equal-width fingers (5) is used for each of the four levels in the transistor stack (PMOS switch, PMOS inverter, NMOS inverter, NMOS switch). For optimal power and speed, the switch transistors are sized wider than the total width of the inverter core transistors. A summary of  $J$  and  $W$  is given in Table 3.1.

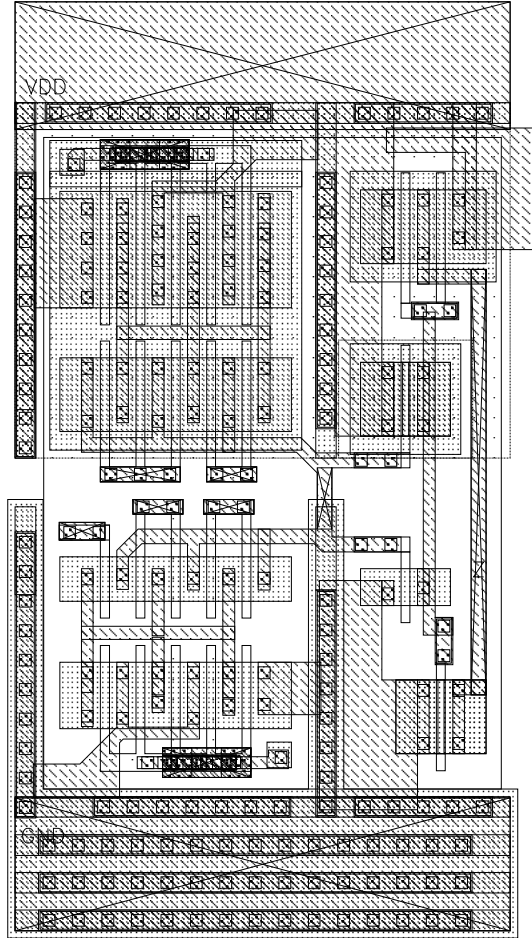


Figure 3-21 Inverter delay cell layout for the prototype GRO (includes an output buffer)

Transistor	Function	$J$	$W$	Total Width ( $\mu\text{m}$ )	Fingers	Finger Width ( $\mu\text{m}$ )
PMOS	Inverter	13	0.25	3.00	3	1.00
PMOS	Inverter	11	0.16	2.00	2	1.00
NMOS	Inverter	9	0.24	1.20	2	0.60
NMOS	Inverter	5	0.24	1.20	2	0.60
NMOS	Inverter	1	0.12	0.60	1	0.60
PMOS	Switch	N/A	N/A	7.90	5	1.58
NMOS	Switch	N/A	N/A	4.50	5	0.9

Table 3.1 Details of the prototype GRO inverter delay cell

Simulations without taking into consideration wiring parasitics indicate that this design efficiently achieves  $\bar{J} = 7.9$ , which, assuming a NMOS/PMOS strength of 2.4



1	2	3	6	7	10	11	14	15	18	19	20
X	47	4	5	8	9	12	13	16	17	22	21
45	46	41	40	37	36	33	32	29	28	23	24
44	43	42	39	38	35	34	31	30	27	26	25

Figure 3-22 Delay cell layout floorplan for the prototype multi-path GRO

is in line with the ideal calculation of

$$\bar{J} = 13 \cdot 0.25 + 11 \cdot 0.16 + 9 \cdot 0.24 + 5 \cdot 0.24 + 1 \cdot 0.12 = 8.4. \quad (3.12)$$

To include the parasitics, we can estimate  $\eta$  equal to 0.5-0.7, which results in a value of  $\bar{J}_{eff} = 4-6$ . Compared with the prior work on multi-path oscillator architectures discussed earlier with  $\bar{J}_{eff} = 2$ , this is roughly a factor of 2-3 improvement. The expected performance is confirmed with measurement results, which are discussed in Chapter 5.

To minimize mismatch both in the delay elements and in the routing parasitic capacitance, a serpentine arrangement of delay elements within was used in the layout, as shown in Figure 3-22. However, the routing was done by hand in a single pass, employing no special techniques to equalize the routing lengths or parasitic capacitances of each delay element output.

### 3.2.3 Non-linearity of the Proposed Multi-Path GRO

With the raw resolution of the TDC much improved with the multi-path architecture, we can now revisit the issue of reducing the magnitude of the quantization error

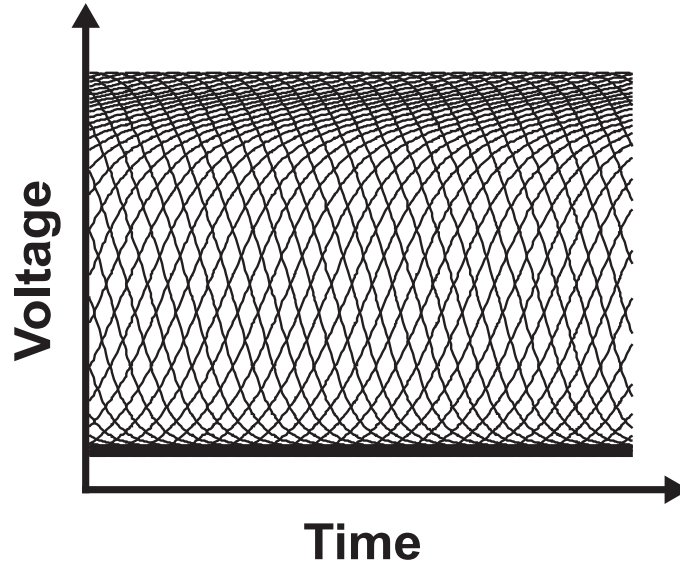


Figure 3-23 Simulated transient voltages of the multi-path delay element outputs

transfer non-linearity. Recall the hypothesis from before that the magnitude of  $T_{skew}$  can be reduced by averaging the skew contributions from multiple elements that are in transition at the same time. To get a sense of how the different transitions relate to each other in the proposed multi-path GRO design, Figure 3-23 plots all of the transient voltages on the same time axis. If we look closely at this figure and carefully count the number of transitions active at any given time, we should not be surprised to find about 13 overlapping transitions, since 13 is the maximum value of  $J$  for this particular multi-path design.

With this picture in mind, we can then revise the cartoon depicting gating skew error for the multi-path architecture as shown in Figure 3-24. At the top of the figure, the alternating pattern of positive and negative transitions vs. GRO phase state are the same waveforms as in Figure 3-23, except that here each delay element output is presented individually. We also see that defining the GRO phase state is much more ambiguous, which is an issue that is later discussed in more detail in Chapter 4.

Because the transitions of the multi-path oscillator delay elements are much wider with respect to  $T_q$  than before, we can also expect that the gating skew contribution from each transition will be much wider as well. In the center of Figure 3-24, we now depict a gating skew error with the same conceptual shape and magnitude as

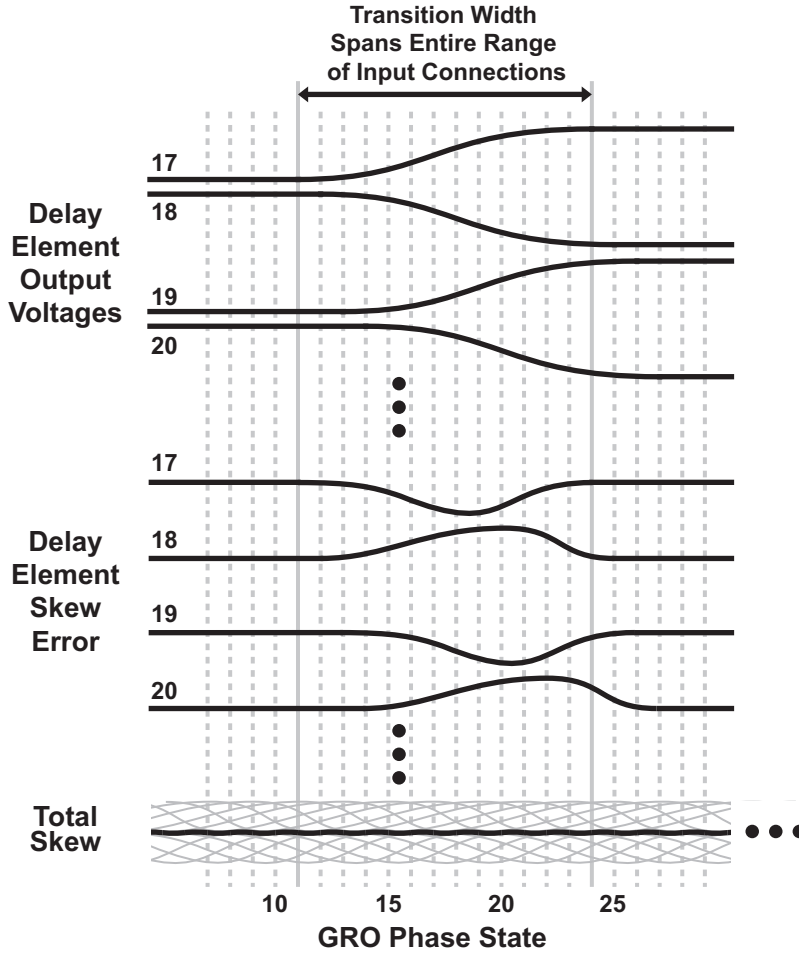


Figure 3-24 Concept of how the overlapping skew from positive and negative transitions for a multi-path GRO significantly reduces the total skew

before in Figure 3-6, although here the width of the contribution has effectively been stretched over a span of  $13T_q$ . Depicting the individual error contribution in this way is a physically intuitive and reasonable thing to do, since we have already seen that charge redistribution is the primary mechanism for skew error, and also that any delay element in transition will observe some amount of charge redistribution. In addition, the equivalent circuit schematic for each individual delay element during the disable window has not significantly changed from the schematic shown earlier in Figure 3-9.

Finally, we show at the bottom of Figure 3-24 that the overall skew error is the “average” of the individual contributions from each delay element, with the result

being much smaller than any of the individual contributions. To consider how this “averaging” relates to the physical oscillator, recall that the delay elements in a multi-path oscillator are strongly coupled together. Thus, when a charge is unnaturally injected into one of the transitioning delay elements, its influence will be mitigated by the inertia of the other delay elements, since all of the elements must work together in converging to a single phase state. This physical analogy provides some justification for depicting the total skew as an “average” of individual contributions that we will later verify through simulation and measurements.

Although Figure 3-24 demonstrates that summing the overlapping transition skew contributions from many stages will result in a smoother skew function with decreased variation, it is not clear *how much* improvement we can expect. In fact, the amount of reduced variation that results from “averaging” multiple functions in this manner strongly depends on the specific characteristics of the individual functions, as well as the time offset that separates them. In addition, we have so far approximated the oscillator state space with only two-dimensions (phase and time), which provides a useful, albeit crude, tool for understanding the relevant issues of gating skew, but does not model the complex intricacies within the GRO. Therefore, we again turn to a simulation testbench similar to that in Figure 3-7 to gain a more quantitative sense of the improved variation of  $T_{skew}$  in the multi-path GRO.

Figure 3-25 displays a single simulated curve for the proposed multi-path GRO  $T_{skew}$  as a function of  $\hat{\theta}_{GRO}$ , assuming typical operating conditions of a 1ns disable width and 50ps rise / fall times, and also with the DC component of  $T_{skew}$  removed for clarity. While the smooth, near sinusoidal shape and period of  $2T_q$  are as expected, the aspect of this figure that is striking is the very small magnitude of the error. Compared to the gating skew error simulated for the inverter-based GRO, the peak-to-peak magnitude shown here is almost an order of magnitude smaller, and this result is with respect to  $T_q$ . Thus when the reduction of  $T_q$  is also considered so that the gating skew error is seen in units of time, the simulated peak-to-peak variation of the proposed multi-path oscillator is smaller than the inverter-based GRO by significantly more than a factor of 10.

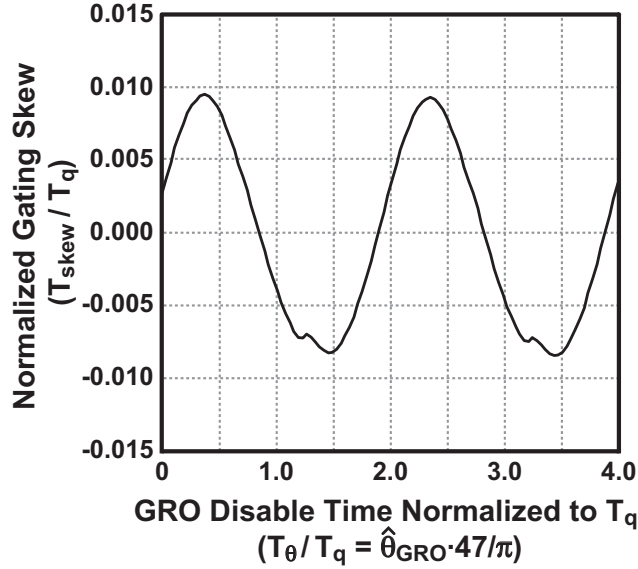


Figure 3-25 Multi-path GRO  $T_{skew}$  as a function of  $\hat{\theta}_{GRO}$  for typical conditions with a disable width of 1ns, and a rise / fall time of 50ps

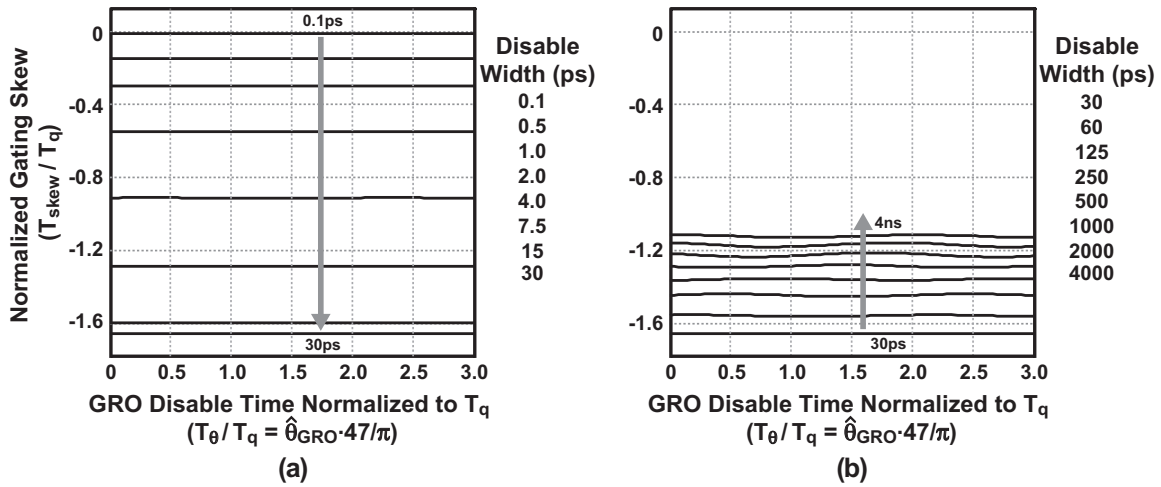


Figure 3-26 Multi-path GRO gating skew  $T_{skew}$  as a function of  $\hat{\theta}_{GRO}$  for stepped values of disable width ( $T_{disable}$ ) from (a) 0.1-30ps and (b) 30-4000ps. The  $Enable$  rise and fall times are held constant at 0.5ps.

To compare the multi-path GRO topology with the inverter-based approach simulated earlier, the same set of simulation conditions are applied to trace  $T_{skew}$  as a function of  $\hat{\theta}_{GRO}$ . As a fair design comparison, both simulations have the total transistor widths within each delay element, with the multi-path transistor gates being assigned to multiple delay elements according to the prototype design instead of

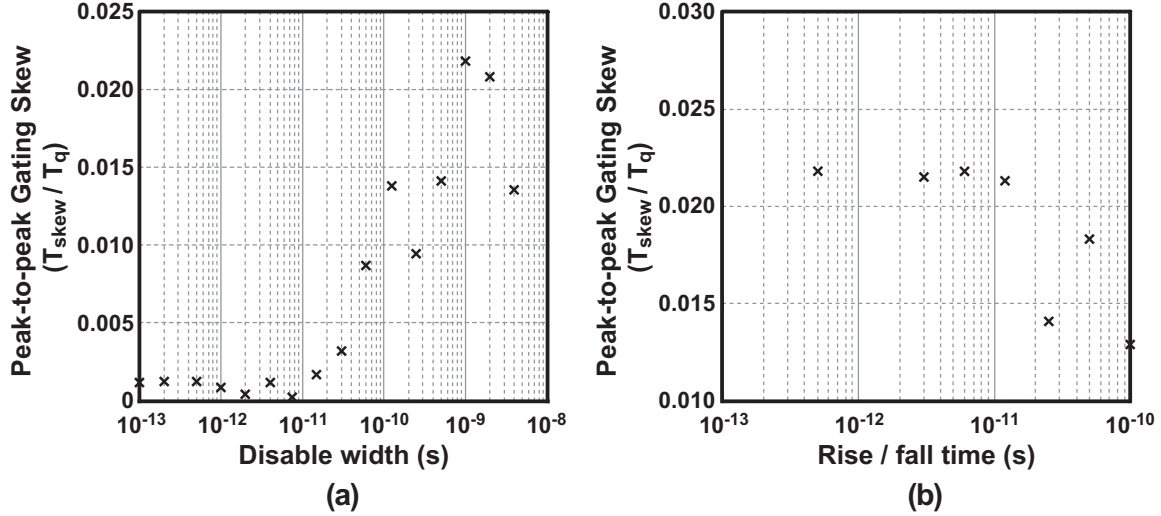


Figure 3-27 Multi-path GRO peak-to-peak  $T_{skew}/T_q$  plotted vs. (a) disable width and (b) rise / fall time

sharing a common connection. However, no attempt was made to scale the parasitic capacitance for the multi-path design, since an accurate value is specific to the implementation and difficult to estimate accurately. To avoid artificially inflating the performance improvement of the multi-path oscillator by neglecting this important consideration, all results from both simulations are normalized to  $T_q$ .

In Figure 3-26, the normalized value of  $T_{skew}$  for the multi-path GRO simulation is plotted for a wide range of disable widths from 0.1-4000ps. To again visualize the two time constants that are present in the multi-path oscillator, the figure is separated according to shorter disable widths of 0.1-30ps on the left in (a), and longer disable widths of 30-4,000ps on the right in (b). As mentioned earlier, the circuit schematics during the disable window for both the inverter and multi-path delay elements are virtually equivalent to each other, with only a modification needed for the value of  $R_{inv}$ , which was defined for the inverter-based GRO in Figure 3-9. Therefore, it is not surprising at all to see the same trends appear in the multi-path oscillator, and we attribute the movement of  $T_{skew}$  to the same charge redistribution mechanisms that were discussed earlier in Section 3.1.3. The peak-to-peak variation in  $T_{skew}$  as a function of disable width is plotted in Figure 3-27(a).

The trend of multi-path GRO gating skew error versus the rise / fall time of

*Enable* also appears very similar to the inverter-based GRO results discussed earlier, with a slight decrease of variation in  $T_{skew}$  for slower *Enable* transitions. This result is seen most clearly in the plot of peak-to-peak variation in  $T_{skew}$  as shown in Figure 3-27(b). To recapitulate an earlier comment, a slower *Enable* may suffer from increased thermal and 1/f noise contributions, although it does seem to provide some benefit in terms of smoothing out the gating skew error.

By providing a physical intuition as well as simulation results, we can conclude that the gating skew error for the proposed multi-path GRO architecture is significantly reduced compared to the inverter-based topology. We can also say that there are two key features of the proposed multi-path oscillator design that enable such a marked improvement in the gating skew error. First, the large number of delay elements in transition at any given time means that the overall gating skew has the potential to be influenced by more than one delay element. Second, the distributed set of connections in this design, chosen originally to ensure oscillation in the primary mode, provide a web that strongly couples the delay elements together. Together, these features enable a very digital circuit structure to accurately preserve the analog state information that is required for noise-shaping. We will later see in Chapters 5 and 6 that this level of gating skew performance is inherently sufficient to achieve robust first-order shaping of the quantization and mismatch error.





# Chapter 4

## GRO readout techniques

### 4.1 Measurement entirely with counters

As shown earlier in Figure 2-11, a simple technique for keeping track of the GRO phase transitions for a given measurement interval is to simply count the number of transitions for each output, and then sum the counter values to result in the TDC output. Figure 4-1 illustrates that for the most basic implementation, two counters are in fact required for each output stage to account for both the positive and the negative transitions. For a moderate number of stages ( $<20$ ) in a standard ring oscillator, in terms of power and area, the overall penalty of having two counters for each stage is modest. We will see later that for the multi-path ring oscillator the penalty in power is more severe.

Other than efficiency, there are more subtle concerns with this simple counting technique when it comes to ensuring that each transition is counted the correct number of times. The counters in a GRO-TDC have two unique considerations in that the “digital” inputs are asynchronous signals with voltages that can often be held at undefined logic levels. Since achieving any noise-shaping at all relies on precisely accounting of GRO phase error, miscalculation of the phase transitions is unacceptable for the GRO-TDC.

To deal with the first issue of asynchronous counter inputs, an obvious solution is to latch the delay element outputs before the counter needs to be sampled. The

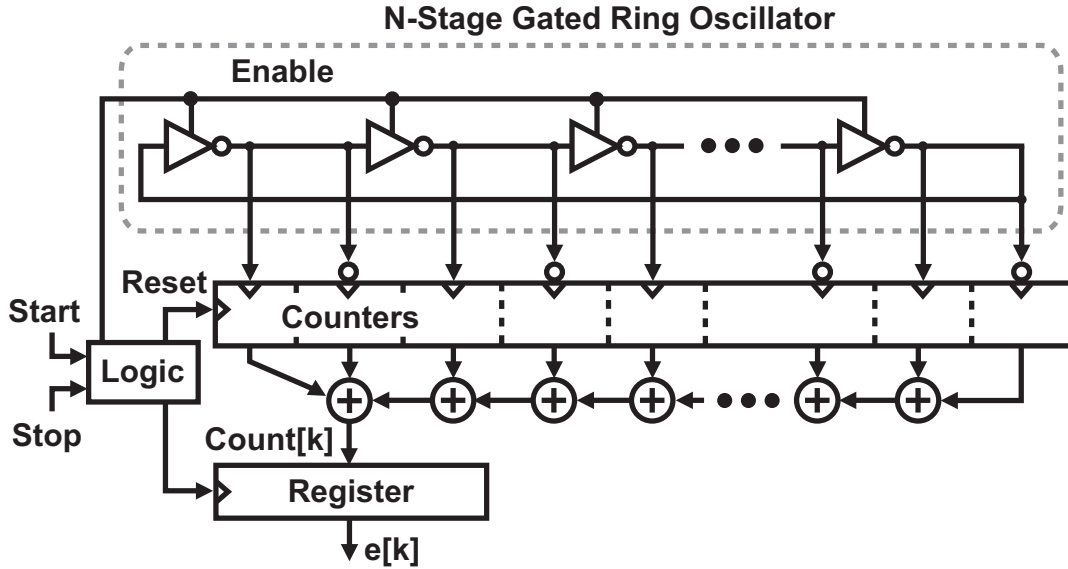


Figure 4-1 Using two counters for each output stage to keep track of the total number of phase transitions

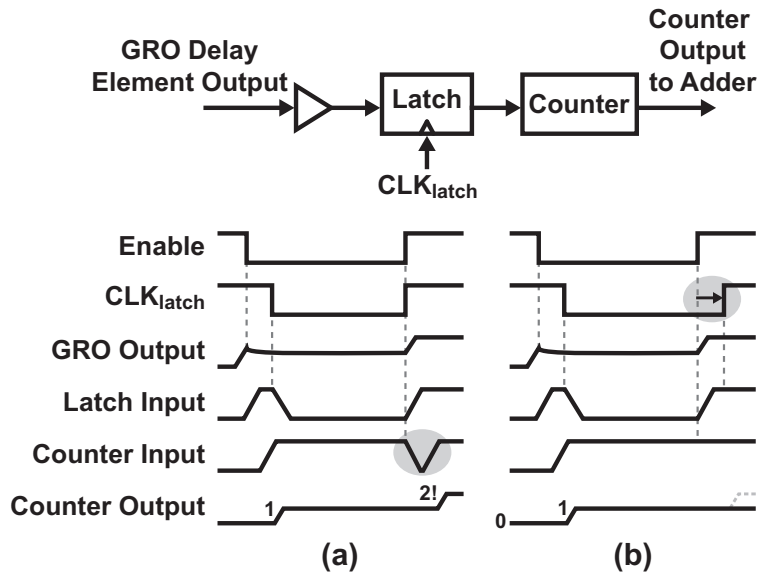


Figure 4-2 Double-counting transitions in the GRO measurement due to ambiguity in delay element output logic levels. (a) Double-counting example, and (b) Suppressing the glitch with a carefully timed latch control signal

counter input simply needs to be latched early enough to guarantee that the ripple counter has properly settled from the time of the last possible input transition.

The second issue of dealing with counter inputs that are stopped at invalid logic levels can be helped somewhat by a few obvious circuits, however addressing the

fundamental issue is more complex. For example, buffering and using positive feedback for delay stage outputs very close to a logical threshold can virtually eliminate metastability problems, but this does not decrease the possibility of the delay stage output moving across the threshold during the disabled window. As shown in Figure 4-2(a) without additional measures in place, the counter can advance more than one count for a single transition event.

One possible solution to address this double-counting of transitions is to de-glitch the negative pulse with a carefully timed latch control signal. Figure 4-2(b) illustrates that after the GRO is enabled, the delay element output in question will quickly resolve itself to a logical state that it will hold for a relatively long time ( $\approx NT_{inv}$ ). By opening the latch slightly after  $Enable \uparrow$  (but well before the next transition), any potential glitches at the counter input will be removed.

When contemplating how phase measurement entirely with only counters can be used for the multi-path oscillator, there are two primary areas of concern. First, while 30 counters operating at a relatively slow rate ( $<1\text{GHz}$ ) does not consume much area or power for the standard inverter GRO [21], the situation worsens considerably for the multi-path oscillator, which would require 94 counters operating at approximately 2GHz. Second, de-glitching the counter inputs by means of careful timing is not a robust technique that can easily be implemented with simple digital synthesis techniques. Although it is understood that the GRO core has custom attributes, we would prefer a more elegant solution that is robust even when implemented by relatively crude automation.

## 4.2 A more efficient measurement technique

In this section we describe an efficient and robust phase measurement technique that is applicable to a wide range of ring oscillators. Compared to the previous approach, which operates on each delay element outputs independently, the foundation for this technique takes advantage of the predictable sequencing of oscillator transitions. In this way, the motivation for both the multi-path oscillator topology and the phase

measurement approach is that the designer can anticipate known phase state patterns to make decisions more intelligently. However, we will first continue to use the standard oscillator in this section to illustrate the concepts of this technique, and later apply the concepts to the multi-path oscillator. We also present a robust de-glitch circuit that does not require precision timing to avoid double-counting.

### 4.2.1 Measuring frequency by tracking phase

For the GRO, counting the delay element outputs is, by far, more expensive in terms of area and power than is sampling the output with a digital register, since in general the TDC sampling rate is much slower than the oscillation frequency. Yet, a single counter provides a full record of its input transitions since its last reset, whereas an undersampled single register appears to provide no transition information at all. In fact, a single register only provides a crude sample of the *phase* of the oscillator. However, we know that the GRO frequency and phase are related by

$$f_{GRO}[k] = \frac{\Delta\theta[k]}{T_s}, \quad (4.1)$$

and we can then say that

$$\frac{1}{2NT_q} = \frac{\hat{\theta}_{GRO}[k] - \hat{\theta}_{GRO}[k-1]}{2\pi T_{in}[k]} \quad (4.2)$$

$$\frac{\pi T_{in}[k]}{NT_q} = \hat{\theta}_{GRO}[k] - \hat{\theta}_{GRO}[k-1] \quad (4.3)$$

$$\frac{\pi}{N} \left( Out[k] + \frac{T_{error}[k]}{T_q} \right) = \hat{\theta}_{GRO}[k] - \hat{\theta}_{GRO}[k-1] \quad (4.4)$$

$$Out[k] = \frac{N}{\pi} \left( \hat{\theta}_{GRO}[k] - \hat{\theta}_{GRO}[k-1] \right) - \frac{T_{error}[k]}{T_q}. \quad (4.5)$$

We see that it is not only possible to estimate frequency indirectly via phase, but the noise-shaping properties of the GRO-TDC are also preserved through  $T_{error}$ . Therefore, calculating phase by using  $N$  registers appears very attractive compared to tracking frequency with  $2N$  counters.

Figure 4-3 illustrates the basic concept of calculating the GRO-TDC output by

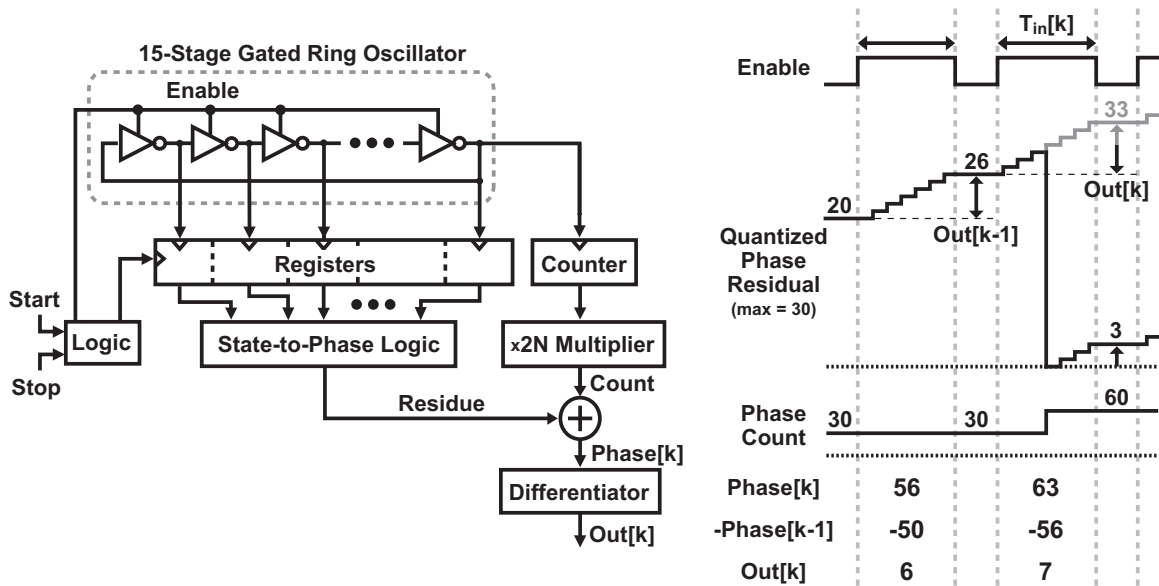


Figure 4-3 Basic concept of calculating the GRO-TDC output by differentiating phase

quantizing the oscillator phase with registers, and then differentiating from sample to sample. Of course, the problem with using *only* registers to measure the average GRO frequency (or number of transitions) is that the oscillator phase value is calculated modulo  $2N$  (or  $2\pi$ , depending on units), and without a means to keep track of the number of phase wraps, the measurement output will be incorrect. To solve this problem, we separate the phase into two components, a fine phase residual that is calculated from the registers, and a coarse phase that accumulates  $2N$  (in the figure  $N = 15$ ) each time the oscillator phase wraps around *without a reset operation*. The coarse phase accumulation can simply be implemented by counting the positive transitions of a chosen delay element.

To accurately calculate the phase residual we need to observe the entire oscillator state, which means utilizing the outputs from all the delay elements. The key idea here is to leverage a simple, predictable mapping between the sampled oscillator output code and phase that is inherent in the fundamental operation of the oscillator. For example, Figure 4-4 charts how the 30 possible phase states of the example 15-stage ring oscillator are encoded in the delay element output values. The starting phase, or equivalently the state mapping to zero residual, is determined by the polarity and location of the counted delay element. To calculate a binary-coded phase residue for

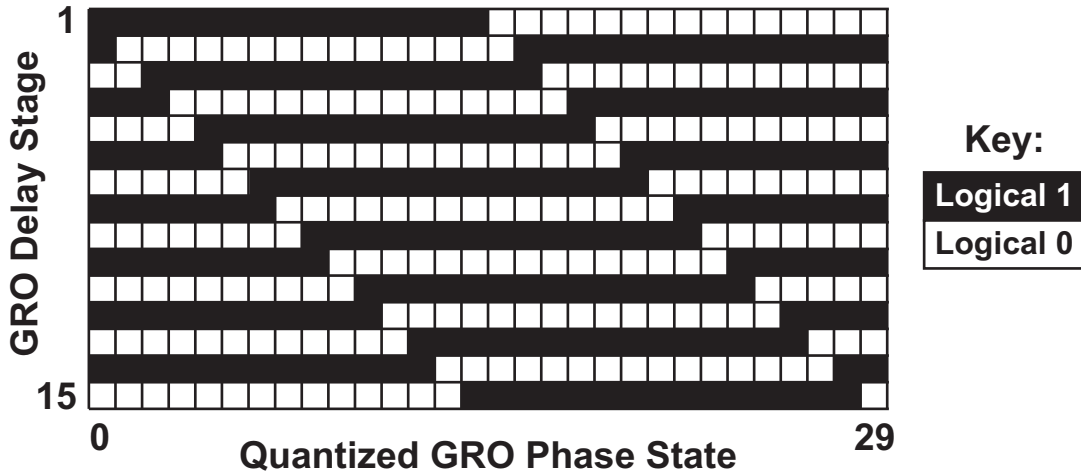


Figure 4-4 Chart showing the logical states of a standard 15-stage ring oscillator for each of the 30 possible discrete phase states

each state, we then use a Karnaugh map for each of the phase residue bits, and to determine the number of transistions for each measurement we implement a simple first-order difference operation.

Although using a counter to deal with the modulo  $2N$  phase wrapping, ironically the fundamental problem is not solved, instead it is inherited by the counter. Therefore, we use the overflow output of a standard  $\beta$ -bit ripple counter to indicate that its range has been exceeded (by design overflow should happen at most once per measurement), and to compensate we simply need to add  $2^\beta$  to the first-order difference output (for that measurement only). Figure 4-5 extends the example of a 15-stage oscillator, where the counter has a range of  $\beta = 4$  bits.

### 4.2.2 Robust de-glitch technique

Earlier in Section 4.1, we discussed how latching the counter inputs during the disable window with careful timing could prevent double-counting transitions that would destroy the quantization error-shaping. While any phase measurement error at all is destructive, if one of the  $2N$  counters in the first approach double counts a single transition, the TDC output will be off by a single LSB. For the phase measurement approach just discussed, the majority of delay elements are seen only by registers

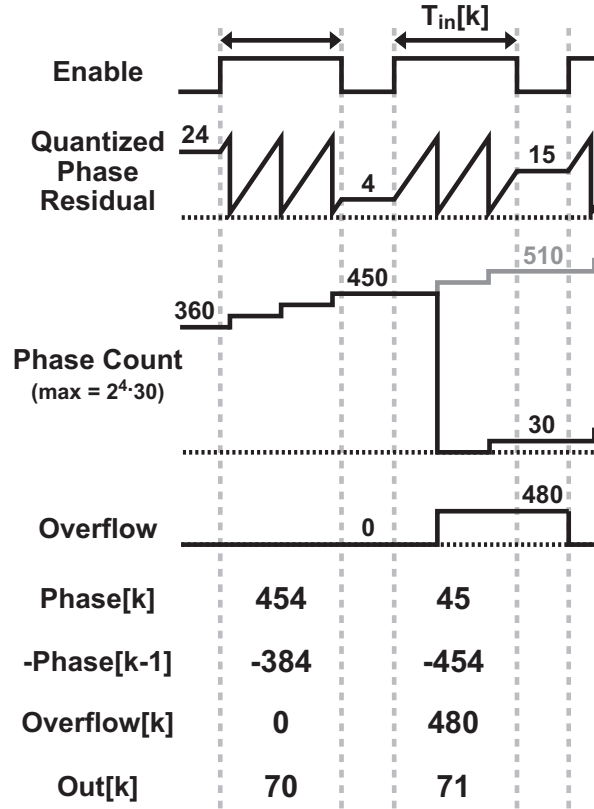


Figure 4-5 Accommodating a counter with a limited range of  $2^\beta$  levels (here  $\beta = 4$ )

which are much less sensitive to glitch events. However, if a double-counting error in the counter is made in this topology, it is likely that the TDC output will be wrong by at least  $2N$ , since the counter output is amplified by this value. This magnitude of error lacks noise-shaping and would likely be very disruptive at the application level.

The first step that we take to remove counting glitches is again to latch the counter input, as seen in Figure 4-6. The delay element output to be counted,  $V_{ocount}$ , is then input to both a latch as well as a register, since its state information is required for both the phase count as well as the phase residue. Putting aside the issue of double-counting for now, we can see another potential source of phase measurement error that the latch output is not guaranteed to be the same as the register output. The two distinct samplers will undoubtedly have different offset and sampling instants, which is problematic since the GRO output  $V_{ocount}$  can be held near mid-supply during the disable times. Although in noise-shaping applications it is likely that a latch/register

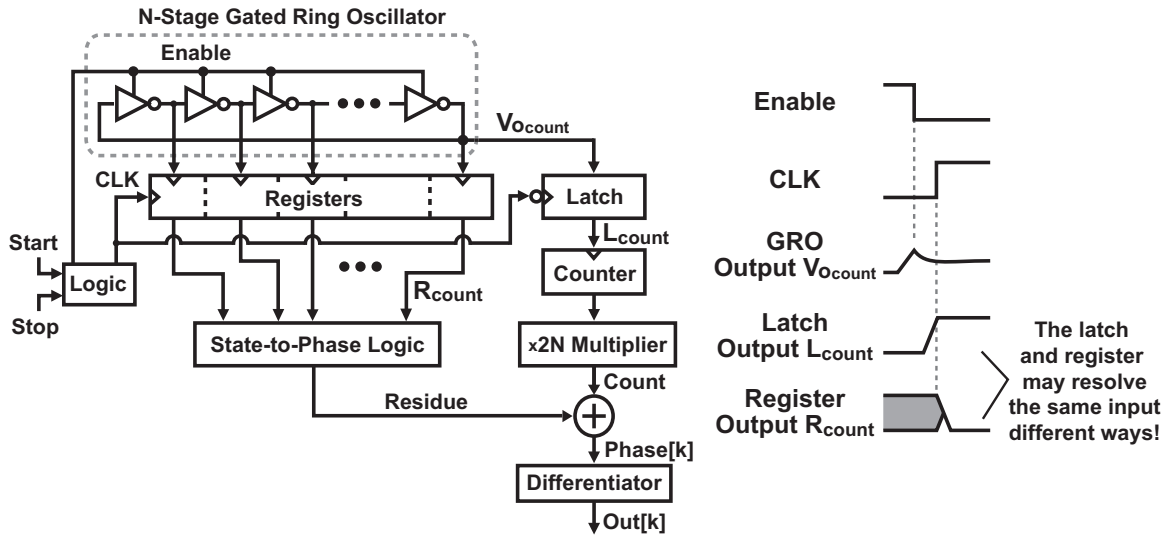


Figure 4-6 A potential phase error when the oscillator state is determined by both registers and counters

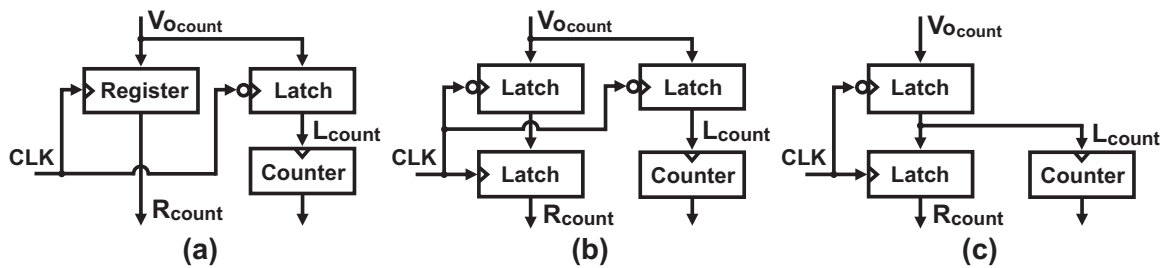


Figure 4-7 Combining register and latch functions into a single element to resolve the potential discrepancy between register and latch outputs. (a) shows the original problematic implementation, (b) illustrates that a D flip-flop is composed of two serial D latches, and (c) combines the redundant latches to ensure the same signal is observed by both the register and the counter.

discrepancy would be corrected in the next sample, the TDC outputs for at least two samples would be incorrect, which is generally unacceptable.

A very efficient way to resolve the potential discrepancy between the latch and register outputs is to utilize a common latch circuit for both functions. Figure 4-7 illustrates that we can implement a D flip-flop register as a master-slave pair of D latches, and coincidentally in (b) we find that the first D function is implemented by both the register as well as the latch. As seen in (c), we can eliminate a redundant latch, and at the same time achieve a unified signal path that will ensure the phase count and phase residual are consistent with each other (note that in this statement



we rely on a monotonically increasing phase during the enabled window).

With assurance of a consistent phase count and phase residue, we now focus on the issue of double-counting errors due to glitches at the counter inputs (as discussed earlier in regard to Figure 4-2). Instead of clocking the latch signals with precisely controlled timing, we can avoid glitches with a more robust technique that once again leverages the predictable sequence of the oscillator phase state.

Recall that the goal for the de-glitch circuit is to ensure that the counter increments exactly once for each GRO phase rotation, regardless of how slowly the counter voltage threshold is crossed, or even how many times the threshold is crossed! Therefore, the key idea for the proposed de-glitch circuit is the knowledge that when the counter input  $V_{o_{count}}$  is held near mid-supply, almost all the other stages are resolved to unambiguous logic levels.

Specifically, if  $V_{o_{count}}$  is transitioning high at the time  $Enable \downarrow$ , then we can say with certainty that a delay element output  $V_{o_{de-glitch}}$  preceding  $V_{o_{count}}$  by a small, even number of stages (e.g.  $V_{o_{de-glitch}} = Z_{count-2}$ ) has just completed its positive transition. Similarly, the negative transitions follow in the same sequence. Therefore, we can say that to prevent the counter input from “moving backward”, it should only transition when both  $V_{o_{de-glitch}}$  and  $V_{o_{count}}$  share the same logic level. A truth table for the de-glitch logic can be seen in Table 4.1, where  $L_{de-glitch}$  and  $L_{count}$  are defined as the latch outputs corresponding to  $V_{o_{de-glitch}}$  and  $V_{o_{count}}$ , respectively, and  $L_{cd}$  is the de-glitch logic output.

$L_{de-glitch}$	$L_{count}$	$L_{cd}$
1	1	1
1	0	No change
0	1	No change
0	0	0

Table 4.1 Truth table for the de-glitch logic

Figure 4-8 shows one circuit realization of the de-glitch logic using a four-transistor stack along with weak regeneration. When both  $V_{o_{de-glitch}}$  and  $V_{o_{count}}$  share the same logic level, the appropriate pull-up or the pull-down network is active. Alternately, if

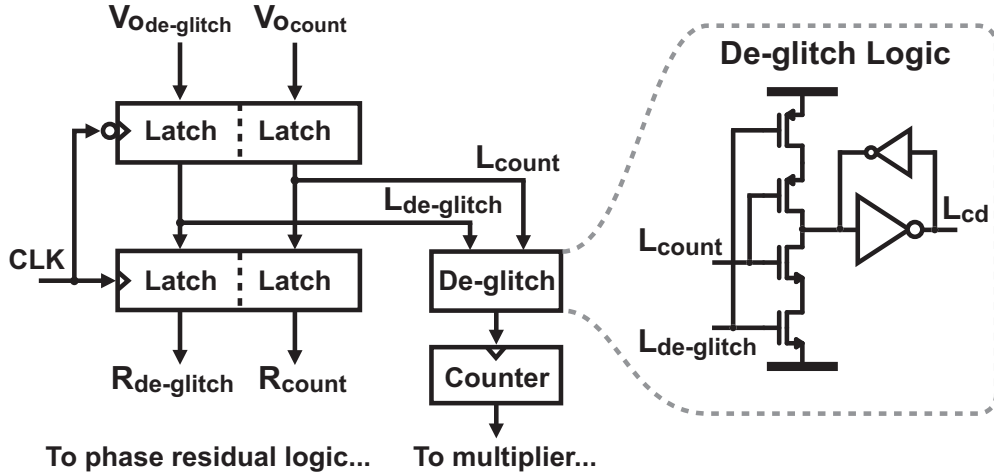


Figure 4-8 Implementation of a de-glint circuit that achieves hysteresis by relying on the sequence of oscillator states

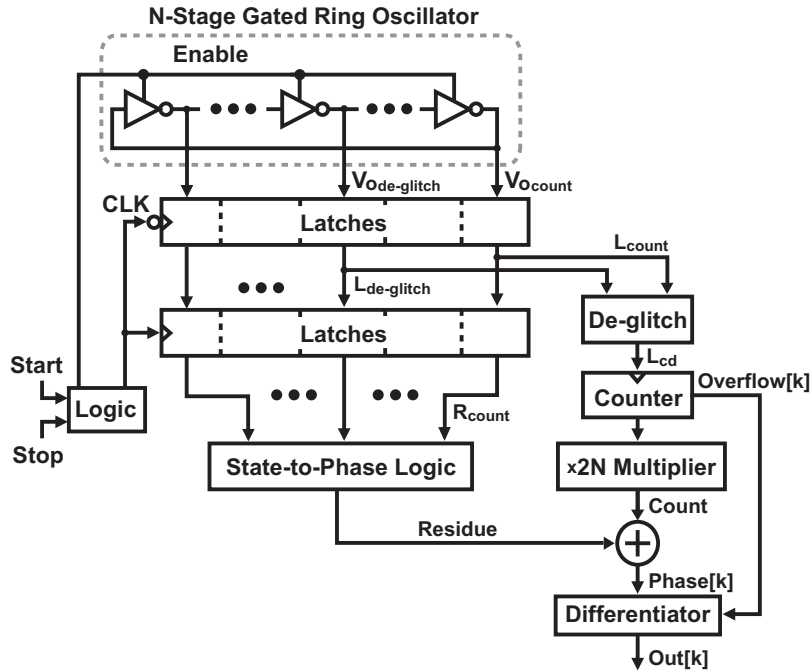


Figure 4-9 Overall block diagram of efficient and robust phase measurement technique for an inverter-based GRO

the inputs do not have the same value, the networks have no influence and  $L_{cd}$  is held constant with the positive feedback. Since the overlap time of  $V_{ode-glitch}$  and  $V_{ocount}$  is shorter than half the oscillator period, the timing requirements for this circuit can influence not only transistor sizing for the de-glint logic, but the choice for the overall number of oscillator stages  $N$  as well.

The overall block diagram of the technique applied to a standard inverter-based GRO is pictured in Figure 4-9. The diagram includes both the efficient measurement approach with phase differentiation as well as the robust de-glitch circuits just discussed. With the example of the simple GRO implementation completed, we can now consider these techniques for use in the more complex multi-path oscillator.

## 4.3 Multi-path GRO-TDC implementation details

Although the measurement approach has been presented for the simple GRO, there are significant differences in the multi-path GRO that make directly adopting the approach challenging. In this section we first describe issues involved in precisely measuring phase of the GRO that is an essential component of the efficient measurement technique described earlier. We then present a way to address these issues by partitioning the oscillator into smaller components, with each component having the properties required for accurate phase measurement. Subsequently we provide a system level description for a prototype GRO-TDC, and last we describe the details for implementation including digital circuit elements and clock generation.

### 4.3.1 Phase measurement of a 47-stage multi-path oscillator

As mentioned before, the key idea of the phase measurement technique is to leverage the predictable relationship between the GRO state and phase in order to significantly reduce the complexity of the measurement circuitry. In the case of the serial inverter ring oscillator, the predictable relationship is established because each inverter must wait to transition until the preceding stage is close to completing its own transition. Therefore, both the transitions and phase of an inverter-based ring oscillator *must* proceed in a monotonic sequence according to each delay element’s location on the ring.

In contrast to the inverter-based topology, each delay element in the multi-path oscillator may begin transitioning well before the preceding stage is close to completing its own transition. In fact, this “anticipation” is the very thing that allows for

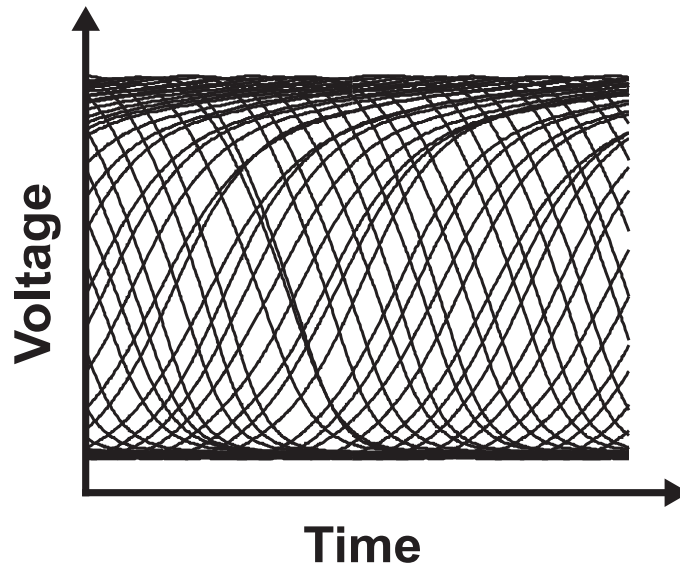


Figure 4-10 Simulated transient voltages of the multi-path delay element outputs when mismatch is included

significant reduction of the effective delay per stage. As a result, we have already seen in Figure 3-23 how approximately 13 delay elements in the proposed multi-path oscillator are in transition at any instant.

When considering a practical implementation, Figure 4-10 shows an example of delay element output transient voltages when the simulation includes the effect of mismatch. For this plot, mismatch was assumed for the transistors as well as for a small parasitic capacitance with 20% standard deviation. In this figure, note that a few of the transitions moving in the same direction appear to be very close together, and at other times the transitions are more spread apart. The differential non-linearity is not a problem in and of itself for the GRO-TDC, since this error is first-order shaped. However, the close proximity of edges does pose a problem for the efficient phase measurement techniques that we would like to use.

Recall that the quantized GRO state is encoded with the logical value of the delay element outputs, and that mapping from the GRO state to phase requires knowing the exact transition sequence that delay elements will undergo during oscillation. In this case, the sequence of transitions may be deterministic within a specific realization, but this sequence is almost impossible to predict, and in addition there is the possibility

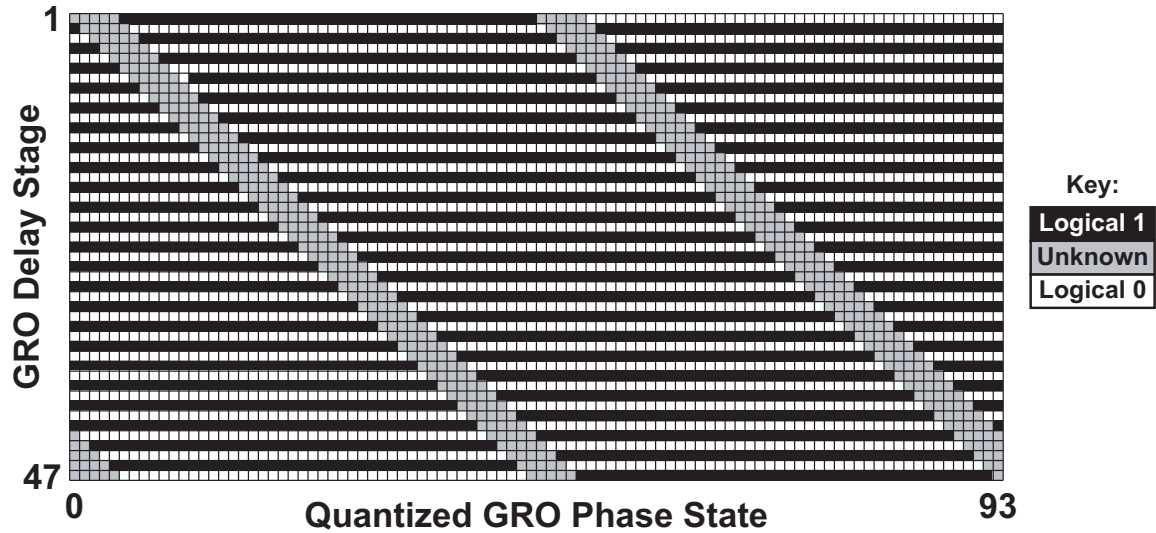


Figure 4-11 Logical states of the 47-stage multi-path oscillator for each of the 94 possible quantized phase states

that two transitions could cross their respective logical thresholds in a random order. With so much ambiguity clearly evident in the GRO state, establishing a predictable relationship between the transition sequences becomes a primary challenge.

We illustrate the ambiguity in the mapping between the quantized state and phase for a 47-stage multi-path GRO in Figure 4-11. This mapping is a critical part of the phase measurement approach, but without being able to predict the transition sequences in the design flow, it is impossible to hard-wire logical circuits that precisely calculate the overall GRO phase.

One potential way to solve this issue is to create an algorithm that populates a dynamic look-up table based on observing the TDC output, but this approach is cumbersome and inefficient. Alternately, we could simply revert back to counting each of the delay element outputs independently, but we have already discussed the associated drawbacks in this case. Fortunately, there is a compromise between having a single counter and having  $2N$  counters.

Figure 4-12 illustrates the concept of partitioning the entire GRO state into 7 smaller measurement cells. Here we choose enough cells and distribute the cell inputs so that instead of having multiple ambiguous inputs in the state-to-phase logic, there is at most one delay element in transition per cell at any given time. The tradeoff in

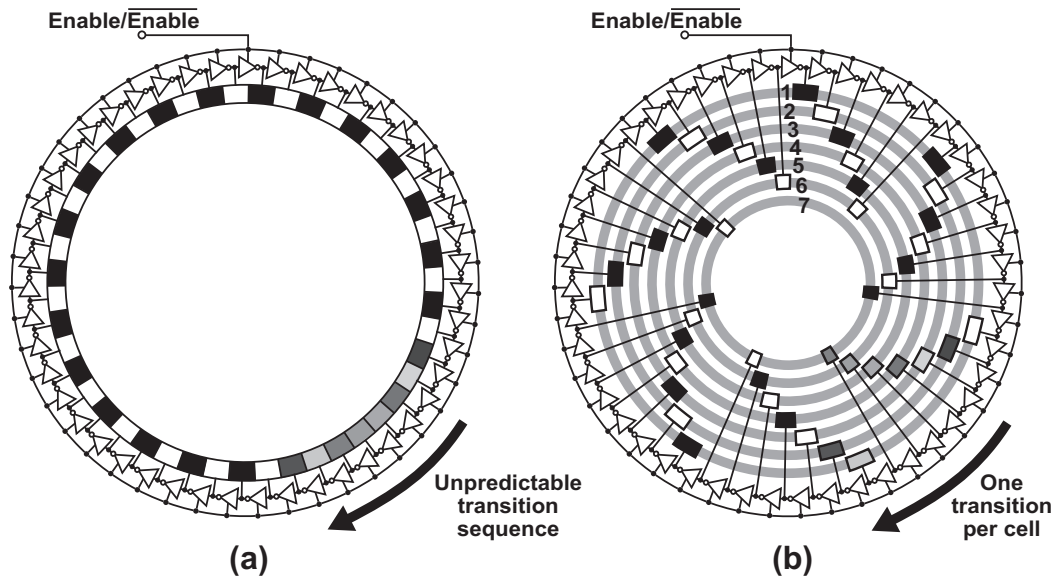


Figure 4-12 A geometric view of an example multi-path GRO state illustrating (a) the unpredictable transition sequence considering the entire multi-path oscillator, and (b) a partitioned approach that re-establishes predictable transition sequences within each of the 7 independent measurement cells

this approach is the increased power of having one counter for each cell instead of one counter for the entire GRO. This small penalty is far outweighed by re-establishing the predictable sequence of states, at least with respect to each individual cell. The measurement cells can then independently calculate their outputs, which are then simply summed together in the final step to result in the overall TDC output.

The interesting aspect to this approach is that although we have separated the entire GRO state into independent groups for purposes of measurement, we have not altered any of the GRO properties. In fact, as shown in Figure 4-13(a), by simply rearranging the outputs in a convenient manner, the ambiguity in the overall *GRO* phase state has not actually been resolved. Instead, as shown in (b), the phase state for each *cell* is now predictable and internally self-consistent. From this perspective, these 7 cells may be seen as coupled oscillators, although in this case we do not require all of the cells to be equivalent, nor do we require a conventional pattern for the state sequence.

For convenience it is simpler to have one measurement cell repeated multiple times, however the prime number of GRO stages is more important for stability reasons. In

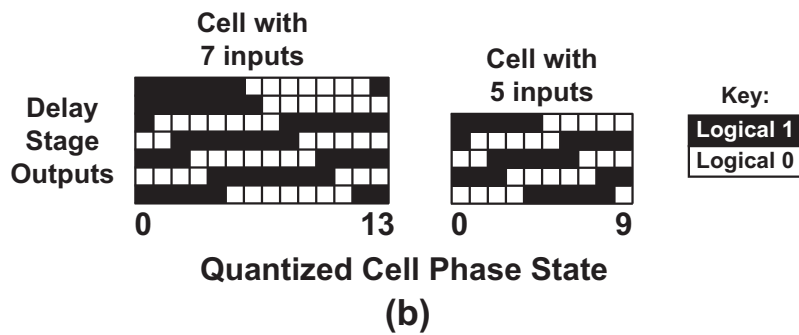
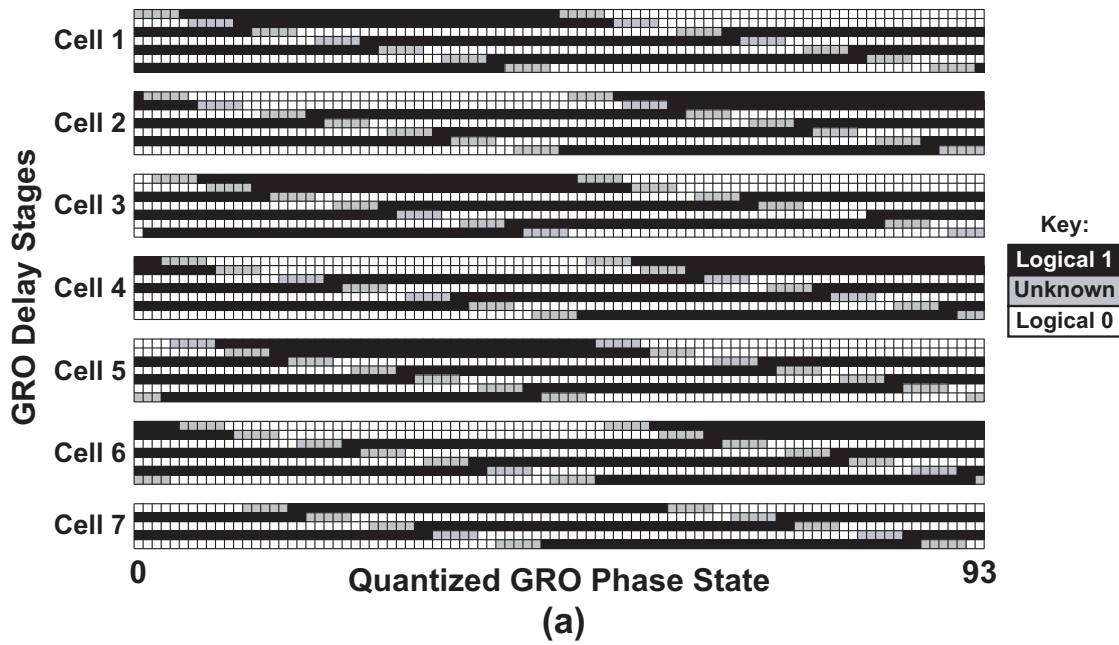


Figure 4-13 Re-arranging the logical states of the multi-path GRO into groups that correspond to the 7 measurement cells. (a) charts the ambiguity in the overall GRO phase state, and (b) charts the predictable phase state for the smaller cells

general, it *is* possible to have only two kinds of cells, and here we choose to have 6 cells with 7 inputs each, and 1 cell with 5 inputs. The assignment of delay elements to cells is shown in Table 4.2, and we note that the first pair of inputs for each cell are separated by 6 stages to use in the de-glitch logic.

Finally, we now show a system block diagram for the proposed 47-stage multi-path GRO-TDC in Figure 4-14. Although we have discussed at some length the GRO core and the measurement cells, a few other digital circuit blocks are also needed within the TDC. The timing generation block takes a start and stop signal input, generates the differential *Enable* signal, and sufficiently buffers *Enable* in order to drive the

1.1	1	2.1	2	3.1	3	4.1	4	5.1	5	6.1	6	7.1	13
1.2	7	2.2	8	3.2	9	4.2	10	5.2	11	6.2	12	7.2	20
1.3	14	2.3	15	3.3	16	4.3	17	5.3	18	6.3	19	7.3	27
1.4	21	2.4	22	3.4	23	4.4	24	5.4	25	6.4	26	7.4	34
1.5	28	2.5	29	3.5	30	4.5	31	5.5	32	6.5	33	7.5	41
1.6	35	2.6	36	3.6	37	4.6	38	5.6	39	6.6	40		
1.7	42	2.7	43	3.7	44	4.7	45	5.7	46	6.7	47		

Table 4.2 Assignment of delay element outputs to measurement cell inputs

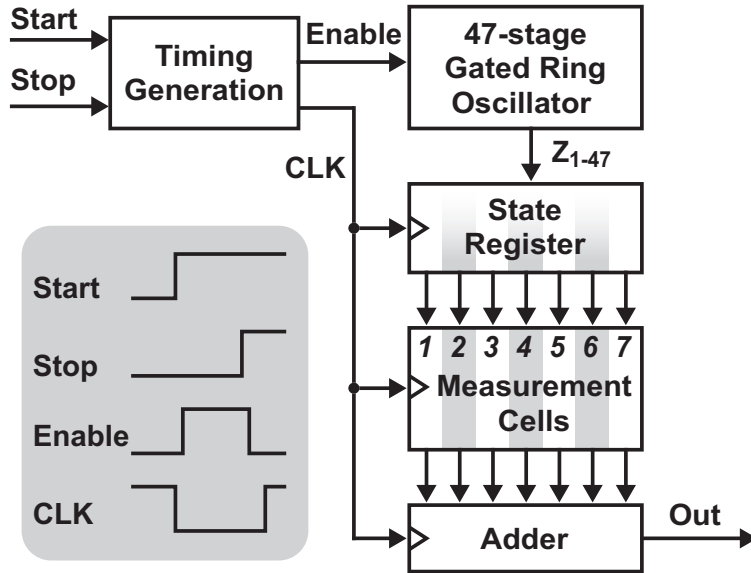


Figure 4-14 Overall system block diagram for the proposed 47-stage multi-path GRO-TDC

GRO core with modest rise and fall times (and correspondingly modest jitter). In addition, the timing generation block derives the other clocking signals as required by the measurement cells. Last, the output adder receives all of the calculated outputs from each of the measurement cells and sums them to result in the overall GRO-TDC output.

### 4.3.2 Other design considerations

Although the GRO-TDC can easily accommodate very large range input signals by adding bits to the counters, the penalty for doing so is an increase in the minimum length of the disable time, since these counters must fully settle and be sampled before the oscillator can be enabled again. In addition, the processing time for a



large number of bits can increase the pipeline delay of the measurement cells and output adder significantly if very high-speed operation also must be supported. Low pipeline delay is important in many closed-loop applications because it can pose an upper limit on the loop bandwidth. Therefore, design of the overall TDC must trade the parameters of maximum sampling rate, maximum range, and acceptable pipelined delay against each other to find an appropriate balance.

For our prototype demonstrations, we chose to implement two versions of the GRO-TDC, with specifications determined by the system applications. The multi-path GRO core is common and, assuming a minimum resolution design takes first priority, can be used for a very wide range of applications. The first TDC is a general purpose 11-bit, 100Msps version that can typically be used for systems comparing to crystal references such as PLL and multiplying DLL [21, 25]. The second version is an 8-bit, 500Msps TDC that can be used in high-speed timing applications such as CDR. These various applications will briefly be discussed later in Chapter 6.



# Chapter 5

## GRO-TDC results and discussion

At this point, the concept of a gated ring oscillator TDC has been introduced, and a number of design considerations have been discussed that relate to overall performance, for example raw resolution, gating skew error, measurement precision, efficiency, and range vs. sampling rate. To demonstrate how these considerations relate to a practical implementation, a total of three GRO-TDC were designed and fabricated in  $0.13\mu\text{m}$  CMOS technology.

The first GRO-TDC is based on a simple 15-stage inverter-based oscillator core, and has a 10-bit measurement range using only counters. The second and third GRO-TDC are based on the same multi-path GRO that is described in 3.2.2, and both use the efficient readout techniques described in Section 4.3. The difference between these two GRO-TDC, then, is the range and maximum operating frequency, with a 8-bit, 500Msps part and an 11-bit, 100Msps version. A single microphotograph depicting an 11-bit GRO-TDC  $1.0\text{mm}\times 1.0\text{mm}$  die is shown in Figure 5-1, which is nearly identical to the other die in terms of visible markings.

In this chapter, we first describe the requirements and proposed approach for the measurement setup. Next, we present measurement results for the inverter-based GRO-TDC, including the non-linear effects of the gating skew error for this implementation such as corrupted noise shaping and deadzones. Then, measurements of the 11-bit multi-path GRO-TDC are shown, which verifies the inherent noise-shaping capability of the GRO-TDC architecture. Finally, we conclude this section with a

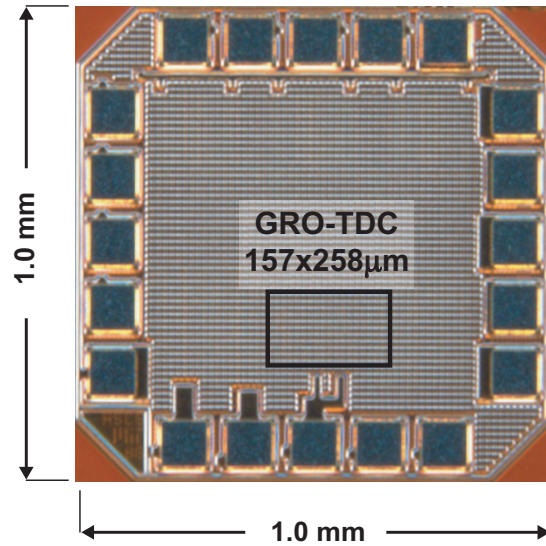


Figure 5-1 Microphotograph of a multi-path GRO-TDC chip

discussion of the results.

## 5.1 Measurement setup

The GRO-TDC can measure a time difference between edges created by two distinct time sources, however the overall jitter in such a measurement is significantly larger than the internal TDC noise. Instead, a preferred way to take data is to measure the delay of a single time source, as shown in Figure 5-2, which removes the noise contributions from the source entirely. Although there is some noise contribution from the delay element itself, this is expected to be comparable to the internal TDC noise itself.

There are two primary issues with using the modulated delay method to create an input signal to the TDC. The first problem is that it is very difficult to create a large signal that spans the entire TDC range, and the second problem is that the linearity performance for large signals is generally quite poor. Although pulse-width modulation can be used to achieve very high linearity for audio frequencies, achieving such linearity with low noise at 50Mpsps with discrete parts is actually quite challenging. Therefore, we have chosen to implement the variable delay by

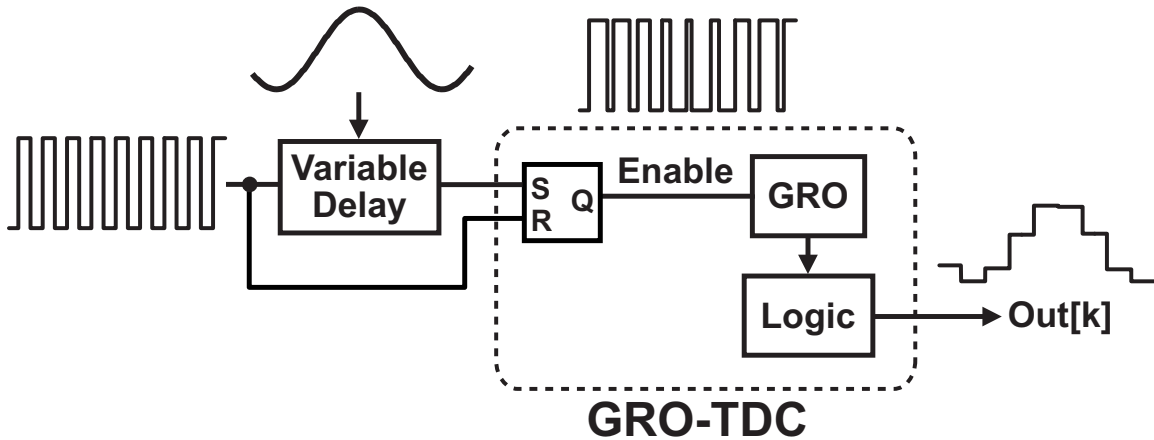


Figure 5-2 A method to create a low-noise input signal for the GRO-TDC testing

modulating the power supply of an off-chip buffer, which is suitable for measuring the GRO-TDC noise performance with relatively small input signals. This signal generation capability is designed onto a gold-plated FR-4 circuit board, which also provides power supplies, decoupling capacitors, and a substrate for direct-bonding of the GRO-TDC chips.

Due to the limitations just discussed for generating large input signals, we choose to use two synchronized signal generators to verify large-signal performance across the full range of the GRO-TDC. In this setup, the frequency and phase of the first signal is held constant, and the second signal generator can be phase modulated to create a time difference that fully spans the GRO-TDC range. Again, the quality of the input in terms of both noise and linearity using this approach is quite poor, however the measurement does establish a full-scale signal level for the TDC.

## 5.2 Inverter-based GRO-TDC measurements

Current consumption of the inverter-based GRO-TDC from a 1.2V supply is a linear function of the duty cycle of the input, and ranges from 1.7mA with 2% activity to 4.4mA at 80% (2.0 to 5.3mW). Of the 1.0mm×1.0mm chip with 20 pads, this GRO-TDC requires only 172μm×120μm of active area, not including decoupling capacitors, and the GRO core is 66μm×19μm. The input range of the 10-bit TDC is 0.2-45ns,

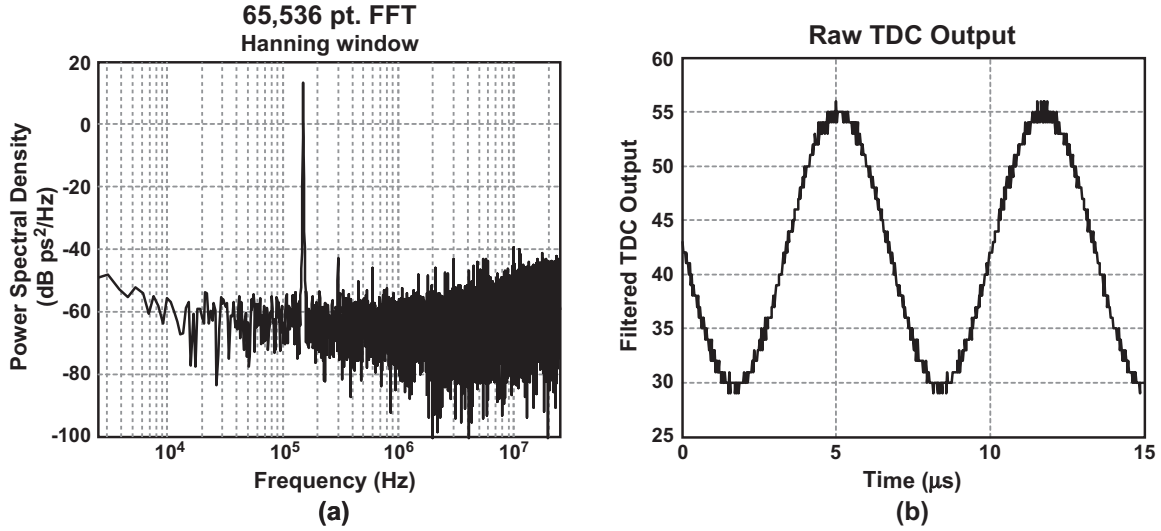


Figure 5-3 Measured 65,536-pt. FFT of an inverter-based GRO-TDC output

and the minimum sampling period is 4nsec as required for timing control. For all reported measurements, the nominal sampling rate is 50MHz.

To properly scramble the GRO phase and achieve reasonable noise-shaping, a relatively large, asynchronous input to the TDC is required. An example of this case is shown in Figure 5-3(a) with an input that is phase-modulated at a rate of 150kHz and at a amplitude of 0.25rad. The 65,536-point FFT spectrum with Hanning windowing does in fact show some level of noise-shaping at high frequencies near 25MHz, or  $F_s/2$ , and the time-domain view appears perfectly normal in Figure 5-3(b). However, we can notice the very high noise floor that is caused by scrambling the large gating skew error. With the noise levels in the figure normalized to show an equivalent two-sided power spectral density, the high noise floor corresponds with the ideal variance from a classical quantizer with 25-30ps resolution sampling at the same rate of 50MHz. This level of noise is much larger than  $1/f$  or thermal noise limitations, and implies that the noise-shaping benefit is small for the inverter-based GRO-TDC.

While the measurement shown in Figure 5-3 does not achieve a low noise floor, it does represent a fairly linear behavior compared to other measurement scenarios. There are many other inputs that can be applied to the inverter-based GRO-TDC that do not result in adequate scrambling of the GRO phase, and the resulting non-

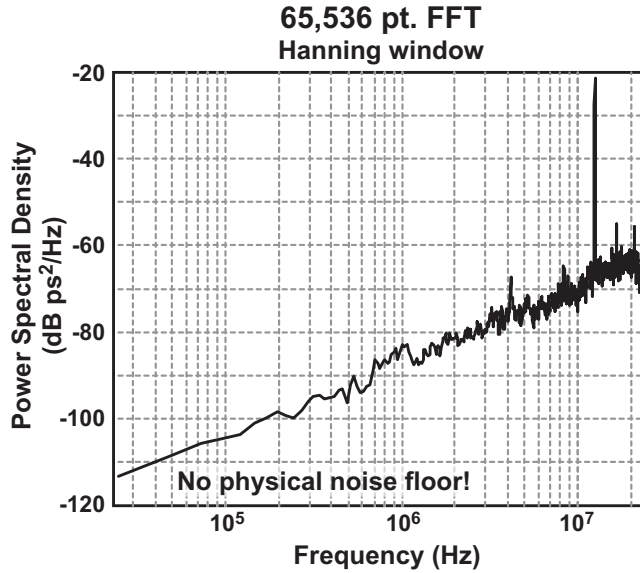


Figure 5-4 An example of non-linear behavior in the inverter-based GRO-TDC

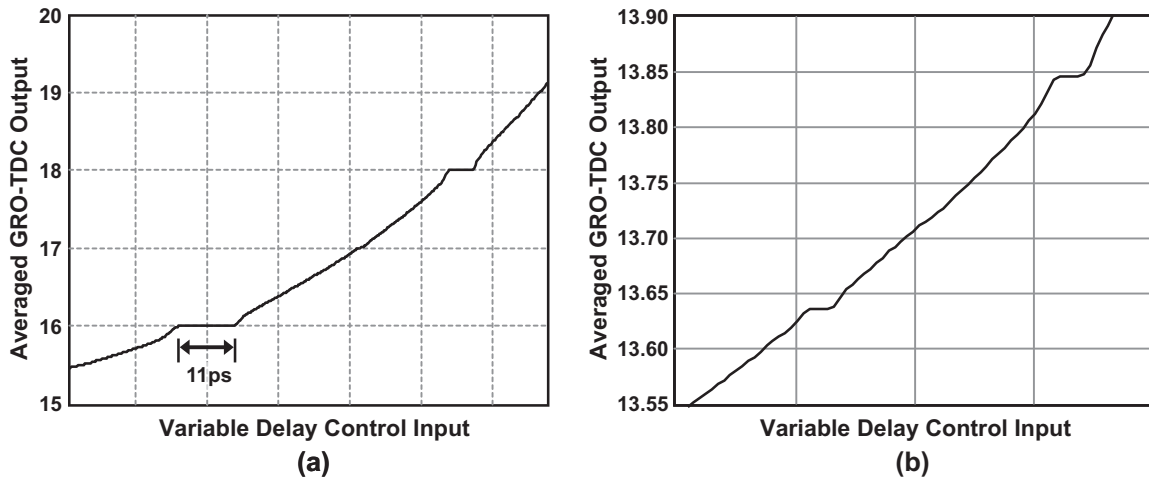


Figure 5-5 A measured DC transfer characteristic for the inverter-based GRO-TDC that demonstrates the presence of deadzones. (a) indicates the deadzone behavior for integer TDC outputs, and (b) shows the potential for small deadzones at non-integer output values.

linearity can be clearly seen in the TDC output. For example, in Figure 5-4, an input that is synchronously modulated at 12.5MHz is applied to the GRO-TDC, and the FFT spectrum clearly first-order noise-shaping. However, the figure also reveals non-linear behavior since there is no observable noise floor in the TDC output.

The issue of deadzones in the DC transfer characteristic as a result of gating skew non-linearity was theoretically discussed earlier in Section 3.1.4, and this behavior

can also be seen experimentally in the inverter-based GRO-TDC. To generate a DC signal for the GRO-TDC, the variable testing delay is controlled with a digital-to-analog converter, and in this particular measurement setup the overall tuning system is quite non-linear. Nevertheless, a DC transfer characteristic of the inverter-based GRO-TDC is plotted in Figure 5-5. The deadzone behavior at the integer boundaries is clearly evident in (a), with larger deadzone widths for the even TDC outputs as predicted from simulations. Closer examination of the curve in (b) reveals that much smaller deadzones are possible for some non-integer TDC outputs as well.

### 5.3 Multi-path GRO-TDC measurements

Within the 1.0mm×1.0mm chip, the active silicon area of the larger 11-bit GRO-TDC is 258μm×157μm, and the area of the 8-bit chip is 217μm×143μm, which both include a guardring but exclude power supply decoupling capacitors. The area for the shared 47-stage multi-path GRO core is 88μm×54μm. All measurements reported here are using the 11-bit part at 50Msps, since at this sampling rate and with output values less than 8-bits, the parts are verified to have identical functionality.

#### 5.3.1 Delay, power, and efficiency performance

A 1.5V supply is used in general for measurements, and functional operation was verified from 1.0-1.6V. As shown in Figure 5-6, the raw delay per stage of the GRO is a strong function of the power supply, and has a nominal value of 6ps at 1.5V. Also as expected, the power consumption of the GRO-TDC is measured to be a linear function of the width of the input signal. At 50Msps, the minimum power is 2.2mW for a very small input, and the maximum is 21mW for full-scale.

The measured multi-path delay of 6ps represents an improvement factor of over 5 compared to an inverter-based GRO-TDC delay of 30-35ps under the same voltage supply and operating conditions. This result verifies the significant benefit in raw resolution that multi-path oscillators can offer for TDC applications. Recall that in Section 3.2.1, we defined  $\bar{J}_{eff}$  to be the product of a weighted sum of multi-path



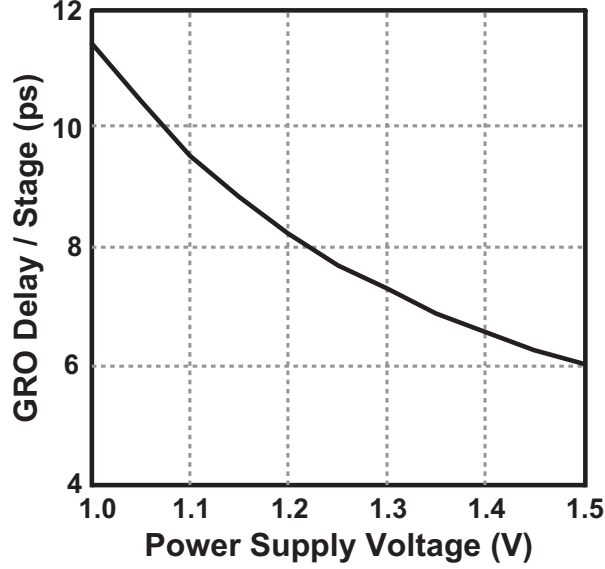


Figure 5-6 Measured delay per stage for the multi-path GRO vs. power supply voltage

connections with an efficiency factor,  $\eta$ . Now with the measured results in place, we can calculate  $\bar{J}_{eff}$  of the multi-path design to be 5, and using the values of  $J$  and  $W$  given in Table 3.1, we find that

$$\bar{J}_{eff} = \eta \sum_{k=1}^K w_k \cdot j_k, \quad (5.1)$$

$$5 = \eta (13 \cdot 0.25 + 11 \cdot 0.16 + 9 \cdot 0.24 + 5 \cdot 0.24 + 1 \cdot 0.12), \quad (5.2)$$

$$\eta = 0.60. \quad (5.3)$$

Therefore, while this particular design has lost a small amount of efficiency due to implementation parasitics compared to the improvement that might be expected from unextracted simulations, the speed benefit compared to the inverter-based implementation is still very significant.

A typical method to measure efficiency for converters is by the standard figure of merit,  $P/F_s/2^{ENOB}$ . Although it is difficult to calculate the effective number of bits for the TDC in a manner comparable to a classical ADC, as an alternative we can use an efficiency figure of merit defined by

$$\text{FOM} = \frac{\text{Power}}{(\text{Sampling Rate})(\text{Conversion levels})} \quad (5.4)$$

$$= \frac{21 \times 10^{-3}}{(50 \times 10^6)(2^{11})} \quad (5.5)$$

$$= 0.2\text{pJ/step.} \quad (5.6)$$

The GRO-TDC compares favorably with other TDC in this metric, yet there is a fundamental flaw in this FOM because it does not appropriately factor the TDC resolution. For example, a very large range can easily be achieved by using a cyclic TDC, but this does not imply anything about the minimum detectable signal. Therefore, we now move on to demonstrate the strength of the GRO-TDC, which of course is the ability to achieve first-order noise-shaping.

### 5.3.2 Noise shaping performance

While the improved raw resolution is an important benefit of the multi-path oscillator, recall that a fundamental design goal is to linearize the noise-shaping performance by significantly reducing the gating skew. To examine whether this is accomplished with the prototype GRO-TDC, we can apply *very* small input signals using the modulation techniques described in the previous section. After collecting data in this way we can examine the TDC output in both the time and frequency domain, and also in the DC transfer characteristic to look for the presence of any non-linear deadzone behavior.

Figure 5-7 shows the both the frequency and time domain GRO-TDC 50-Msps output with a 26kHz input of 1.2ps<sub>pp</sub> in addition to a DC level of about 1.6ns. In (a), the 65,536 point FFT is performed with a Hanning window on 20 sequential collects before being averaged to result in the double-sided power spectral density as shown. Noise-shaping of more than 20dB is clearly evident, with 1/f noise appearing to dominate at low frequencies. The wide, shaded horizontal line in Figure 5-7 shows that the low frequency power spectral density of the GRO-TDC output is comparable to what ideally would be produced by a 50Msps classical quantizer (i.e. no noise shaping) with 1ps steps.

By looking at the time domain output after digitally filtering with a 1MHz bandwidth in Figure 5-7(b), the GRO-TDC is clearly able to resolve a 1.2ps<sub>pp</sub> signal,

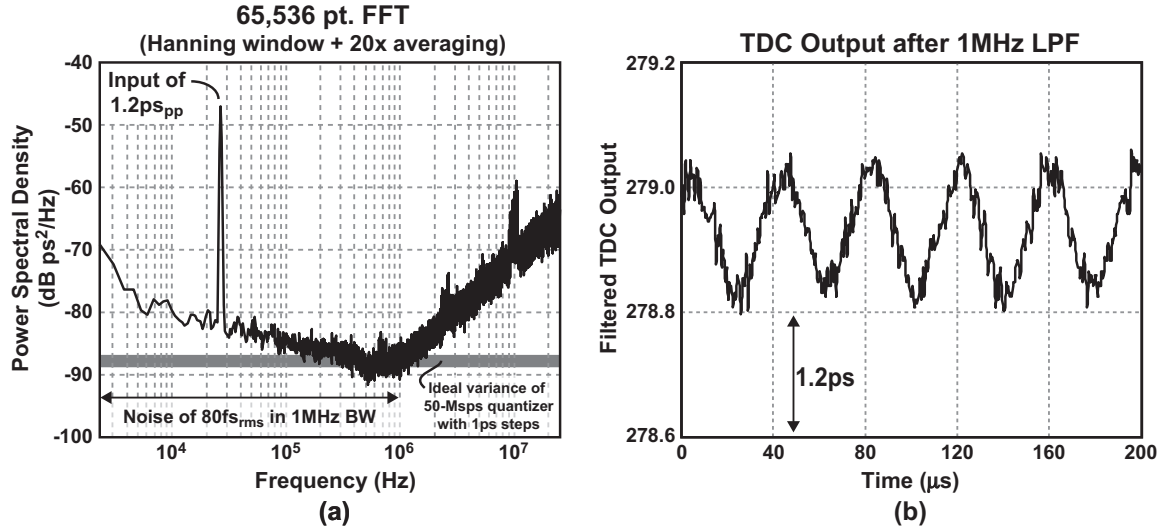


Figure 5-7 Measured GRO-TDC output for a 1.2ps<sub>pp</sub>, 26kHz input signal. (a) plots the signal and power spectral density in the frequency domain, and (b) is a transient view of the output after digital low-pass filtering with a 1MHz bandwidth

whereas a classical quantizer with 1ps resolution would struggle due to the lack of quantization noise scrambling. In fact, the integrated noise of the GRO-TDC from 2kHz to 1MHz is below 80fs<sub>rms</sub>, which includes the noise of both the GRO and the off-chip buffer delay.

When considering how  $T_{skew}$  affects the noise-shaping of the multi-path oscillator, recall that our hypothesis from earlier was that if  $T_{skew}$  could be reduced below the level of physical random processes, then it would be scrambled and contribute a negligible amount of error to the overall TDC output. To conservatively estimate the overall GRO-TDC jitter due to random physical processes, we approximate the thermal noise floor of the GRO-TDC by taking the minimum PSD value of  $-88\text{dBps}^2/\text{Hz}$  from Figure 5-7(a). This implies that the rms jitter for the entire TDC bandwidth due to thermal noise alone is about 281fs<sub>rms</sub>. By comparison, the maximum simulated *peak-to-peak* error of  $T_{skew}/T_q$  from Figure 3-27 is less than 0.025. For  $T_q = 6\text{ps}$ , the gating skew error in units of time is 150fs<sub>pp</sub> (107fs<sub>rms</sub>).

Although the simulated gating skew error for the multi-path GRO-TDC is below its thermal noise floor, which should inherently scramble the GRO phase with adequate magnitude to linearize the performance, we do observe a small deadzone in

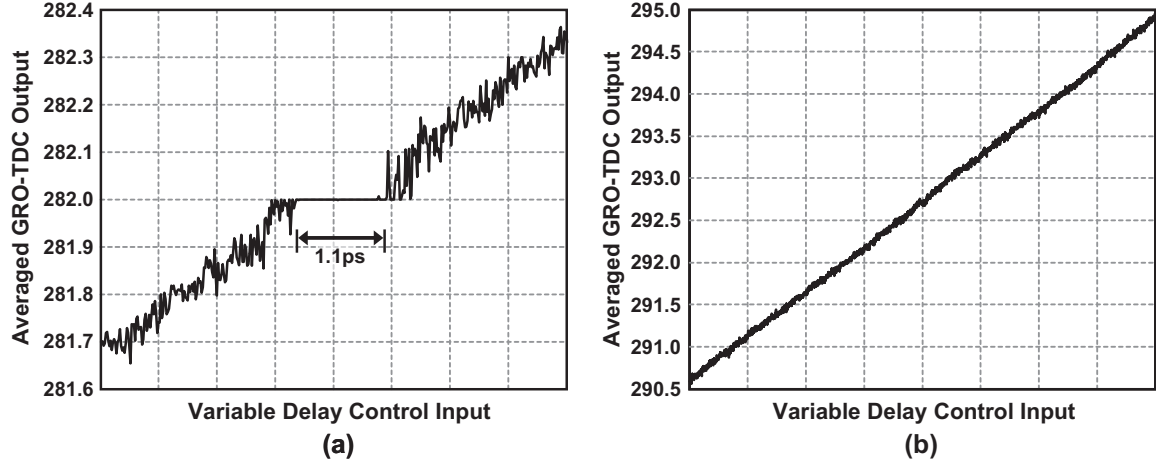


Figure 5-8 A measured DC transfer characteristic for the multi-path GRO-TDC that demonstrates (a) the presence of small deadzones for TDC outputs at  $2NK$ , and (b) linear behavior for integer TDC outputs

the multi-path GRO for the special case when the input time is close to an integer multiple of the GRO period,  $T_{in} = KT_{osc}$ , where  $K$  is an integer. This result is shown in Figure 5-5(a). Recall in Section 3.1.4 that the most sensitive location for deadzone behavior is when the GRO is stopped on the exact same transition for each measurement, since this is similar to injection-locking the GRO with the TDC sampling frequency. Therefore, we can hypothesize that while the contribution of  $T_{skew}$  with a period of  $2T_q$  has been reduced dramatically compared to the inverter-based architecture, the mismatch between delay elements is now the dominant source of  $T_{skew}$ , and this error is periodic with  $T_{osc} = 2NT_q$ .

For the multi-path GRO, no deadzones are evident for GRO-TDC outputs other than at  $2NK$  (e.g. Figure 5-5(b)), and the size of the worst-case deadzone is only 1.1ps. Assuming that the size of this deadzone corresponds with the peak-to-peak error of  $T_{skew}$  for the entire GRO phase state, and also assuming that this error is typically scrambled, we can expect that the GRO-TDC output noise generally be dominated by  $1/f$  and quantization noise as shown in Figure 5-7. Therefore, we can conclude that the multi-path GRO has significantly linearized the converter performance compared to the inverter-based GRO topology. Compared to the inverter-based GRO that demonstrated deadzones even for fractional outputs, in a system

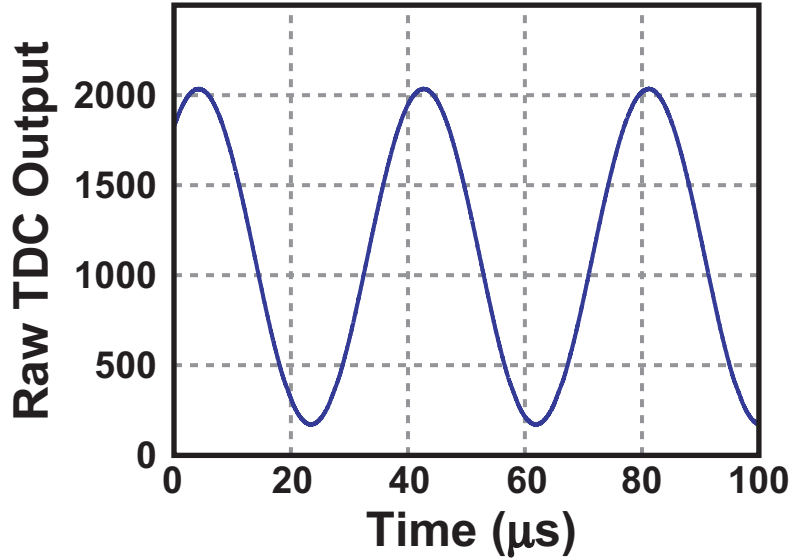


Figure 5-9 Raw measured GRO-TDC output for a 26kHz input signal with an amplitude near full-scale

application avoiding the small range of GRO-TDC outputs that correspond with  $2KN$  is relatively straightforward.

To illustrate the full 11-bit operation of the GRO-TDC, Figure 5-9 plots raw output data from the chip when a 26kHz input is applied with amplitude near full-scale. A frequency domain plot is not given in this case due to input signal quality as described in the previous section. Nonetheless, with a full-scale of 11-bits, the dynamic range in a 1MHz bandwidth is calculated to be 95dB, or an equivalent range of 15.5-bits. The TDC efficiency from before earlier can now be calculated in the 1MHz bandwidth to be 0.23pJ/step, which is almost identical to the efficiency calculated with full bandwidth due to the GRO quantization noise-shaping.

A summary of the 11-bit GRO-TDC performance is shown in Table 5.1. Further demonstration of the measured TDC performance can be seen in Chapter 6, where the GRO-TDC has been proven in a number of system applications.

## 5.4 Discussion

Table 5.2 compares the prototype GRO-TDC to other reported CMOS TDC. Although we notice that there are different examples of TDC with comparable perfor-

Specification	Value
Maximum Sampling Frequency	100 MHz
Range	11-bits
Raw delay resolution	6ps
Effective resolution	1ps @ 50Msps
Integrated noise	80fs, 2kHz-1MHz
Dynamic range	95dB
Power	2.2-21mW (1.5V)
Efficiency	0.2pJ/step
GRO-TDC Area	157 $\mu$ m $\times$ 258 $\mu$ m
Total Chip Area	1.0mm $\times$ 1.0mm
Technology	0.13 $\mu$ m IBM CMOS

Table 5.1 Summary of multi-path 11-bit GRO-TDC measured performance

Ref.	Process Node ( $\mu$ m)	Effective Resolution (ps)	Sample Rate (Msps)	Power (mW)	Area (mm <sup>2</sup> )
[30]	0.8	300	40	17.5	N/A
[46]	0.35	N/A	156	72	1
[13]	0.7	150	265	N/A	10
[18]	1.2	107	63	8	4
[8]	0.35	57	0.033	0.0035	0.12
[9]	0.35	50	0.1	0.75	0.25
[48]	0.8	50	N/A	20	32
[19]	0.8	47	80	N/A	N/A
[10]	0.35	37.5	0.1	150	0.222
[56]	0.8	32	100	350	10
[37]	0.6	30	66	50	5
[43]	0.7	25	N/A	110	10.7
[44]	0.25	24.4	40	N/A	N/A
[27]	0.35	24	150	50	0.6
[71]	0.8	20	0.05	N/A	0.025
[66]	0.09	20	26	2	0.01
[29]	0.35	12.2	0.5	40	5
[23]	0.09	4.7	180	4	0.02
[34]	0.09	1.25	10	3	0.6
<b>This work</b>	<b>0.13</b>	<b>1</b>	<b>100</b>	<b>2-21</b>	<b>0.04</b>

Table 5.2 Comparison with published TDC

mance in any given metric, the GRO-TDC achieves state-of-the art performance in *all* areas, with no calibration of differential non-linearity required.

The drawbacks to the GRO-TDC are similar in nature to issues that many TDC architectures face. For example, a large delay variation across power supply is an issue that is inherently related to the use of digital circuit elements as time references. While the TDC gain can be often be calibrated at the system level, dynamic issues such as power supply coupling can be harder to eliminate, causing possible issues such as spurs in a digital PLL. Additionally, an issue that the GRO-TDC shares with cyclic converters is the linear relationship between power consumption and the input signal. This strong correlation can cause non-linearities at the system level.

The one drawback that is most unique to the gated ring oscillator architecture, the gating skew error from stopping and starting the oscillator, can be a real and significant contribution of error for some GRO implementations. However, we have also shown that these errors can be practically mitigated by proper design and implementation of a multi-path oscillator. The multi-path techniques outlined in this work have not only improved the effective resolution by a factor of 5 compared to classic inverter rings, but also have reduced the gating skew errors to a level comparable to that of random physical processes, which significantly limits their contribution to the overall TDC error. To our knowledge, this work for the first time practically demonstrates a noise-shaping time-to-digital converter with the ability to accurately transfer error across a gap of inactivity from one measurement to the next.

Because of the very high resolution that is possible with the GRO-TDC, the applications that will significantly benefit from this technology are likely to be the most demanding in terms of performance. We will discuss in the chapter to follow a few of these applications that are able to demonstrate lower noise, spurious content, higher bandwidths, etc. as a result of the GRO-TDC performance than would otherwise be possible. The fundamental architecture of the GRO-TDC is compact, efficient, and simple, and therefore can be easily adapted to many other less demanding applications as well, especially if techniques are used to trade resolution for power. Finally, we anticipate that as TDC become more adapted into integrated systems, the use

of digital, high-performance TDC such as the GRO will become more sophisticated, and perhaps lead to the enabling of system architectures that would not be practical in a previous technology.



# Chapter 6

## GRO-TDC applications and discussion

### 6.1 Digital PLL for wireless communication

With the very compact, inexpensive, and reliable digital signal processing capability that continues to improve with more advanced CMOS processes, traditional analog circuit functions over time have been replaced by digital implementations. The area of frequency synthesizers is no exception to this rule, with the recent emergence of digital phase-locked loops (PLL) as an architecture capable of delivering performance adequate for wireless communication standards [7, 15, 25, 67, 72, 77].

As shown in Figure 6-1, the concept of a digital PLL is to replace the analog phase detector, charge pump, loop filter, and VCO with a TDC, digital loop filter, and digitally-controlled oscillator. The primary advantage of this approach is that the large passive components required for the analog loop filter can be replaced with a relatively simple digital FIR filter, which can either reduce component count or silicon area. As we will soon see, there are other aspects of a digital PLL implementation that can take advantage of the signal path being in the digital domain.

Because we can see the similarities in Figure 6-1 between the analog and digital PLL structures, we can leverage much of the modeling developed for analog PLL in the new digital architecture. We refer the reader to [51, 52] for more details on this

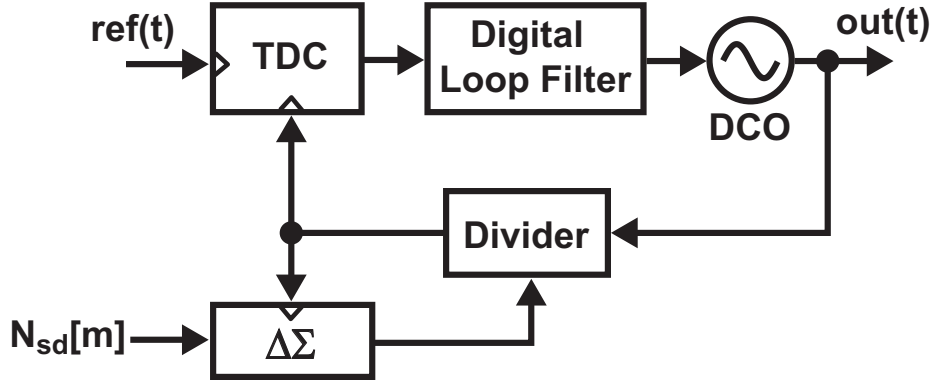


Figure 6-1 Basic architecture of a fractional-N digital PLL

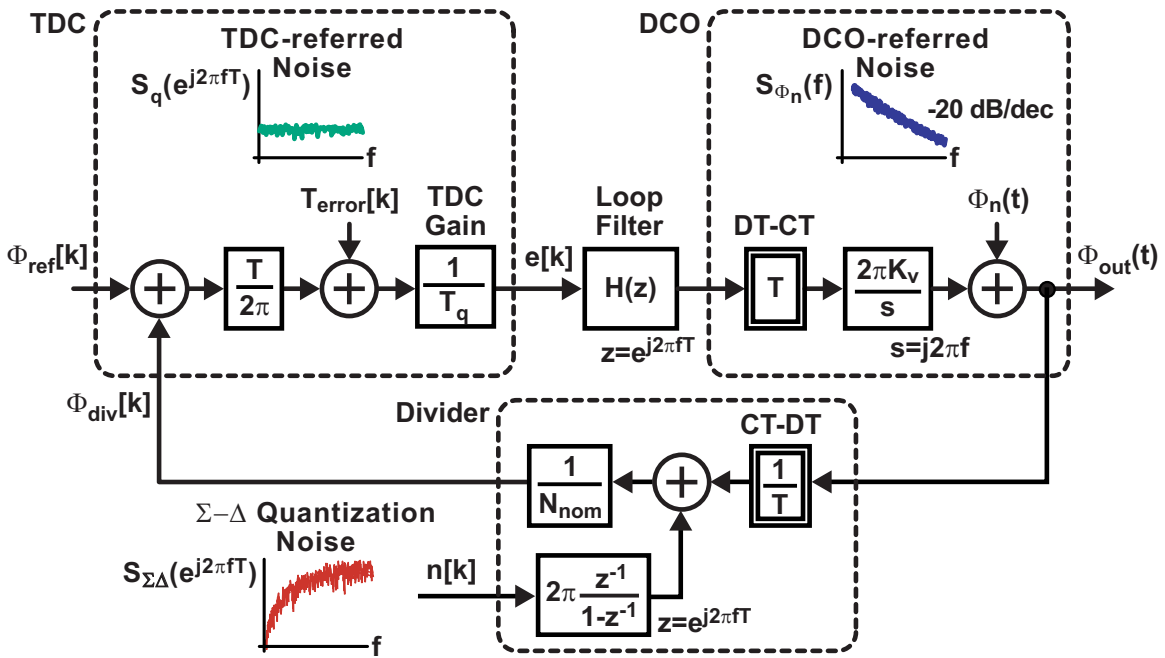


Figure 6-2 A general model for the fractional-N digital PLL

background. Therefore, we show in Figure 6-2 a model for the fractional-N digital PLL that includes noise contributions from the TDC, VCO, and  $\Sigma\Delta$  quantization. Although the GRO-TDC quantization noise has been shown to be first-order shaped, we depict a white PSD for simplicity here corresponding to thermal noise limitations.

Note that in this model the TDC replaces the analog phase and frequency detector (PFD) and charge pump, which means that its noise performance will similarly be low-pass filtered in the PLL output phase noise according to the PLL closed-loop transfer function  $G(f)$ . In fact, this low-pass response is clearly visible when the model is

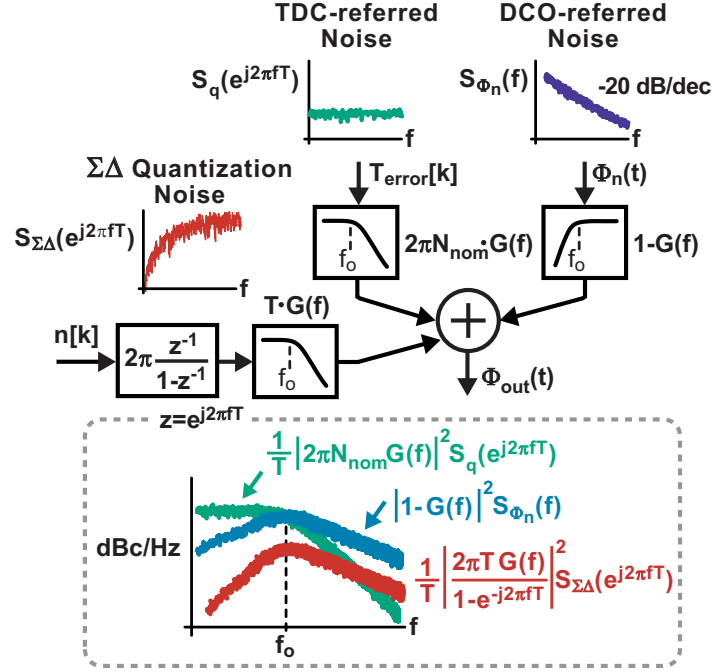


Figure 6-3 Transfer functions for the three primary contributions to the digital PLL phase noise

expanded in Figure 6-3 to consider how each of these three noise sources contributes to the output phase noise. Based on the figure, we have that the contribution to the PLL output phase noise from the TDC is

$$S_{\phi_{out}}(f) = \frac{1}{T} |2\pi N_{nom} G(f)|^2 S_q(e^{j2\pi f T}). \quad (6.1)$$

To provide a simple example of how typical TDC resolution will map into PLL phase noise, we now consider a delay-chain TDC with resolution of 20ps. In Figure 6-4(a), we can see that for a 50kHz PLL bandwidth with typical VCO and  $\Sigma\Delta$  noise parameters, the TDC quantization noise does not contribute significantly to the phase noise at any offset frequency. However, when a larger loop bandwidth of 500kHz is desired, the TDC noise will dominate the output phase noise for offset frequencies up to 2MHz. In addition, the  $\Sigma\Delta$  quantization noise becomes the other source of significant noise in the system, which is not acceptable. Increased loop bandwidth is desirable for locking time, in-loop modulation, etc., and we see that this requires both a high-resolution TDC as well as  $\Sigma\Delta$  quantization noise suppression.

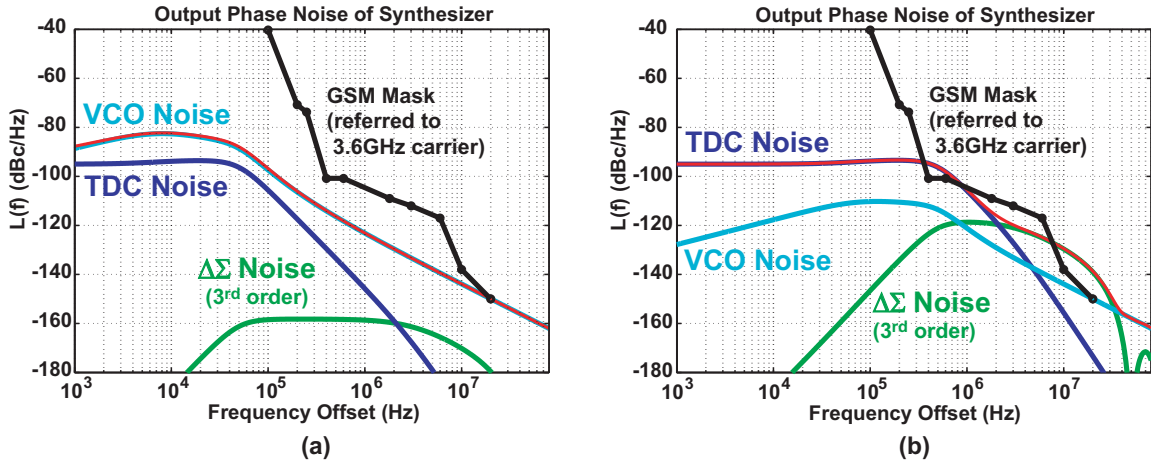


Figure 6-4 Calculated phase noise of a 3.6GHz fractional-N digital PLL using an inverter-based TDC with 20ps resolution and assuming (a) a 50kHz loop bandwidth output, and (b) a 500kHz loop bandwidth

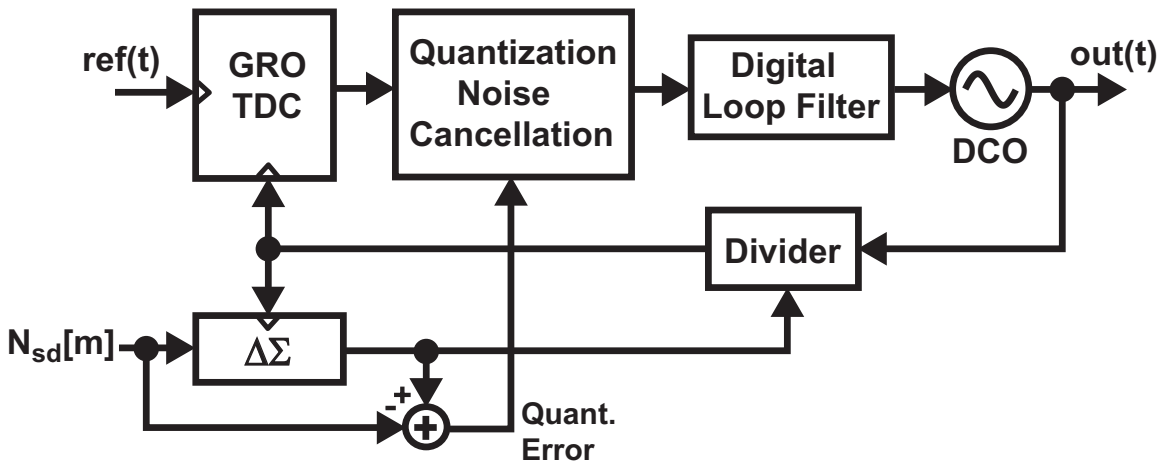


Figure 6-5 A fractional-N digital PLL using the GRO-TDC and quantization noise cancellation

A conceptual block diagram of a digital PLL using the GRO-TDC and quantization noise cancellation is shown in Figure 6-5 [25]. In this case, the high-resolution from the GRO-TDC allows the quantization error from the  $\Sigma\Delta$  division to be accurately subtracted in the digital domain. Accomplishing this compensation digitally is quite simple to implement [25], and eliminates the problems with mismatch that plague analog implementations. As a result of the  $\Sigma\Delta$  noise suppression and the improved resolution of the GRO-TDC, we can see in Figure 6-6 the much improved phase noise despite the large 500kHz PLL bandwidth.

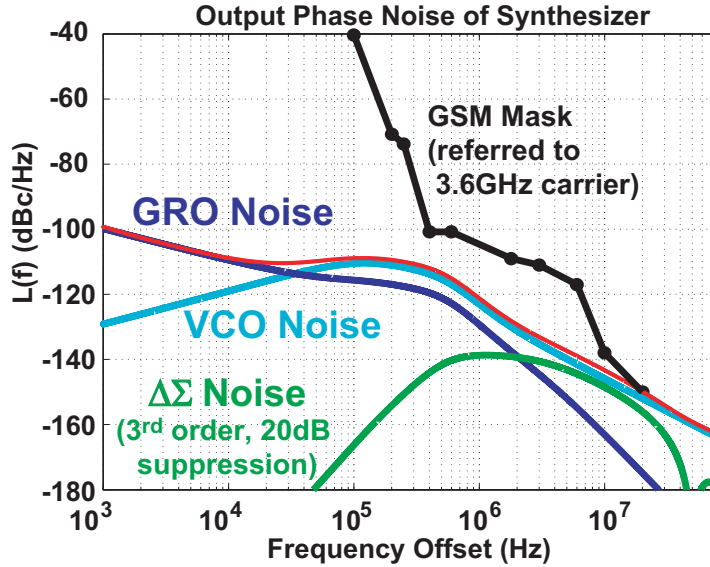


Figure 6-6 Calculated phase noise of a 3.6GHz fractional-N digital PLL using the prototype GRO-TDC

To substantiate these calculations, we can refer to a custom digital PLL that was implemented using the GRO-TDC in a  $0.13\mu\text{m}$  CMOS process [25]. The fully integrated  $1.4\text{mm}\times 1.4\text{mm}$  chip has an active area of  $0.95\text{mm}^2$  including an on-chip VCO, the GRO-TDC, and digital circuitry. Current consumption is 26mA from a 1.5V supply, excluding the VCO output buffer that consumes 7mA from a 1.1V supply. Figure 6-7 shows the measured phase noise at 3.67GHz from an Agilent Signal Source Analyzer E5052A, where the results are shown with and without cancellation of the quantization noise. As the figure reveals, greater than 15 dB noise cancellation is achieved such that out-of-band noise is dominated by the VCO. With noise cancellation enabled, the in-band noise is -108dBc/Hz at a 400kHz offset, and out-of-band noise is -132dBc/Hz and -150dBc/Hz at 3MHz and 20MHz offsets, respectively. In particular, the very low in-band phase noise verifies the very high-resolution of the GRO-TDC achieved through noise-shaping.

To examine how the  $1/f$  phase noise below 10kHz offset frequencies in this measurement can be compared to the GRO-TDC chip measurements, we first convert from the power spectral density shown in Figure 5-7 to a TDC quantization noise,  $S_q(e^{j2\pi fT})$ , by multiplying with  $2 \cdot 10^{-24}/T$ , which accounts for the double-sided to

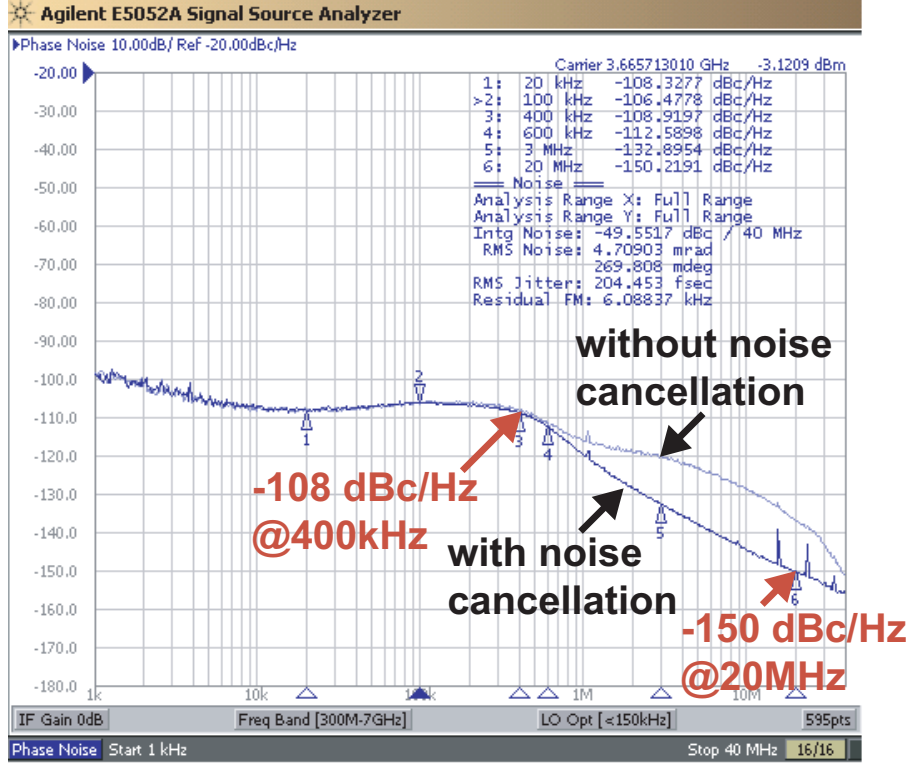


Figure 6-7 Measured output phase noise from the prototype 3.6GHz fractional-N digital PLL using the GRO-TDC

single-sided spectral densities, the TDC sampling rate, and the unit change from picoseconds to seconds. For example, at 10kHz offset, the GRO-TDC PSD from Figure 5-7 is approximately  $-79\text{dBps}^2/\text{Hz}$ , which in this case means that  $S_q \approx -239\text{dB}$ . When this value of  $S_q$  is substituted into Equation 6.1, we find that

$$S_{\phi_{out}}(10^4) = 50 \times 10^6 |2\pi \frac{3.6 \times 10^9}{50 \times 10^6} G(10^4)|^2 10^{-239/10} \quad (6.2)$$

$$S_{\phi_{out}}(10^4) = 12.8 \times 10^{-12} |G(10^4)|^2 = 12.8 \times 10^{-12} |1|^2 \quad (6.3)$$

$$10 \cdot \log(S_{\phi_{out}}(10^4)) = -108.9\text{dBc/Hz} \quad (6.4)$$

This calculated value is about 1dB lower than the digital PLL noise seen in Figure 6-7, which can likely be attributed to  $1/f$  noise added from other PLL circuits in the signal path. As we will see in the next section, we can expect that any increase in delay or TDC measurement offset to result in additional noise.

Note that the GRO-TDC used in this high-performance digital PLL requires no

calibration of TDC differential non-linearity, and does not receive any special treatment at the system level to avoid deadzones or limit-cycle behavior. In addition, the reported phase noise results are robust, repeatable, and consistent over time, which proves the robust implementation of the GRO and the employed phase measurement techniques.

Finally, the reference spur was measured with an Agilent Spectrum Analyzer 8595E to be -65dBc, and fractional spurs were tested from 3.620 GHz to 3.670 GHz. The worst case spurs are -42dBc at carrier frequencies of 3.6496 and 3.6504GHz, and typical spurs were measured below -64dBc. Reduction of fractional spurs is an ongoing research area for PLL for both analog and digital PLL [74], since achieving excellent spectral purity is an important consideration for fully-integrated synthesizers. Although the fundamental issues of crosstalk and power supply coupling can be improved through careful layout and design, in the future we may expect significant improvement in this area from novel system architecture that can take advantage of either the high-performance or digital nature of converters such as the GRO-TDC.

## 6.2 PLL for timing synchronization

While wireless communication standards are a primary application of commercial interest, there are a number of other applications for low-noise PLL with much different sets of specifications. In this section, we leverage the building blocks from the previous section to demonstrate a prototype digital PLL for synchronizing an extremely low-noise 100MHz crystal oscillator with an arbitrary timing reference, which in this case is 98MHz. In fact, a primary advantage of implementing the PLL with the high-performance GRO-TDC is that the loop parameters, performance, and even the architecture may be adjusted according to the specific application requirements with a relatively small amount of redesign or with a reconfigurable PLL.

Precise, low-noise, master timing references are critical for many communication and instrumentation systems, especially when dealing with locating or steering over very large footprints. A primary challenge in this field is to derive a large set of possi-

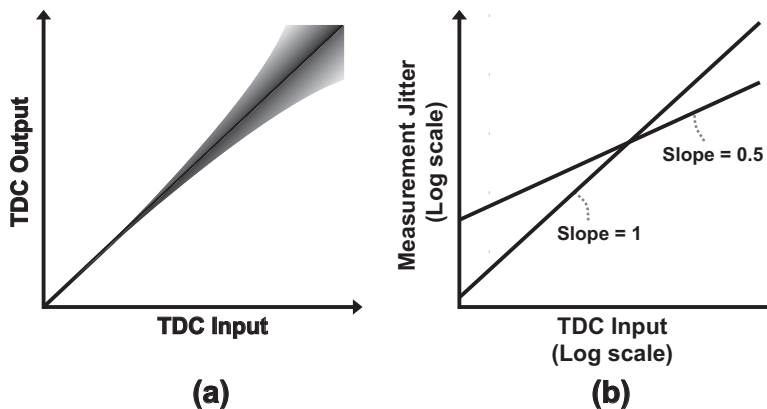


Figure 6-8 The relationship between the magnitude of the TDC input and the random measurement error due to thermal and  $1/f$  noise. (a) depicts the TDC input / output transfer characteristic, and (b) generally relates the statistical measurement jitter to the TDC input

ble output frequencies, all with very high accuracy and low-noise, from a single system clock. Although typical timing reference frequencies are comparable or below crystal oscillator frequencies in the wireless communication industry, the normalized phase noise performance for these applications can often be 30dB lower than standards such as Bluetooth, or even GSM. Another primary difference between these applications is that for synchronization of a frequency reference, we are primarily concerned with adjusting the output frequency to compensate for slow drift due to temperature and other environmental changes. Therefore, a very low loop bandwidth of 10-100Hz is needed, which can be leveraged (through Equation 6.1) to reduce the impact of TDC noise significantly.

Even despite the very low loop bandwidths that are permissible in this application, the GRO-TDC  $1/f$  noise will still have non-zero contribution to the output phase noise. To consider how this contribution can be minimized, in Figure 6-8(a), we see that a large DC value for the TDC input will result in increased uncertainty in the TDC output due to the accumulating jitter of the TDC delay elements. Another way to view the same issue, as presented in [20] and shown in (b), is to plot the



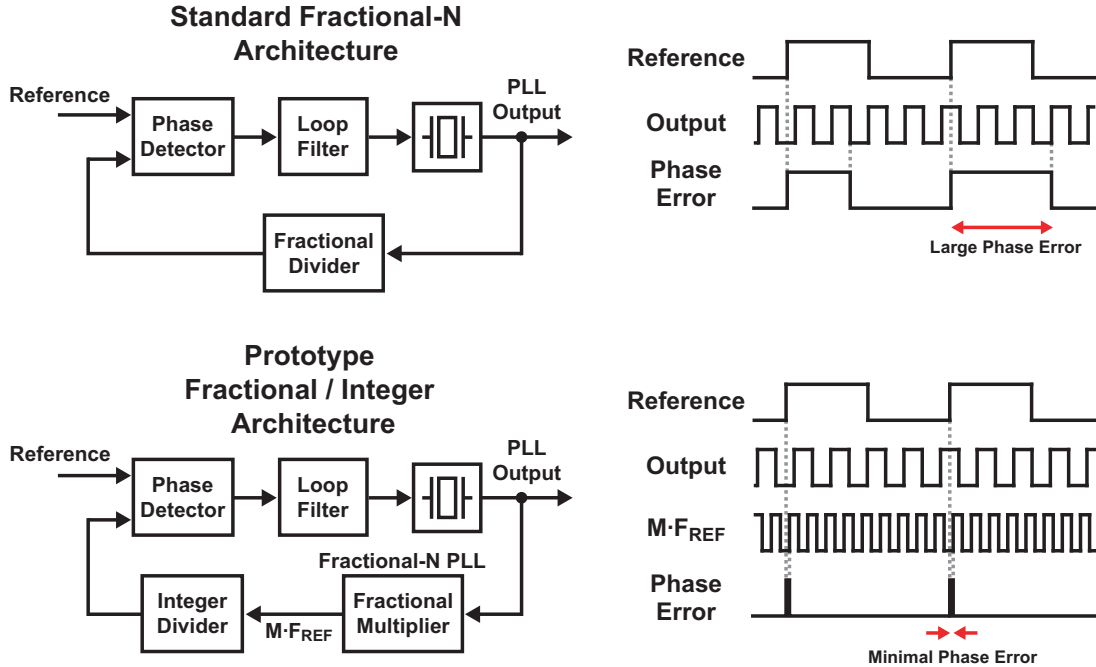


Figure 6-9 Concept behind the proposed fractional / integer synthesizer that minimizes the length of time input into the GRO-TDC

jitter of a measurement output vs. the length of the measurement interval with a log-log scale. In either case, the conclusion is the same in that a smaller average TDC input will reduce its overall noise contribution (Note that this conclusion describes a fundamental issue of time uncertainty, and is equally valid for digital as well as analog PLL).

In fractional-N digital PLL, the TDC offset must be set large enough to accommodate many periods of the VCO, since the divider value is dithered within a range of 4-8, depending on the order of  $\Sigma\Delta$  modulation. This large offset shown on the top of Figure 6-9 does introduce additional noise. However, in many communication systems this issue is not of concern for two reasons. First, with an output frequency typically larger than 1-2GHz, even a TDC offset of 10 VCO periods represents a relatively small length of time. Second, typical wireless communication requirements for in-band noise are not high, as evidenced by the use of low-cost, relatively high-noise crystal oscillators (high-noise when compared to the requirements for the current application).

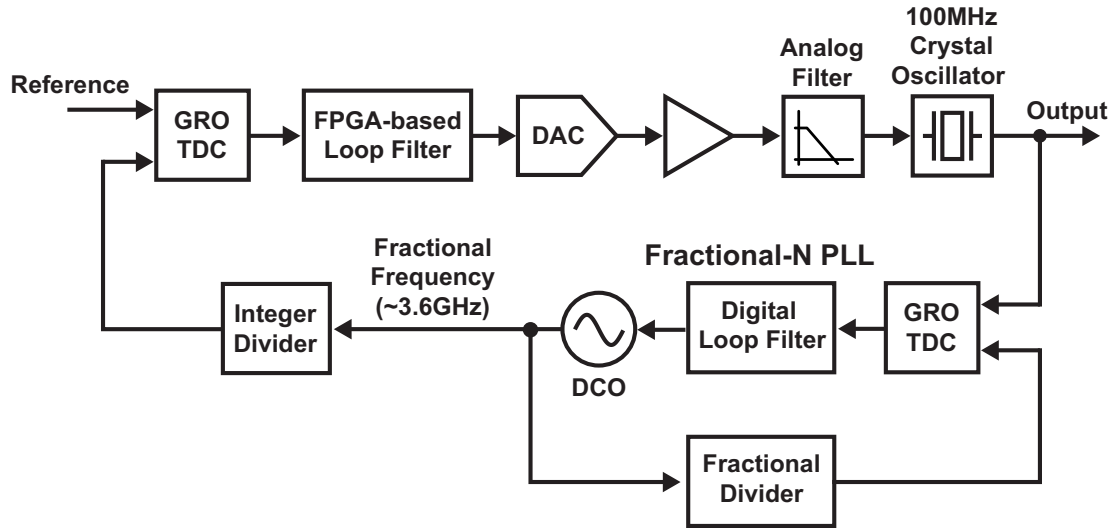


Figure 6-10 Prototype implementation of the fractional / integer synthesizer

For synchronizing a 100MHz crystal to a timing reference with even lower frequency with the lowest possible noise, it is clear that a classical fractional-N architecture is non-optimal. To achieve a much smaller average TDC input, as shown on the bottom of Figure 6-9, we instead propose a fractional / integer PLL architecture. In this architecture a fractional divider is implemented by first multiplying the 100MHz crystal output with a fractional-N digital PLL, and then following with an integer division. Although there are two GRO-TDC in the signal path, which may intuitively imply a larger noise, the sum of TDC input widths here is much smaller than in a classic fractional-N topology. Specifically, the fractional-N GRO-TDC sees an average input of less than 2ns, and the primary loop phase error can be maintained at a very small value because the frequency of the feedback signal is synchronized to be equal the reference frequency.

A prototype of this fractional / integer PLL synthesizer shown in Figure 6-10 is implemented by combining the fractional-N synthesizer in [25] with a custom PCB that includes a multi-path GRO-TDC [69], an FPGA-based loop filter, a DAC, amplification, and a single-pole passive RC filter. The digital IIR loop filter is programmed in the FPGA with three taps using bit-shift operations to simplify the loop filter multiplications, since the precision is 64-bit. Although the bit-shift multiplications

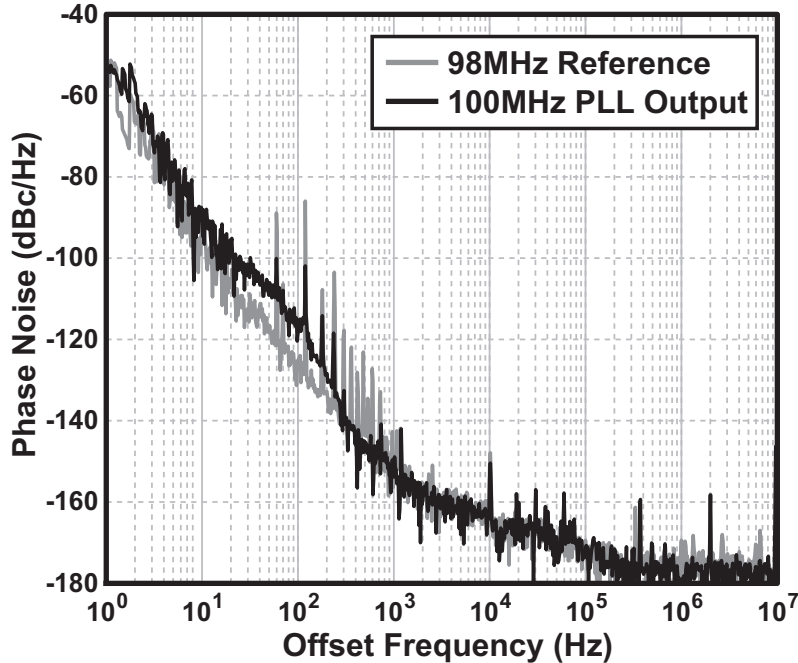


Figure 6-11 Measured 100MHz phase noise of the prototype fractional / integer synthesizer

limit the ability to arbitrarily define the loop dynamics, issues such as settling time and loop bandwidth are somewhat flexible in this application.

A 98MHz, fixed-frequency, temperature-regulated, quartz crystal oscillator is used as the timing reference frequency, and a tunable 100MHz oscillator with the same characteristics is used for the output frequency. The tuning gain of the 100MHz oscillator,  $K_v$ , is about 500Hz/V. Both crystal oscillators are manufactured and provided by Frequency Electronics, Inc.

Measured phase noise performance for both the 98MHz timing reference as well as the 100MHz synchronized output are shown in Figure 6-11. The overall PLL has Type-II dynamics, and has a loop bandwidth for this measurement set approximately to 10Hz. Although the entire loop filter can be implemented in discrete-time, due to the more relaxed size and cost requirements there is little penalty in this application for including a coarse RC analog filter with a pole at about 100Hz to attenuate spurs and noise from the FPGA and DAC. As seen in the measured data, all noise outside the frequency range of 10-300Hz is limited by the crystal oscillators, and a peak deviation from the crystal noise is about 10dB for frequencies of 50-100Hz.

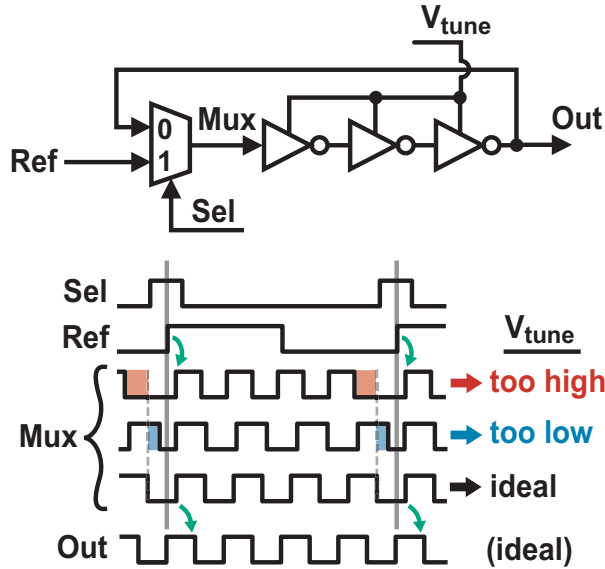


Figure 6-12 Concept of a multiplying delay-locked loop

The PLL noise performance demonstrated in this prototype for very low-offset frequencies is competitive with all-analog implementations, yet the result is obtained while maintaining the versatility and portability. of an all-digital PLL. The proposed fractional / integer architecture is easily adaptable to accomodate different frequency plans for both the reference as well as the radio frequency. Finally, while the fractional / integer prototype underutilizes the 3.6GHz on-chip output, if fractional-N multiplication is required at the application level, a hybrid approach using a variety of off-chip oscillators can also be considered.

### 6.3 Very high-resolution frequency measurement

Other than digital PLL, there are many other applications that can use the GRO-TDC technology as well. For example, timing circuits such as clock and data recovery are well-suited to benefit from oversampling and high-resolution TDC. In this section, we consider how the GRO-TDC can be utilized in a multiplying delay-locked loop (MDLL) application to address an analog matching issue through oversampling and digital processing.

As shown in Figure 6-12, MDLL operate by replacing every  $N^{th}$  edge of a naturally

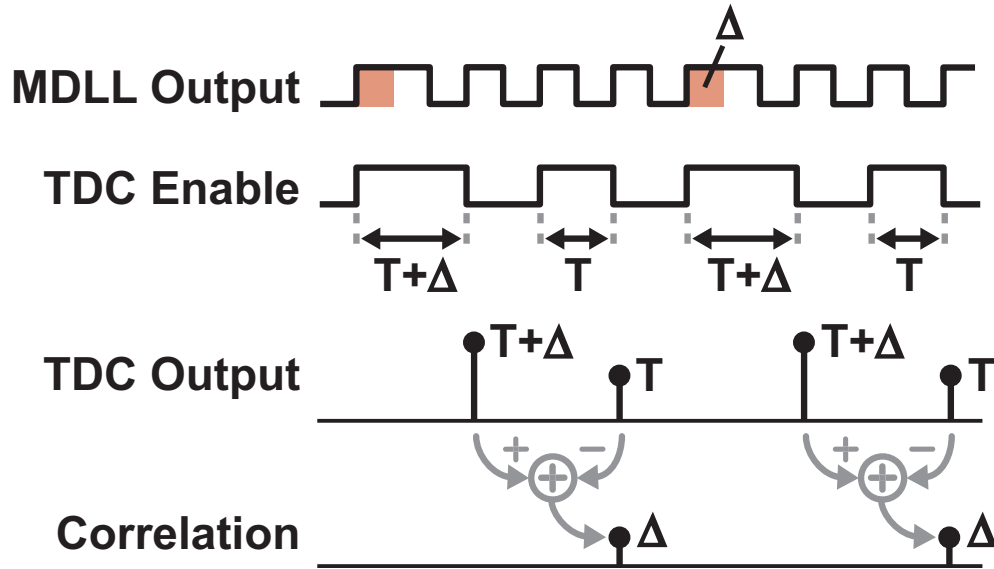


Figure 6-13 Correlation of spurs to period measurements

running ring oscillator VCO with a reference frequency edge, where  $N$  corresponds to the frequency multiplication factor. This has been shown to allow significant suppression of jitter caused by phase noise of the VCO [2]. However, as shown in the figure, an incorrect setting of the  $V_{tune}$  voltage on the VCO (which tunes its corresponding frequency) leads to substantial undesired “deterministic jitter” due to corresponding periodic changes in the output period [1-2, 4-6].

Because elimination of this deterministic jitter is quite challenging in the analog domain due to mismatch [4,5], an alternate approach is proposed in [21] that uses the GRO-TDC to measure and compensate for this error. With the approach illustrated in Figure 6-13, only one signal is examined, *Enable*, whose pulse width alternates twice every reference cycle between the free running period of the oscillator,  $T$ , and the period of the error-affected cycle,  $T + \Delta$ . By doing a relative comparison of each consecutive pulse period of the *Enable* signal, the value of  $\Delta$  can be obtained in a manner such that the issue of mismatch is greatly mitigated since only one signal is being examined.

The overall MDLL prototype, which is shown in simplified form in Figure 6-14, consists of two integrated chips, a GRO-TDC chip and another with the MDLL core logic, an FPGA board that implements the correlator, accumulator, a first-

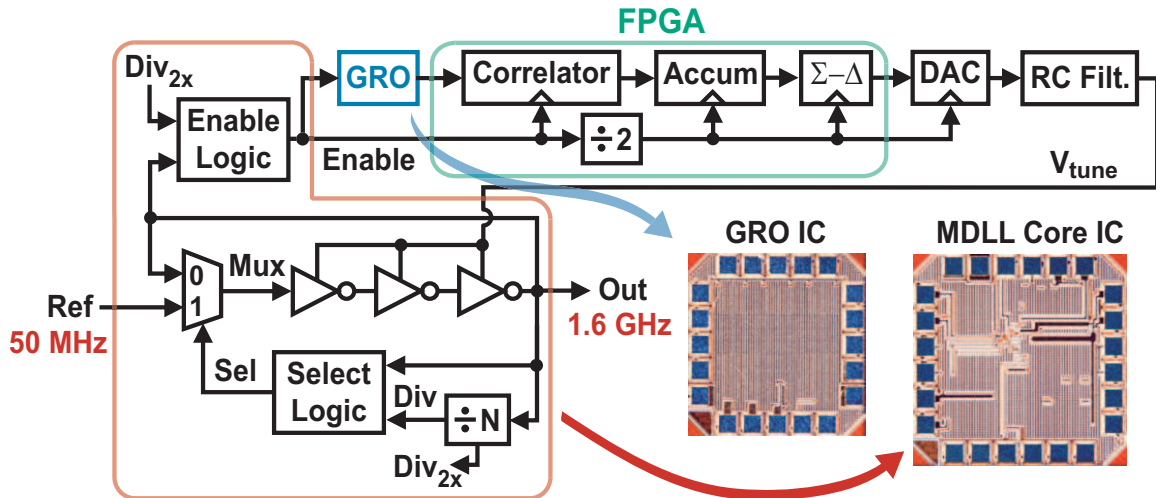


Figure 6-14 A block diagram of the implemented MDLL prototype

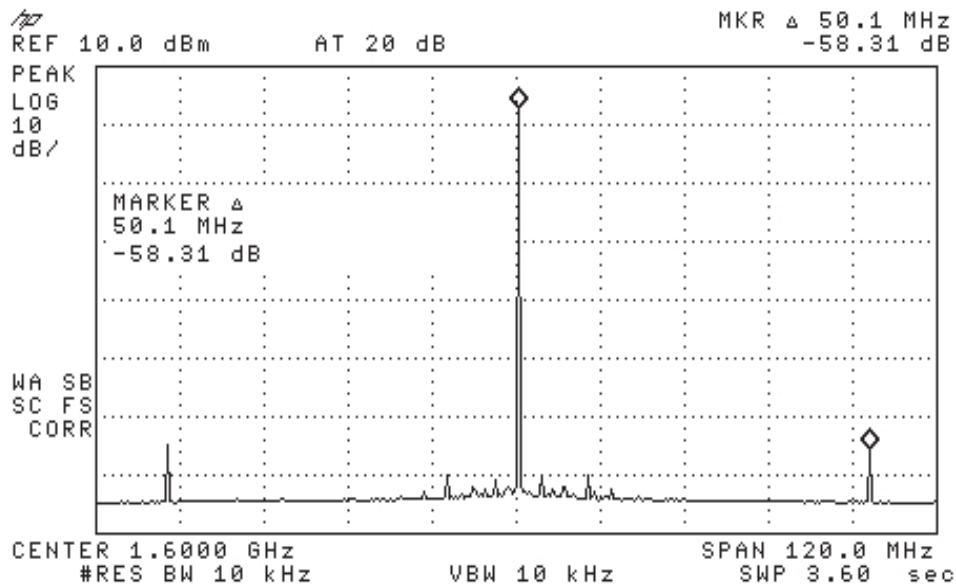


Figure 6-15 Measured -58dBc spurious performance from the MDLL prototype

order, digital  $\Sigma\Delta$  modulator, and other basic logic operations, an off-chip, low noise, 100MHz reference source, and a commercially available 16-bit DAC. While 16-bits are available for the DAC, only 8-bits are used in conjunction with a first order  $\Sigma\Delta$  modulator. Notice that again in this architecture, the key elements are the GRO-TDC, a custom oscillator, a DAC, and some digital logic, which highlights how a high-performance TDC can be leveraged for multiple applications by adding a small number of new components.

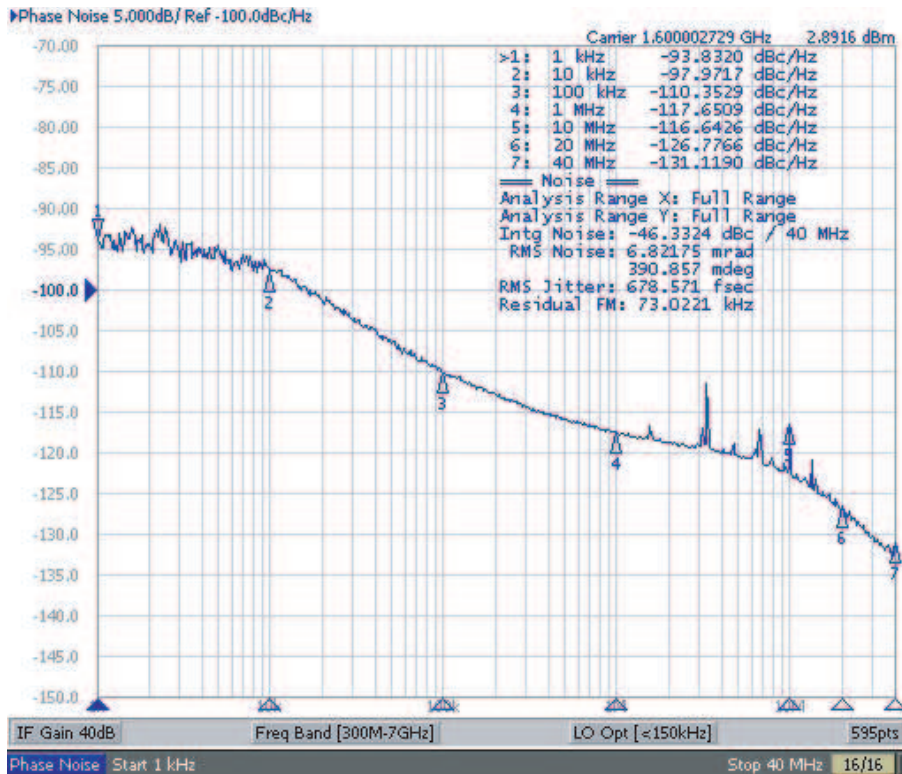


Figure 6-16 Measured MDLL phase noise at 1.6GHz output frequency

As the measurement of the MDLL output with HP8595E spectrum analyzer reveals in Figure 6-15, the reference spur of the MDLL prototype is -58.3dBc. From this number the deterministic jitter is reported to be  $760\text{fs}_{pp}$ , which validates the proposed techniques ability to achieve sub-picosecond deterministic jitter. As an additional measure of the performance, the phase noise of the MDLL output is shown in Figure 6-16. The random jitter can be estimated by integrating the measured phase noise from 1kHz to 40MHz, and is reported to be  $679\text{fs}_{rms}$ .

Therefore, the proposed MDLL architecture leverages the GRO-TDC in a unique way to achieve a very low level of both random and deterministic jitter. In this case, the TDC is not used to compare an output signal against a reference frequency as in a digital PLL, but rather it is used to directly measure the periods of the output signal. Without any external reference, the digital GRO-TDC output can then be processed to identify undesired properties in the output signal, and feedback can be applied as compensation. Not surprisingly, identifying spurs is possible for other architectures

as well (e.g. pulse injection-locked oscillators [22]), and the digital processing can easily be modified to compensate for other spectral content as well. In fact, given the high-resolution TDC now available as a tool for designers, this general technique appears to be very promising for a wide variety of future system architectures.



# Chapter 7

## Background on VCO-based quantizers

High-bandwidth and high-resolution ADC implementations face many challenges for circuit designers using nanometer-scale CMOS processes, and yet the demand for ADC performance is unrelenting. With limited power supply voltages and decreasing gain for the minimum size transistors, achieving large dynamic range for high speed converters is difficult for classical architectures that rely on precision operational amplifiers and comparators. At the same time, advanced CMOS processes offer very fast switching speed and high transistor density that can be utilized in interesting and unconventional ways.

VCO-based quantization carries the very attractive aspect of having a highly digital implementation, and as a result these structures strongly take advantage of Moore's law and the enormous industrial investment in digital process development. Reducing the digital gate delay improves both the resolution of the VCO-based quantizer as well as the achievable sample rate; a 9dB improvement in signal-to-quantization noise results from a 50% reduction in gate delay. As such, there has been an increasing level of interest in using VCO-based quantization to achieve analog-to-digital conversion (ADC) in modern mixed-signal circuits [1, 28, 31, 39, 45]. However, one challenge for VCO-based quantizers is to mitigate the poor linearity that can severely limit ADC performance.

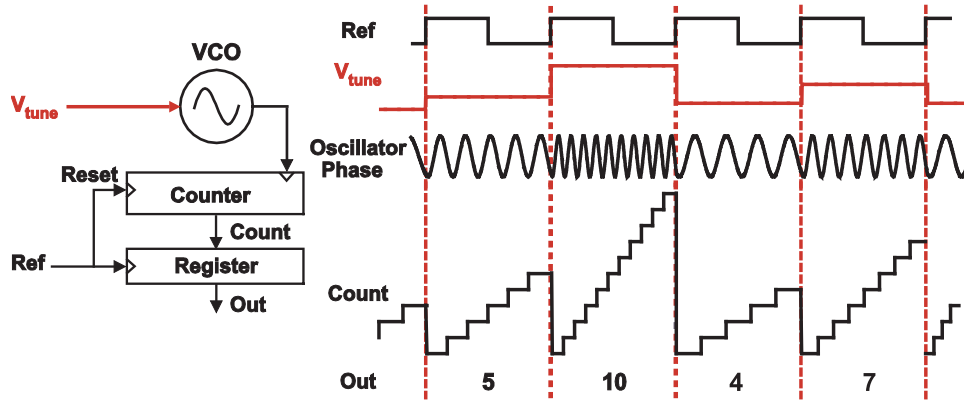


Figure 7-1 Simple VCO-based ADC

To address such issues from an architectural perspective, in the following chapters we explore the use of a multi-phase voltage-controlled oscillator (VCO) as a quantizer element in oversampling continuous time (CT) ADC.

## 7.1 Common VCO-quantizer implementations

One of the earliest reported VCO-based ADC was proposed more than thirty years ago for use in a digitally controlled switching regulator [5], and a similar topology was later applied in the superconductivity community five years later [26]. While the exact implementation of the converters differed due to the choice of technology (i.e., semiconductor vs. superconductor), the overall architecture for each was essentially the same, and is shown in Figure 7-1. Here, the ADC comprises a single-phase output VCO, a counter, and a sampling register. As the analog input signal modulates the VCO frequency via the tuning node, the counter continuously accumulates the number of transitioning edges during the sample period. At the end of the period, the resulting count is sampled by a register, the counter reset to zero, and the process repeated. As can be seen from the figure, the sampled count is proportional to the oscillation frequency of the VCO, and therefore the input signal level.

One very interesting aspect of VCO-based quantizers is their potential ability to achieve first-order noise-shaping of their quantization noise [24]. Figure 7-2 illustrates this principle in simplified form by examining the counting process of one phase of the

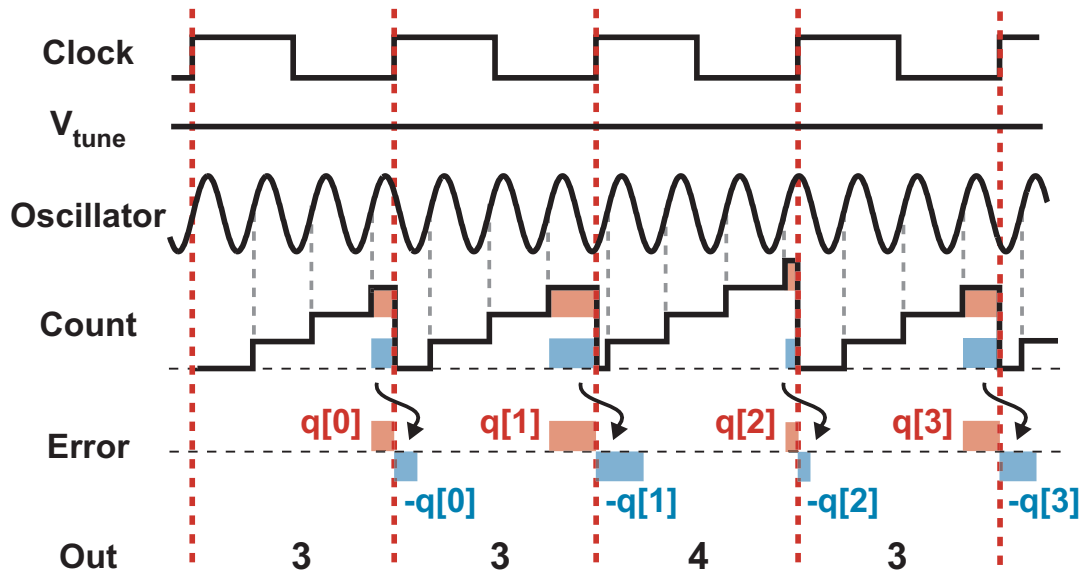


Figure 7-2 First-order noise shaping of a classical VCO-based ADC

oscillator with a constant  $V_{tune}$  input. The key point here is that the truncation error  $q[k]$  at the end of a clock period boundary is not lost, but rather it is accounted for in the following measurement. The accumulation of phase error from sample to sample is then maintained to within a single quantization level, which leads to a time-varying output even with a constant input. This is shown in the figure by the extra count in the third sample of the sequence [3 3 4 3]. Examination of the quantization error signal, *Error*, in the figure reveals that it takes the form

$$Error[k] = q[k] - q[k - 1], \quad (7.1)$$

where  $q[k]$  corresponds to the truncation error that occurs at the edge of each clock period boundary. Under the assumption that  $q[k]$  is white in its noise profile, Equation 7.1 reveals that the overall quantization error is first-order noise-shaped.

The oscillator-based ADC of Figure 7-1 and 7-2 can be related to the well-known slope-based converter (single or dual slope) [64] in that both architectures translate an input voltage signal into the time-domain, where it is then quantized. However, we make a key distinction that the single-slope ADC effectively *compares* an input signal to an integrating waveform, while the VCO-based quantizer actually *integrates*

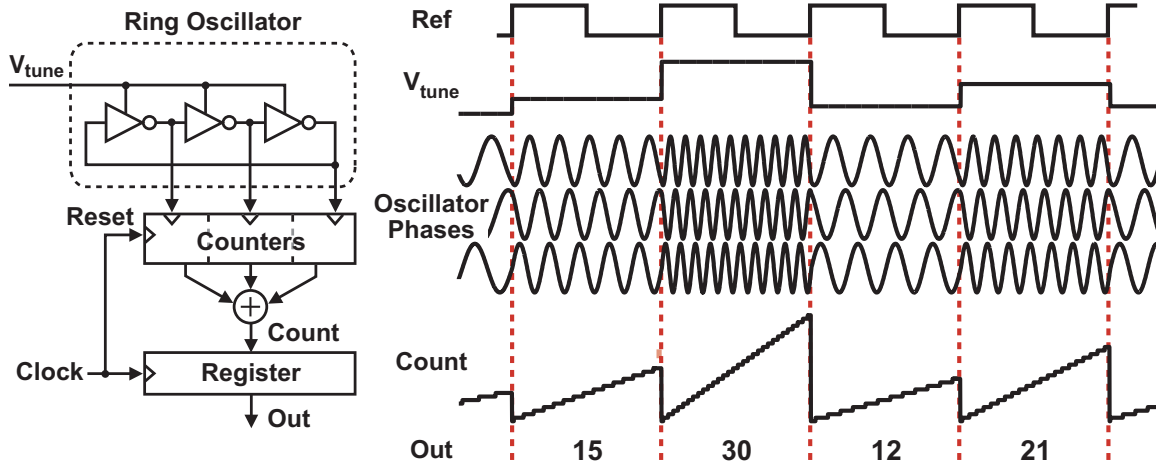


Figure 7-3 Improved resolution by counting positive and negative transitions of a multi-phase VCO

the input signal in continuous time. As a result, the slope-based ADC lacks noise shaping, and is not well-suited for oversampling applications. In fact, the linear tradeoff between sampling rate and dynamic range limit the slope-based Nyquist converters to high-resolution applications only when a very low input bandwidth is desired. Regardless, the many variations on these time-based circuits for ultra low-power sensor applications highlight the efficiency of combining voltage or current integration with digital clocks [14, 33, 73, 75].

To improve the raw resolution of the VCO-based quantizer, the VCO needs to generate more edge transitions during the sample period. This can be accomplished by adopting a ring-oscillator structure to generate  $N$  multiple VCO output phases, as proposed in [24] and shown in Figure 7-3. Here, each positive and negative phase output from the ring-VCO drives a counter input, producing a total count with higher resolution by a factor of  $2N$  compared to the single-phase VCO-based ADC of [5, 26] for the same period.

Although the VCO-based quantizer shown in Figure 7-3 provides a convenient illustration of the basic principles involved, its practical implementation is problematic due to the reset operation that is used on its counters. Indeed, in cases where a VCO edge occurs in close proximity to the reset signal (which will occur quite often), the measured edge count is likely to become corrupted due to the propagation

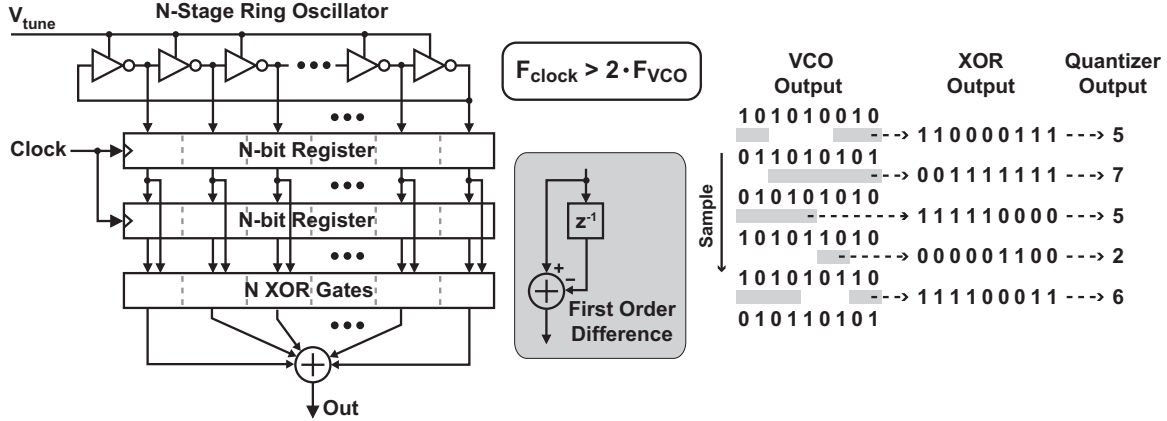


Figure 7-4 High-speed multi-phase VCO frequency measurement

delay characteristics of the counters and the need for adequate setup times on the sampling registers. This count corruption process will, in turn, destroy the desired noise shaping properties of the structure.

There are a variety of alternative VCO-based quantizer structures that could remove the reset issue just discussed; we will focus here on one suited for high sample rate operation which is shown in Figure 7-4 [39]. In this structure, the multi-bit counters and resettable registers shown in Figure 7-3 are avoided in favor of a simpler implementation that requires only a set of standard registers (with no reset), XOR gates, and a final adder stage. We see that an explicit reset operation is avoided, and the relative simplicity of this circuit allows high speed operation with small latency, which are important characteristics when placing the VCO-based quantizer within a CT  $\Sigma\Delta$  ADC structure.

To better understand the operation of the high-speed VCO-quantizer structure, we can examine the binary sequences shown in Figure 7-4. The key idea is to observe whether a given VCO delay cell undergoes a transition within a given clock period by comparing samples of its current and previous states with an XOR operation. The number of VCO delay cells that undergo a transition within a given clock period is a function of the delay through each stage as set by the  $V_{tune}$  voltage, and, in fact, corresponds to the quantized value of the  $V_{tune}$  voltage that we seek. An important observation from Figure 7-4 is that the XOR outputs barrel-shift through their values

with each progressing sample. This property will be exploited later in this chapter.

A key constraint for achieving proper operation of the VCO-based quantizer in Figure 7-4 is that the maximum number of VCO delay cell transitions that occur in one clock period cannot exceed the number of stages  $N$  in the ring oscillator. We express this restriction mathematically as

$$\frac{T_s}{\min \{T_{delay}(V)\}} < N, \quad (7.2)$$

where  $T_{delay}(V)$  is the propagation delay of each delay stage as a function of VCO tuning voltage, and  $T_s$  is the sampling period. Since the oscillator period,  $T_{vco}$ , corresponds to the time it takes a given edge to propagate through each delay stage twice, we also have

$$T_{vco}(V) = 2NT_{delay}(V). \quad (7.3)$$

By combining Equations 7.2 and 7.3, we can offer alternative views of the same restriction to be that

$$\min \{T_{vco}(V)\} > 2T_s, \quad (7.4)$$

$$\max \{F_{vco}(V)\} < F_s/2, \quad (7.5)$$

where  $F_{vco}(V)$  corresponds to the instantaneous frequency (in Hz) of the oscillator and  $F_s = 1/T_s$  corresponds to the frequency (in Hz) of the sampling clock. Equation 7.5 therefore states that the maximum oscillator frequency should be confined to be less than half of the quantizer clock frequency. If we assume that the nominal oscillator frequency,  $F_{vco}$ , is half of its maximum value (such that half of the elements transition for zero input), then we are left with requiring a sampling rate that is four times the nominal VCO frequency. Thus, we have another design constraint that

$$F_s \approx \frac{2}{N \cdot T_{delay}}, \quad (7.6)$$

where  $T_{delay}$  is the nominal delay for each oscillator stage.

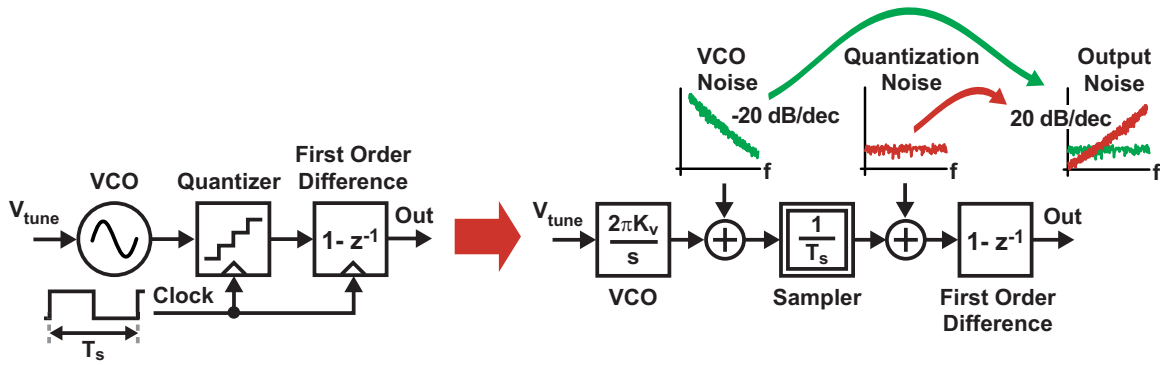


Figure 7-5 Block diagram model and corresponding linearized frequency domain model of the VCO-based quantizer

## 7.2 SNDR limitations for VCO-based quantization

In this section we examine the key limitations in achieving high SNDR for VCO-based quantizers. We begin with a linear model of the VCO-based quantizer to provide a basis for the rest of this chapter, and then examine the theoretical limits to SNR considering only quantization noise. A behavioral simulation example is then presented which indicates the approximate SNDR performance of such quantizers in  $0.13\mu\text{m}$  CMOS technology. The example will draw out the fact that non-linearity in VCO-based quantization is the primary bottleneck to achieving high SNDR values.

### 7.2.1 Linear modeling

Figure 7-5 depicts a functional block diagram of the VCO-based quantizer on the left, and its corresponding linearized frequency domain model on the right. Comparing the block diagram to the corresponding quantizer structure in Figure 7-4, the VCO block corresponds to the ring oscillator and the Quantizer block corresponds to the first set of registers which sample the quantized phase signal of the VCO. The First Order Difference block corresponds to comparison of the register values to their previous sample values by the XOR gates in Figure 7-4. In the corresponding frequency domain model, the VCO is represented as an integrator with gain  $2\pi K_v$ , which represents conversion of the  $V_{tune}$  voltage to a VCO phase signal, and the addition of phase noise. The Quantizer is modeled as a sampler that adds quantization noise, and the

First Order Difference block is seen as a  $1 - z^{-1}$  transfer function that performs a discrete-time differentiation.

A key observation offered by Figure 7-5 is that the quantization noise is first-order noise-shaped by virtue of the first order difference operation shown in the figure, which is in agreement with the time domain view of the quantization noise described in Equation 7.1. We also see that the VCO phase noise is shaped as well, but the result of such shaping is a flat spectrum due to the -20 dB/dec slope of the original phase noise signal. In reality, the shaped VCO phase noise will also include  $1/f$  noise, but this is ignored for now for the sake of modeling simplicity.

In effect, the First Order Difference block converts the VCO phase signal to a corresponding VCO frequency signal. To be precise, however, the discrete-time (DT) differentiation is not an exact inverse function of the continuous-time (CT) integration, noting first that sampling will alias the input signal, and that the  $1 - z^{-1}$  filter is only an approximation to the CT differentiation. As shown in Figure 7-6(a), the resulting DT spectrum of the VCO frequency measurement tightly follows the input spectrum for low frequencies with the expected low-frequency gain factor of  $2\pi K_v$ , but then begins to fall off slightly around  $F_s/2$  ( $\Omega = \pi$ ) due to the CT/DT inverse approximation.

An interesting observation to be made here is that the VCO-based quantizer has an inherent first-order anti-alias filter. This can be seen in the quantizer output on the right side of Figure 7-6(a) by comparing the reconstructed input signal (shown as a dark line) with the aliased copy (shown with a lighter shade). Although by itself this first-order anti-alias filter can be considered as fairly crude, the aliasing rejection approximately equal to  $20 \log(F_s/F_b)$  can be significant for some applications. Here,  $F_b$  refers to the analog input bandwidth.

For purposes of linear analysis it can be useful to choose a primary time domain in which to operate, and for historical reasons we choose here to use discrete time. Therefore, we next will develop a DT model for the VCO-quantizer that will be helpful later in this chapter. First, it is commonly known that the DT accumulation can be



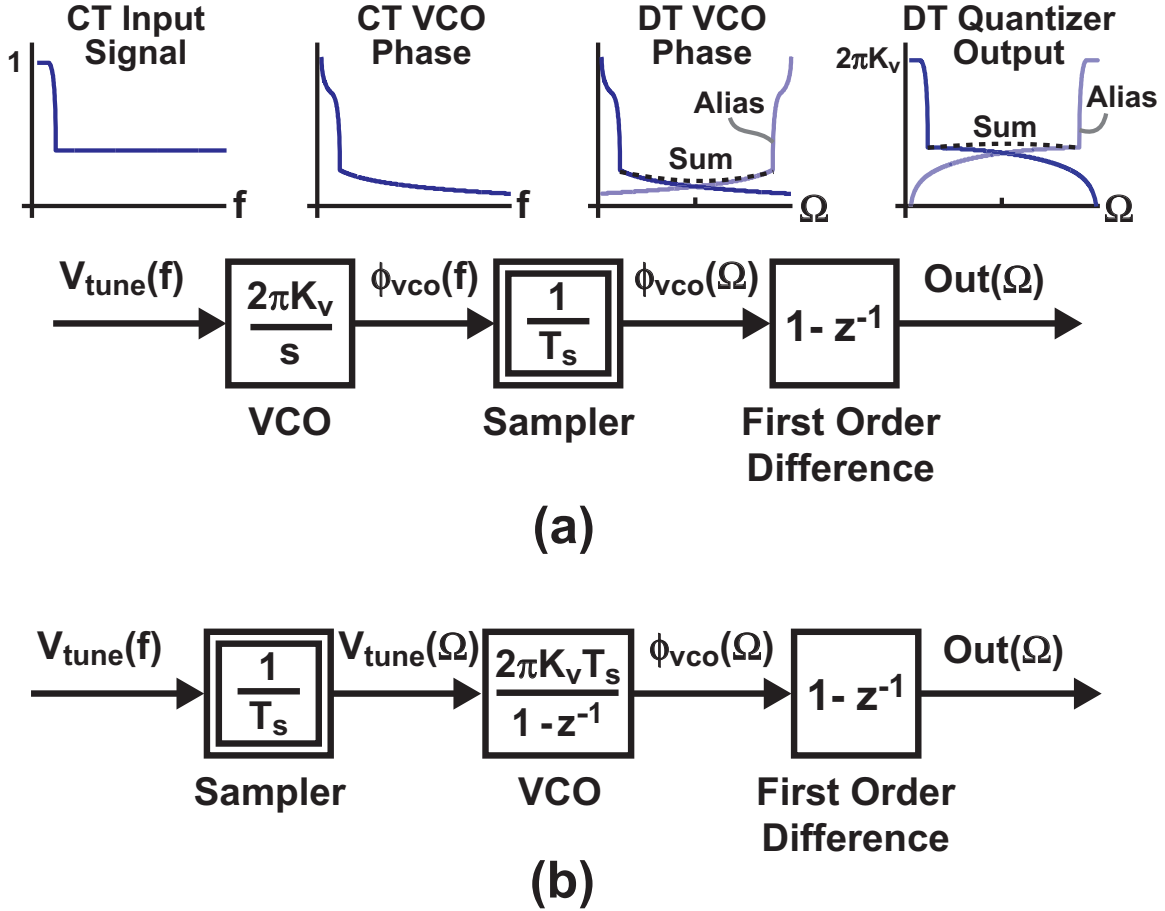


Figure 7-6 View of an example spectrum as it passes through the VCO-based quantizer. (a) shows the mixed-mode view with both CT and DT spectra, and (b) shows the DT linear model with the sampler moved to the front-end

approximated as a CT integration by using the Taylor series expansion of  $e^x$ :

$$\frac{1}{1 - z^{-1}} = \frac{1}{1 - e^{-s \cdot T_s}} \quad (7.7)$$

$$= \frac{1}{1 - \left(1 + \frac{(-s \cdot T_s)^1}{1!} + \frac{(-s \cdot T_s)^2}{2!} + \frac{(-s \cdot T_s)^3}{3!} + \dots\right)} \quad (7.8)$$

$$\approx \frac{1}{s T_s}; \quad |s| \ll F_s. \quad (7.9)$$

To create the DT model, we then replace the CT VCO gain of  $2\pi K_v/s$  with the DT VCO gain of  $2\pi K_v T_s/(1 - z^{-1})$ , and move the sampler gain of  $1/T_s$  before the VCO-quantizer as illustrated in Figure 7-6(b). Not surprisingly, for low frequency input signals we can now approximate the VCO-quantizer as a single block with gain

$A_{vco-q}(z)$  that translates an input voltage  $V_{tune}(z)$  to a frequency (in rad/sample) at the VCO output  $Out(z)$  by

$$A_{vco-q}(z) = \frac{Out(z)}{V_{tune}(z)} \approx 2\pi K_v T_s \quad [\text{rad/sample/V}]; \quad \omega \ll F_s. \quad (7.10)$$

## 7.2.2 Theoretical SNR

Now that a model for the VCO quantizer has been described, we can utilize the well-established analysis of oversampling quantizers in order to provide a theoretical bound to its SNR performance. The expression for peak signal-to-quantization noise ratio (SQNR) of a  $\Sigma\Delta$  converter is found in [17] to be

$$\text{SQNR}_{\text{peak}} = \frac{3\pi}{2} \cdot (2^\beta - 1)^2 \cdot (2n + 1) \cdot \left(\frac{\text{OSR}}{\pi}\right)^{2n+1} \quad (7.11)$$

where  $\beta$  is the number of bits,  $n$  is the  $\Sigma\Delta$  order, and the oversampling ratio  $\text{OSR} = F_s/(2F_b)$ . For the first-order VCO-based quantizer, with  $T_{delay}$  and  $F_s$  as the primary design variables related to  $N$  through Equation 7.6, we have

$$2^\beta - 1 = N = \frac{2}{F_s \cdot T_{delay}}. \quad (7.12)$$

Therefore, we can simplify Equation 7.11 to

$$\text{SQNR}_{\text{peak}} = \frac{9}{4\pi^2(F_b)^3} \frac{F_s}{(T_{delay})^2}. \quad (7.13)$$

One important thing to notice from Equation 7.13 is that  $\text{SQNR}_{\text{peak}}$  of the VCO-based quantizer improves independently with *both* faster sampling and faster delay elements. For a series connected ring oscillator, the nominal delay per stage is set to be approximately twice the minimum inverter delay in the process, and the sampling rate is set to be as large as practical. Thus, advancing the process to reduce the digital delay by a factor of 2 can improve  $\text{SQNR}_{\text{peak}}$  by 9dB for the same input bandwidth.

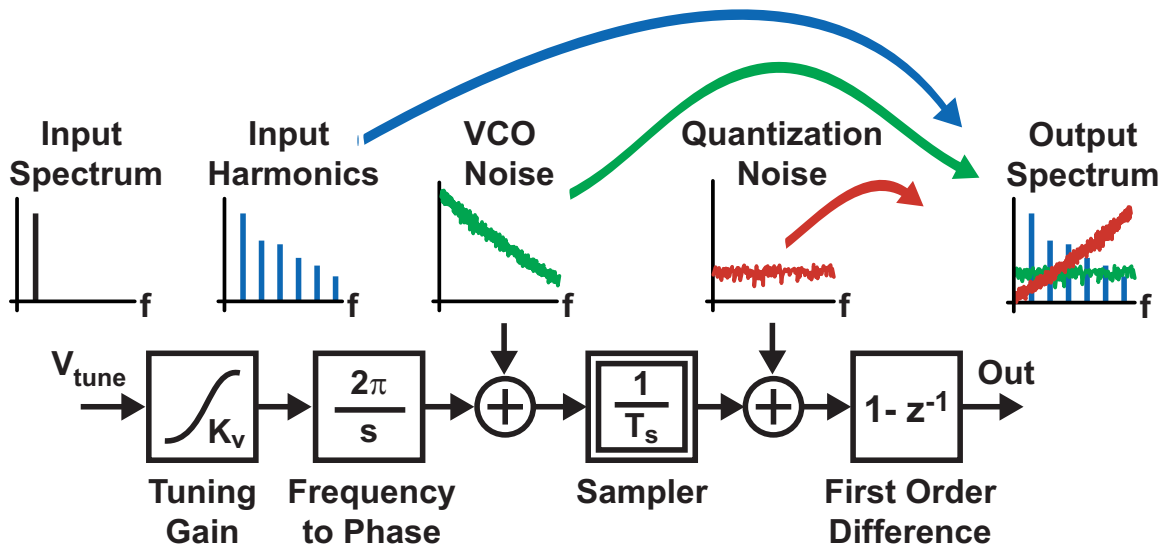


Figure 7-7 Behavioral model illustrating the VCO quantizer non-linearity

### 7.3 Example

The previous subsections highlighted quantization noise and, to a lesser extent, thermal noise as key non-idealities of the VCO-quantizer. However, one important issue that has so far been neglected is that the voltage-to-frequency tuning curve of a VCO is quite non-linear in practice. Figure 7-7 shows that the impact of such non-linearity is to introduce harmonic distortion which can significantly degrade the SNDR performance of the quantizer. Although the linear models so far provide an intuitive understanding of the VCO-quantizer, we will now see that the VCO non-linearity is actually a critical bottleneck to achieving good SNDR performance when this quantizer is used for analog-to-digital conversion.

To gain a better idea of the relative limitations posed by each of these nonidealities, we now present an example design of a VCO-based quantizer. Considering a  $0.13\mu\text{m}$  CMOS process technology, along with typical noise and non-linearity performance, we choose to make the following assumptions for the design example:

- Sampling clock:  $F_s = 1\text{GHz}$ ,
- Nominal delay per stage:  $T_{delay} = 65\text{psec}$ ,
- Nominal VCO gain:  $K_v = 750\text{MHz/V}$ ,

### Example VCO-quantizer Output Spectrum

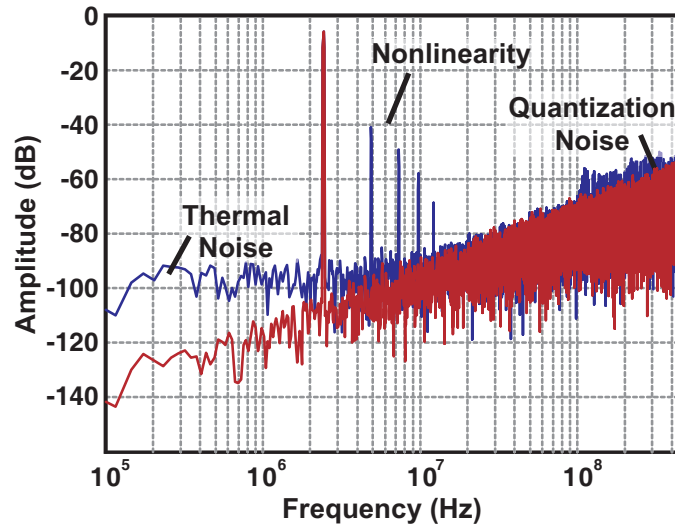


Figure 7-8 Behavioral simulation results of an example VCO-based quantizer

- Non-linearity of VCO tuning characteristic:  $\pm 10\%$ ,
- VCO Noise:  $-100\text{dBc}/\text{Hz}$  at  $1\text{MHz}$  offset.

From Equation 7.6, the above choice of sampling frequency and delay implies that  $N = 31$  and that  $F_{vco} = 250\text{MHz}$ . The  $K_v$  of  $750\text{MHz}/\text{V}$  then restricts the maximum input signal to be  $\pm 300\text{mV}$ .

Figure 7-8 displays the impact of the three key nonidealities on the quantizer output spectrum given a  $2.5\text{MHz}$  input signal near full-scale. The figure illustrates first order noise shaping of the quantization noise, filling in of the low frequency noise by the VCO phase noise, and harmonic distortion caused by the non-linear VCO tuning characteristic.

In this example, let us choose to lowpass filter the quantizer output with a bandwidth  $F_b$  set to  $20\text{MHz}$ , which coincides with the point at which the influence of quantization noise is comparable to that of the VCO phase noise. In such a situation, we obtain the following SNDR values:

- Quantization noise only:  $68\text{dB}^1$ ,

<sup>1</sup>Note that the behavioral simulation with only quantization noise agrees with the theoretical calculation from Equation 7.13 (page 138)

- Quantization noise and VCO phase noise: 65dB,
- Quantization noise, VCO phase noise, and non-linearity: 34dB ( $\text{SQNR}_{\text{peak}} = 50\text{dB}$ )

This example clearly reveals that VCO non-linearity forms the primary bottleneck to achieving high SNDR values for the VCO-based quantizer. It is this issue that leads us to the  $\Sigma\Delta$  ADC architecture presented in the next chapter.



# Chapter 8

## VCO-based quantizer $\Sigma\Delta$ ADC Architecture

One approach to improving a quantizer's linearity and quantization noise performance is to place the quantizer in a  $\Sigma\Delta$  feedback loop. It is natural to consider the VCO-based quantizer for a  $\Sigma\Delta$  ADC [28, 39], since its distortion and quantization errors will be suppressed by the preceding gain of the loop filter. A general block diagram for such an architecture is shown in Figure 8-1, which shows exaggerated waveforms to illustrate the loop limiting the effect of VCO non-linearity.

There are many differences between the VCO-based quantizer and a traditional comparator-based FLASH quantizer in the context of a  $\Sigma\Delta$  ADC. For example, we will see a unique attribute of the VCO-based quantizer architecture is that the overall quantization noise shaping is the sum of the first-order shaping from the VCO-based quantizer *plus* the order of the loop dynamics. Other differences between the quantizers are that a VCO-based quantizer inherently provides dynamic element matching (DEM), lower probability of metastable behavior, less sensitivity to offset and mismatch, and signal-dependent power consumption.

In the second part of this chapter, we define a model for the VCO-based quantizer  $\Sigma\Delta$  ADC *including* non-linearity error that allows for analysis of non-linearity suppression. This model will verify that the VCO-based quantizer  $\Sigma\Delta$  ADC does indeed have an extra order of quantization noise-shaping, and also will highlight the

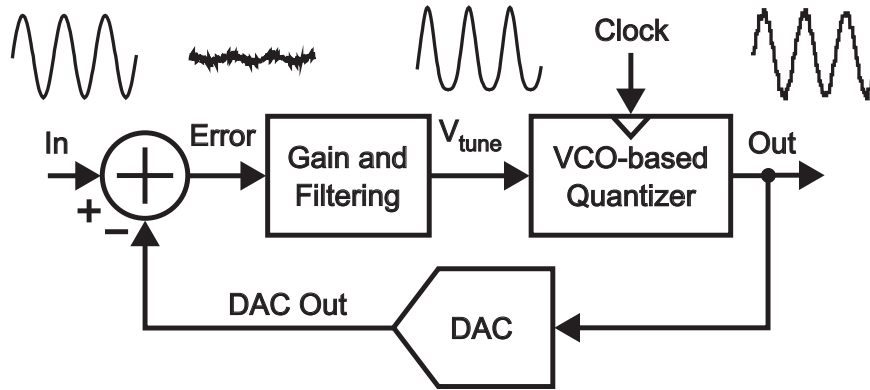


Figure 8-1  $\Sigma\Delta$  feedback to suppress VCO linearity and quantization errors

fact that many traditional techniques for reducing quantization noise also apply to suppressing VCO-based quantizer non-linearity. Last, we confirm the model with behavioral simulation of two idealized converters.

## 8.1 Comparison of VCO-based quantizer and comparator-based FLASH quantizer for $\Sigma\Delta$ ADC

Compared with a stand-alone quantizer, the specific application of a high-bandwidth CT  $\Sigma\Delta$  converter stresses a unique set of quantizer performance requirements. Therefore, in this section, we examine a few of the key differences between the VCO-based quantizer and the classical comparator-based FLASH quantizer in the context of a high-speed CT  $\Sigma\Delta$  ADC.

### 8.1.1 Implicit Barrel-Shift DEM using the VCO-based quantizer

A main attraction to high-speed CT  $\Sigma\Delta$  ADC is the ability to leverage very high-speed sampling in order to maximize input bandwidth and dynamic range. However, for high-speed, multi-bit  $\Sigma\Delta$  ADC (>500Msps and >2-bit), a very significant design challenge is to implement a DEM algorithm for the feedback DAC elements within strict timing requirements and with minimal power consumption. Although many dy-



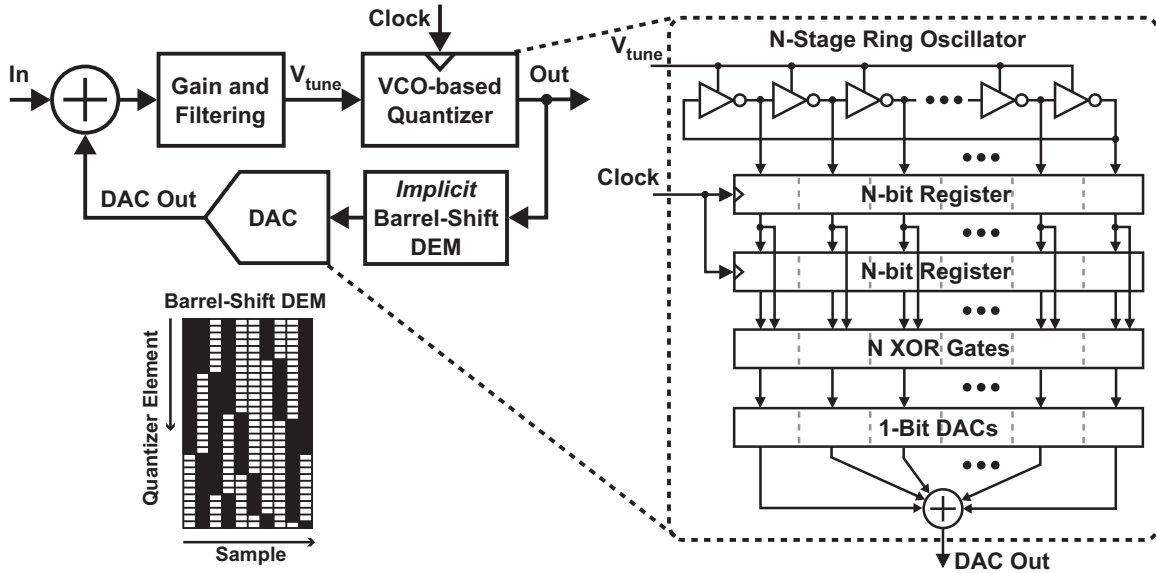


Figure 8-2 Utilizing VCO for implicit barrel shift DEM of DAC elements

dynamic element matching (DEM) techniques are well known, many approaches become overly complex for many levels or are not suitable for clocking at very high-speed. Fortunately, the multi-bit VCO-based quantizer can implement a barrel-shift DEM algorithm *without any penalty in terms of latency or power*, which is a significant advantage of the architecture.

Figure 8-2 illustrates how by connecting the outputs of the VCO-based quantizer to the DAC elements in a bit-wise fashion, the phase rotation of the VCO inherently implements the barrel-shift DEM algorithm [39]. Instead of digitally summing the XOR outputs prior to the feedback DAC, an analog summation is accomplished with current after the DAC. The first element to be used in a sample period is the last one left over from the previous sample, which ensures that each element is used with equal likelihood. To generate the output word, digital adders are still required, but these may be pipelined as the delay has been removed from the critical path.

We should note that some very demanding applications have avoided use of the barrel-shift algorithm due to the potential for tones created by limit-cycles in the signal band. This issue is a valid concern, as will be seen in Chapter 10, although the level of degradation can be considered to be negligible for the vast majority of applications. Compared to the comparator-based quantizer, which has no inherent DEM

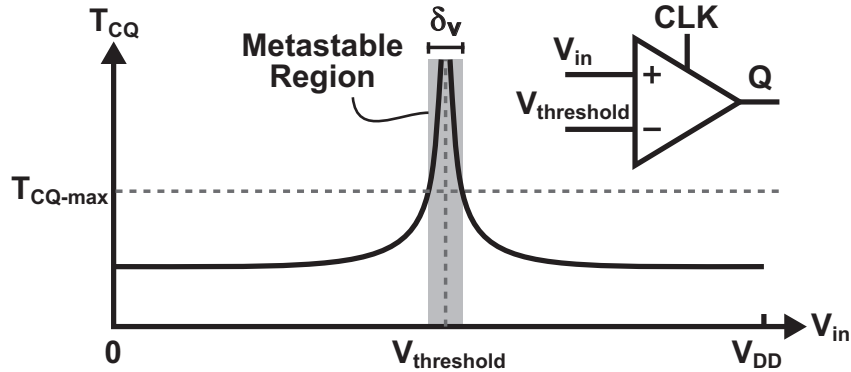


Figure 8-3 Dependence of comparator clock-to-Q time on input voltage

properties, the barrel-shifting DEM of the VCO-based quantizer is very attractive.

### 8.1.2 Metastability

Another critical aspect to a high-speed  $\Sigma\Delta$  ADC design is that the quantizer bit decisions must be made quickly and decisively. It is then worthwhile to consider a useful advantage of the VCO-based quantizer over classical comparator-based, multi-level quantizers with respect to metastability behavior. Let us first consider metastability for the general case of a single comparator and then apply this result to both quantizer topologies.

As shown in Figure 8-3, the comparator regeneration time,  $T_{CQ}$ , between the sampling clock edge and a valid output, is a strong function of how close the input voltage  $V_{in}$  is to the comparator threshold voltage,  $V_{threshold}$ . Without noise, the regeneration time is infinite for an input voltage *exactly* equal to  $V_{threshold}$ . If we can allot a maximum regeneration time  $T_{CQ-max}$  for the comparator decision to be made, then there is a small voltage  $\delta_v/2$  for which

$$T_{CQ}(V_{threshold} \pm \delta_v/2) \approx T_{CQ-max}. \quad (8.1)$$

For simplicity, we can say that the input voltage to the comparator is a random variable with uniform density on the interval  $[0, V_{DD}]$ , which gives us the probability

of metastability in a single comparator to be

$$P_{comp} [metastability] = P_{comp} [V_{in} | T_{CQ} (V_{in}) > T_{CQ-max}] \approx \frac{\delta_v}{V_{DD}}. \quad (8.2)$$

In an ideal FLASH ADC, the input voltage interval  $[0, V_{DD}]$  is uniformly divided into  $N$  subintervals, each with a unique threshold voltage centered on the subinterval. Let us assume that for a single input only one comparator has an input signal close to its threshold, which gives the probability of metastability for the FLASH ADC of

$$P_{flash} [metastability] = P_{flash} [V_{in} | T_{CQ} (V_{in}) > T_{CQ-max}] \approx \frac{N\delta_v}{V_{DD}}. \quad (8.3)$$

As can be seen in Equation 8.3, the probability of a metastable event increases linearly with the number of quantization levels in the flash ADC for the same comparator. To compensate, regenerative amplifiers (or pipelined latches) must be put in front of the comparators in order to effectively reduce  $\delta_v$ . Unfortunately, such improvements inevitably coming at the price of increased power consumption and area.

In the case of the VCO-based quantizer, we first note that the input voltages to the comparators are primarily binary voltage signals saturated to either 0 or  $V_{DD}$ . When the VCO is a ring oscillator comprising of a serial chain of inverters, only one of the outputs is transitioning between these binary levels at a time. As such, when we consider the input voltage distribution of the comparators only one of them will see a uniform distribution at a time. Therefore, the overall probability of metastability for the VCO-based quantizer is the same as the single comparator, or explicitly

$$P_{vco} [metastability] = P_{comp} [T_{CQ} > T_{CQ-max}] \approx \frac{\delta_v}{V_{DD}}. \quad (8.4)$$

To compare, the probability of a metastable event for an arbiter used in the VCO-based quantizer is approximately a factor of  $N$  smaller than when used in a FLASH architecture, and it is also independent of the number of quantization levels. This result simplifies the VCO-based quantizer comparator design and allows for very

high-speed operation with minimal power consumption.

### 8.1.3 Comparator Offset and Monotonicity

Since most high-speed comparators designs utilize minimum-size devices, offset in deep sub-micron comparators can be 50mV or more. For a multi-bit FLASH ADC, this level of comparator offset can be on the order of a quantization step size, which introduces significant non-linearity and threatens quantizer monotonicity. Although this would be a concern for any converter, in  $\Sigma\Delta$  ADC these issues can cause the loop to severely limit-cycle or even become unstable. Consequently, some form of offset calibration is needed in the implementation of a traditional multi-bit FLASH quantizer.

When we consider how comparator offset affects the VCO-based quantizer, we first recognize that the level of comparator offset is much smaller than a quantization step size. Using an argument similar to that discussed above for metastability, the quantization step size is effectively equal to  $V_{DD}$ , which can be argued will *always* be much smaller than a comparator offset. Second, we also recognize that the quantization error due to comparator offset will be first-order shaped. To explain, recall that in the same barrel-shifting manner discussed earlier for the DAC DEM circuit, the use of comparators and their associated offsets are rotated as the VCO rising/falling edge propagates around the ring.

Given these results, it is not surprising that the VCO-based quantizer is also guaranteed to be statistically monotonic, and in fact, it is relatively easy to prove this additional property. Equation 7.10 ( $A_{vco-q} \approx 2\pi K_v T_s$ ) states that the VCO acts as a simple gain element at DC, and thus mapping an input voltage to output frequency is one-to-one and monotonic. Due to the ideal integration and differentiation in the VCO-based quantizer at DC, the measurement or quantization error in determining the DC output frequency limits to zero. We can then conclude that, even in the presence of large comparator offsets, the DC transfer function from analog input voltage to digital output is monotonic.

### 8.1.4 Power Supply Considerations

One final issue to consider in the design of high resolution ADC is the correlation between the input signal and power consumption, either through digital switching or analog biasing. If such power supply variation or noise non-linearly couples into the signal path, distortion in the actual conversion can result. For the multi-bit FLASH quantizer, each of the comparators switches for each sample, and so to first-order the quantizer power consumption does not depend on the input signal. For the VCO-based quantizer, the switching activity within the VCO core is directly proportional to the input signal, and as such the power supply current is a relatively strong function of the input signal. As such, care must be taken to properly isolate the VCO power supply from other analog blocks in the signal path.

## 8.2 Modeling the suppression of VCO-based quantizer non-linearity

While we hypothesized earlier that feedback with high gain will improve the VCO non-linearity, a more quantitative examination of the non-linearity suppression can be useful in highlighting the fundamental tradeoffs and limitations of the technique. Figure 8-4 shows a simplified DT and CT model for a basic  $\Sigma\Delta$  VCO-based ADC that includes error terms from both a quantization error,  $E_q$ , and also a VCO non-linearity error,  $E_{nl}$ . Although each domain has advantages for different stages of the ADC design, as mentioned earlier we will use DT from this point forward, without loss of generality. In this model the units of  $E_q$  are [rad], and the units of  $E_{nl}$  are [rad/sample], which normalizes the non-linearity error to the reference frequency.

As the quantization noise-transfer function  $H_q$  describes how the quantization error  $E_q$  is shaped in the digital output of the ADC, we can also consider a non-linearity transfer function  $H_{nl}$  that will suppress the non-linearity error  $E_{nl}$  from the VCO-based quantizer. For this analysis we make a small-signal linear approximation that allows us to define an input signal  $E_{nl}(z)$  that is decoupled from  $U(z)$ , allowing

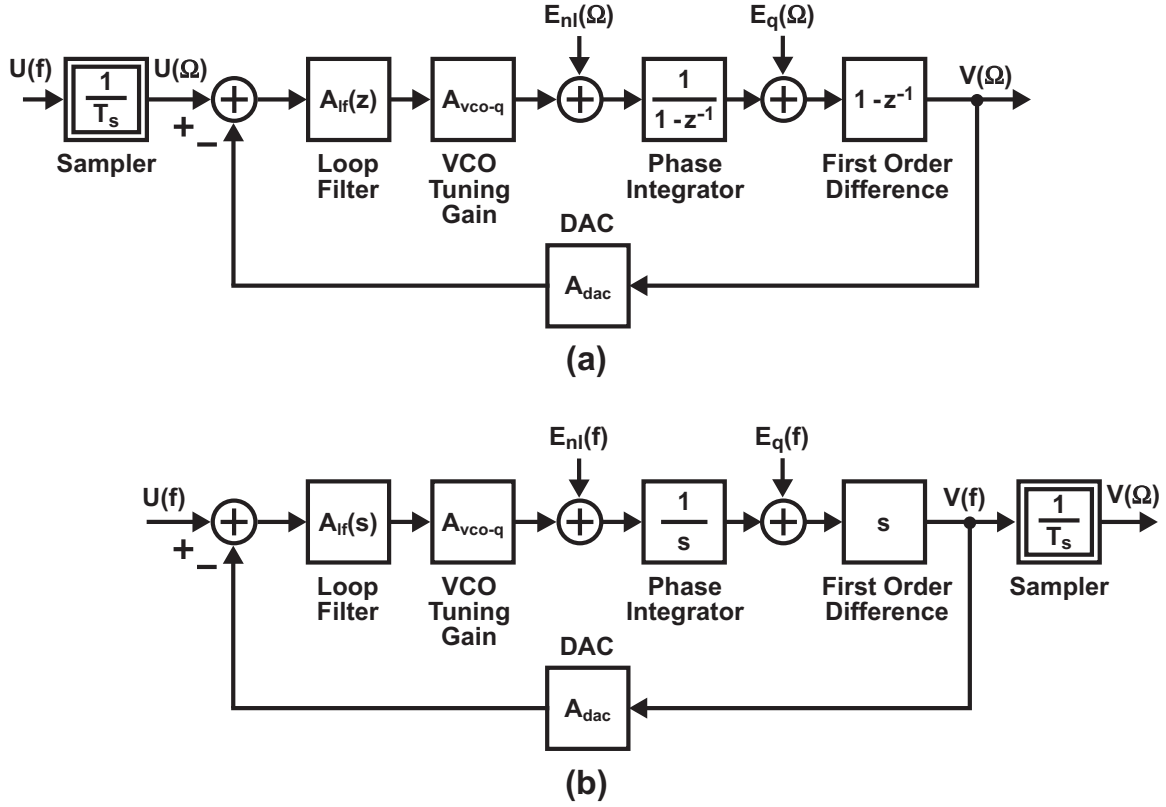


Figure 8-4 A model in discrete-time (a) and continuous-time (b) for the VCO-based quantizer  $\Sigma\Delta$  ADC with non-linearity error  $E_{nl}$  and quantization error  $E_q$

us to estimate how well the loop is able to reject  $E_{nl}(z)$  as a function of frequency.

With these definitions, we can generally describe the modulator output  $V(z)$  as

$$V(z) = G(z)U(z) + H_q(z)E_q(z) + H_{nl}(z)E_{nl}(z). \quad (8.5)$$

From Figure 8-4 we find that

$$G(z) = A_{vco-q}A_{lf}(z)H(z), \quad (8.6)$$

$$H_{nl}(z) = H(z), \quad (8.7)$$

$$H_q(z) = (1 - z^{-1})H(z), \quad (8.8)$$

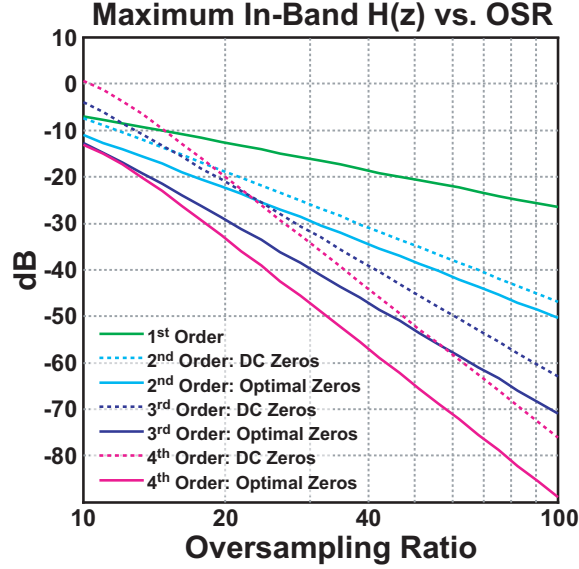


Figure 8-5 Maximum in-band  $|H(z)|$  for a lowpass modulator across oversampling ratio and loop order. The zeros are placed either at DC (dashed line) or at locations optimal for the oversampling ratio (solid line).

where  $H(z)$  is given by

$$H(z) = \frac{1}{1 + A_{vco-q}A_{dac}A_{lf}(z)}. \quad (8.9)$$

Equation 8.7 confirms that the non-linearity error  $E_{nl}$  will observe a high-pass transfer function as set by the overall loop order and dynamics, with suppression approximately equal to the open-loop gain of  $A_{vco-q}A_{dac}A_{lf}(z)$ . Also, we can also see from Equation 8.8 that the quantization noise suppression is one order *higher* than the order of the loop filter due to the  $1 - z^{-1}$  term in  $E_q$ . Lastly, in terms of minimizing both quantization noise and VCO distortion, we clearly desire a large  $A_{lf}(z)$  to minimize  $|H(z)|$  in the signal band of interest, noting that  $A_{lf}(z)$  is a strong function of frequency.

The standard techniques to minimize  $|H(z)|$  given a low-pass signal bandwidth are to increase the loop order and to optimize the placement of  $H(z)$  zeros. Figure 8-5 plots the *maximum* value of  $|H(z)|$  for varied oversampling ratio, loop order, and zero optimality [62], which directly corresponds to the *minimum* amount of VCO non-linearity suppression. A loop order of up to four is readily achievable as a standard

practice today, and in this case a large oversampling ratio (OSR) provides tremendous suppression of VCO nonlinearity error. However, as the OSR decreases to less than 20, for stability reasons the various loop orders begin to cluster together. In fact, if the  $OSR < 16$ , the higher order loops lose so much advantage that a first-order loop is actually preferable to a fourth-order loop without optimal zero-placement. Therefore, applications with larger OSR will especially benefit from the advantages of the VCO-based quantizer.

We can now make a few general observations regarding the suppression of VCO non-linearity from  $\Sigma\Delta$  feedback. In one sense, the  $\Sigma\Delta$  modulator has improved the VCO-based quantizer nonlinearity by approximately the gain of the loop, which is a significant and marked advance compared to the stand-alone architecture. However, we can also see that the linearity performance of the VCO has not been improved *in relation* to the quantization noise. Observe that both the quantization noise  $E_q(z)$  and the distortion  $E_{nl}(z)$  have been modified by the same factor of  $H(z)$  compared to the quantizer without feedback. Therefore, as was the case in the VCO-based quantizer example from Section II, we may expect that the VCO non-linearity may still present a limitation for frequencies very close to the maximum edge of the input bandwidth.

### 8.3 Example

To verify the above analysis, we can again simulate an example VCO-based quantizer  $\Sigma\Delta$  ADC at the behavioral level using CppSim [50], a very-fast code-driven C++ simulator that is especially targeted at high-performance mixed-signal systems. A tutorial that includes the example simulation is also free and available online.

Before simulating the converter from Figure 8-4, we first need to consider that, even in the ideal sense, the VCO-based quantizer has a delay that has so far not been modeled. This excess loop delay causes phase lag in the signal transfer function, and must be accounted for in order to ensure loop stability. For our purposes here, the delay for the VCO-based quantizer is approximated by a single sample period. As we



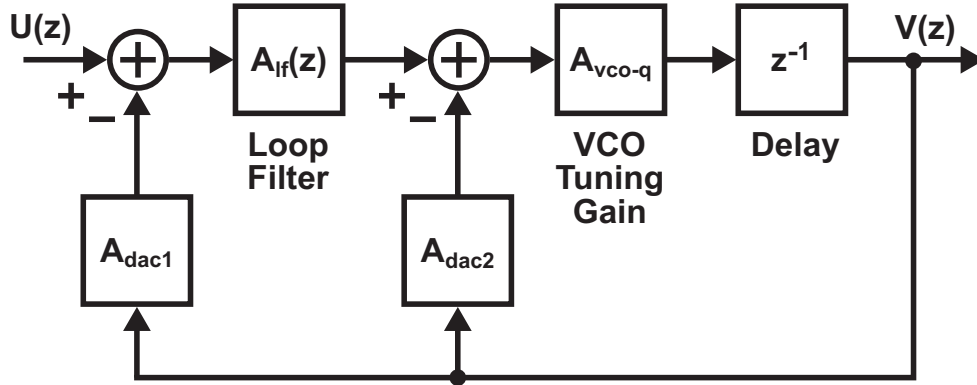


Figure 8-6 Model for the prototype ADC including excess loop delay and a minor compensation loop

will see in Chapter 9, this estimate of a single sample period agrees fairly well with a more precise delay value calculated for a practical system, and allows for relatively simple calculation of loop filter parameters.

A modified block diagram that includes this excess loop delay as a  $z^{-1}$  delay element is pictured in Figure 8-6. Also included in the system is a minor feedback loop that compensates for the impact of excess loop delay incurred by the latency of the VCO-based quantizer [80]. To explain in more detail, we calculate that the prototype noise transfer function  $H(z)$  from Equation 8.9 is modified to now be

$$H(z) = \frac{1}{1 + A_{vco-q} [A_{dac1} A_{lf}(z) + A_{dac2}] z^{-1}}. \quad (8.10)$$

Although the feedback from  $A_{dac1}$  is now delayed by both the loop filter and the excess loop delay, the overall effect on the loop dynamics is mitigated by proper design of  $A_{dac2}$  and  $A_{lf}(z)$ . A design procedure has been outlined in [80] (and scripted in the tutorial) that allows the designer to map from the desired NTF to the design of  $A_{lf}$ .

In this example, we examine the SNDR performance of the same ADC with two different loop filters, and the same assumptions regarding the VCO-based quantizer have been made in this example as in the previous case without feedback. The first case is a  $2^{nd}$  order loop filter *without* zero optimization, and the second is a  $4^{th}$  order loop filter *with* optimized zero placement for  $F_b = 20\text{MHz}$ . Figure 8-7 displays the original VCO-based quantizer spectrum from the earlier example in the background,

### Example $\Sigma\Delta$ ADC Output Spectrum

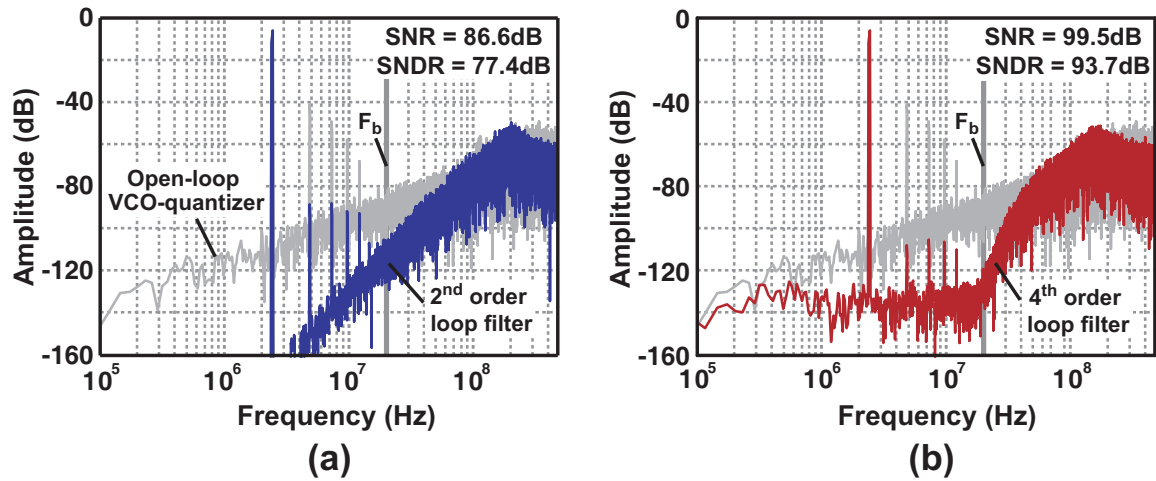


Figure 8-7 Behavioral simulation results of an example VCO-based quantizer  $\Sigma\Delta$  ADC with (a) 2<sup>nd</sup> order loop filter with NTF zeros at DC and (b) 4<sup>th</sup> order loop filter with optimized zeros for  $F_b = 20\text{MHz}$

and overlays the spectrum of the  $\Sigma\Delta$  ADC in the foreground. The first case with a 2<sup>nd</sup> order loop filter is shown on the left side in Figure 8-7 (a), and one can clearly see that the suppression of both the quantization noise and non-linearity decreases with frequency, as expected. On the right side in Figure 8-7 (b) is the second case with a 4<sup>th</sup> order loop filter with optimized zeros. Here, the level of error suppression is significantly increased, and the suppression is generally flatter across the band of interest. Note that the “white” noise in Figure 8-7 (b) is not quantization error, but rather it is believed to be an error from quantization effects.

By comparing the simulation results of the two loop filters, we can justify the assumptions made previously in developing the model for non-linearity suppression. In fact, both the levels of suppression as well as the overall frequency dependence agree with what would be expected from the model. In practice, however, there are many other potential sources of non-linearity in these very high-speed  $\Sigma\Delta$  ADC (e.g. DAC mismatch, front-end amplifier distortion), and these other errors must be balanced not only against the VCO-based quantizer non-linearity, but also against thermal and  $1/f$  noise.

## 8.4 Conclusion

This chapter has compared the use of the VCO-based quantizer to the traditional FLASH based architecture, and found that the VCO-based quantizer offers a few unique advantages such as the ability to provide inherent dynamic element matching, as well as reduced sensitivity to metastability and comparator offset. The primary issue with the VCO-based quantizer, the linearity of its voltage-to-frequency tuning characteristic, has been modeled within a  $\Sigma\Delta$  ADC and we have seen that for large open-loop gains, the linearity performance can be improved significantly. Finally, the model was substantiated with simulation examples, illustrating that while the VCO non-linearity has indeed been suppressed by the gain of the preceding loop filter, it may yet pose a limitation for overall converter distortion performance.



# Chapter 9

## Prototype $\Sigma\Delta$ ADC with a VCO-quantizer

In this section we demonstrate a prototype  $\Sigma\Delta$  ADC that is able to significantly suppress VCO-quantizer non-linearity, achieve third-order noise shaping with a single op-amp, and provide inherent dynamic element matching for the feedback DAC. We will discuss the prototype architecture, detail the design of primary circuit blocks, and then show measurement results.

### 9.1 $\Sigma\Delta$ ADC Architecture

Figure 9-1 displays our proposed ADC structure. This circuit topology incorporates an active loop filter, two 31-element current DACs, and a 31-level VCO-based quantizer to achieve *third* order noise shaping. One should immediately notice the simplicity offered by this structure — the active analog components consist of just one opamp, two current DACs, and a ring oscillator (within the VCO-based quantizer). Indeed, the simplicity allows high-speed sampling at 950Mz to be achieved with compact area and low power dissipation. Note that while a single-ended schematic is shown for clarity, the ADC is fully differential with the exception of a pseudo-differential VCO-quantizer, as will soon be discussed in more detail.

While the topology shown in Figure 9-1 bears resemblance to the popular second-

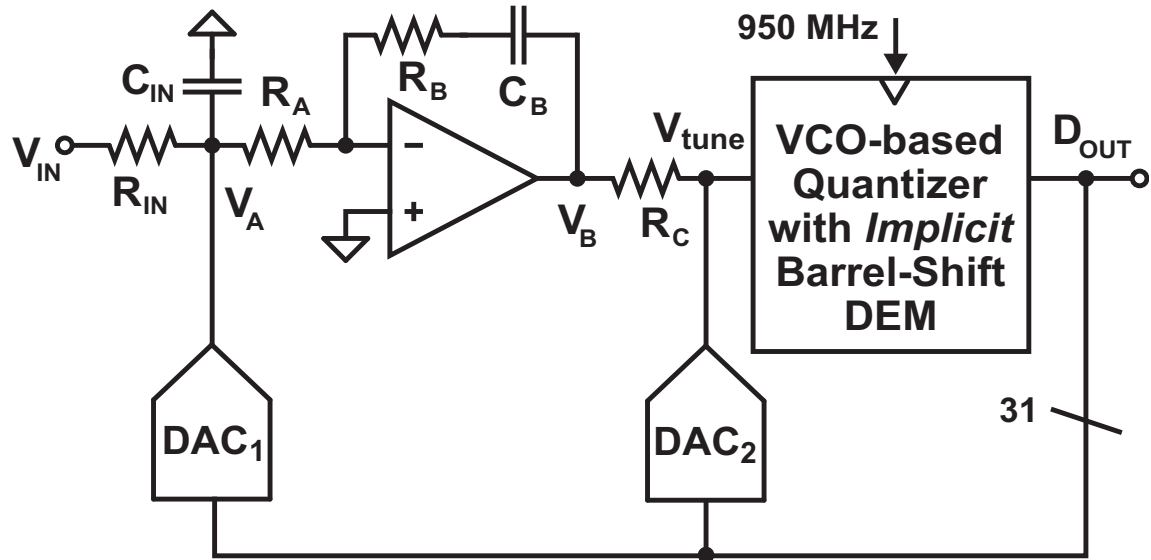


Figure 9-1 Block diagram of the proposed ADC

order Candy structure [47], its design is actually quite different with respect to the means by which it achieves stability. In particular, the minor loop feedback, which is created by feeding the output current of  $DAC_2$  into the  $V_{tune}$  node, is not formed around an integrator as would be done in the Candy structure. Rather, the two integrators occur before the minor loop, and consist of an active integrator (formed by the opamp and elements  $R_A$  and  $C_B$ ) and a lossy integrator (formed passively by elements  $R_{IN}$ ,  $C_{IN}$ , and  $R_A$ ). Stability of the structure therefore requires the inclusion of an open-loop zero in the signal transfer function, which is formed by elements  $R_B$  and  $C_B$ .

With the ADC having a target signal bandwidth of 10-20MHz, the actual closed loop bandwidth of the ADC was then designed to be around 160MHz. To achieve adequate phase margin, the stabilizing zero formed by  $R_B$  and  $C_B$  was set to be in the range of 75-110MHz (as influenced by the setting of  $C_B$ , as explained in the Loop Filter subsection). The passive filter, which forms a lossy integrator as mentioned above, was set to be slightly less than 10MHz in order to attenuate the large current pulses from the  $DAC_1$  output. While the inclusion of the front-end passive filter leads to a slight penalty in noise, it has the advantage of providing a very linear front-end for the ADC and simplifying design of the opamp (which would otherwise have to

deal more directly with the current pulses of  $DAC_1$ ).

As opposed to optimizing the zeros of the ADC noise transfer function for a signal bandwidth of 10-20MHz, we chose to implement a simple ADC topology that highlights the properties of the VCO-based quantizer. Additionally, the chosen topology allows for second-order dynamics and third-order noise shaping with only a single opamp. To explain, the proposed topology achieves third-order noise shaping through the inclusion of three zeros within its quantization noise transfer function,  $E_q$ , as explained earlier. Two of those zeros, as provided by the VCO-quantizer and the active integrator, are located at or very near the origin. The third zero, as provided by the lossy integrator formed by the front-end passive filter, is located slightly below 10MHz as set by the bandwidth of that filter.

While the choice of 10-20MHz signal bandwidth did not explicitly influence the zero placement, it was strongly considered in choosing appropriate thermal noise levels for the opamp,  $DAC_1$ , and the front-end passive filter. These blocks were therefore designed such that the overall thermal noise had a comparable spectral density to the quantization noise at the edge of the signal bandwidth range (i.e., 20MHz).

Given the above overview of the proposed structure, we now examine its various blocks in detail in the subsections to follow. In particular, we will present additional circuit details of the VCO-based quantizer, the current DACs, and the loop filter.

## 9.2 Circuit Implementation

### 9.2.1 VCO-based quantizer

Figure 9-2 illustrates a geometric view of the combined VCO-based quantizer, implicit DEM, and DAC circuitry implemented with 31 levels. In essence, this structure corresponds to the VCO-based quantizer shown in Figure 7-4 which has been augmented with DAC elements. A bit-slice of this structure, which is also shown in the figure, reveals a variable delay consisting of a 4-transistor stack followed by a buffer, some digital logic to implement the first order difference operation, and a DAC element

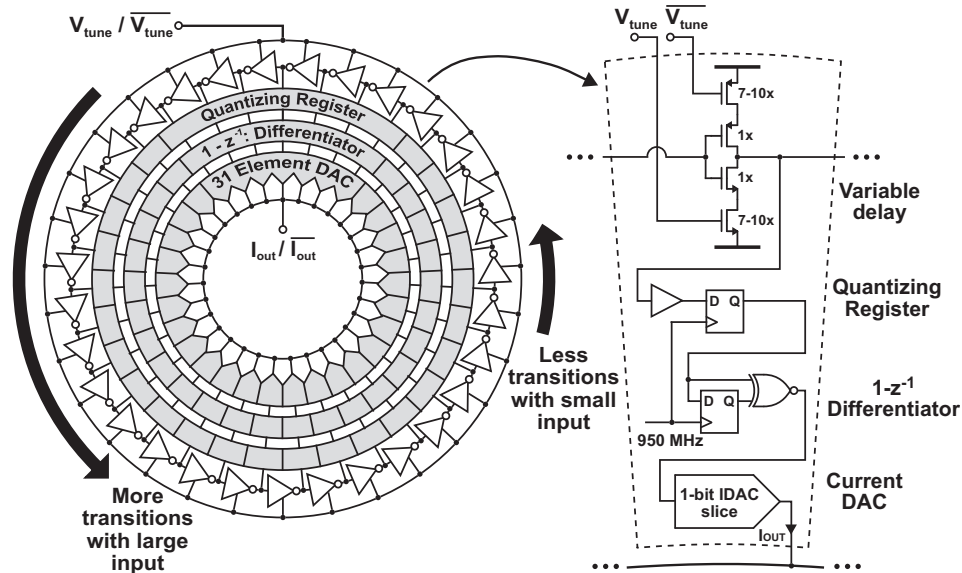


Figure 9-2 Geometric view of the proposed 31-level combined VCO quantizer/DEM and DAC

with current output. The buffer is used to isolate the variable delay output from the sampling register, which is implemented with standard cell regenerative latches. Simulations demonstrated that metastability is not a concern, as predicted from the discussion in Section 8.1.2. In terms of delay timing, a half-period is available before generating the DAC pulses, which allows use of standard cell XOR gates and TSPC DFF for the subsequent first-order difference logic.

There are several advantages of implementing the variable delay element as a complementary 4-transistor stack. First, the pseudo-differential control of the delay value provides a seamless interface with the output of a fully differential loop filter circuit so that common-mode noise in that path is rejected. Second, the topology provides reasonably good linearity in the voltage-to-frequency tuning characteristic of the VCO with a compact and low-power implementation, and allows a very large frequency tuning range for the VCO needed to achieve a high range of quantization levels. Third, full-swing CMOS logic levels in the delay element are directly compatible with the standard cell regenerative latches used for the phase register. Last, the structure supports a high clock rate by achieving a small minimum delay of 35-40ps in the  $0.13\mu\text{m}$  CMOS process, which is comparable to a loaded inverted delay in that



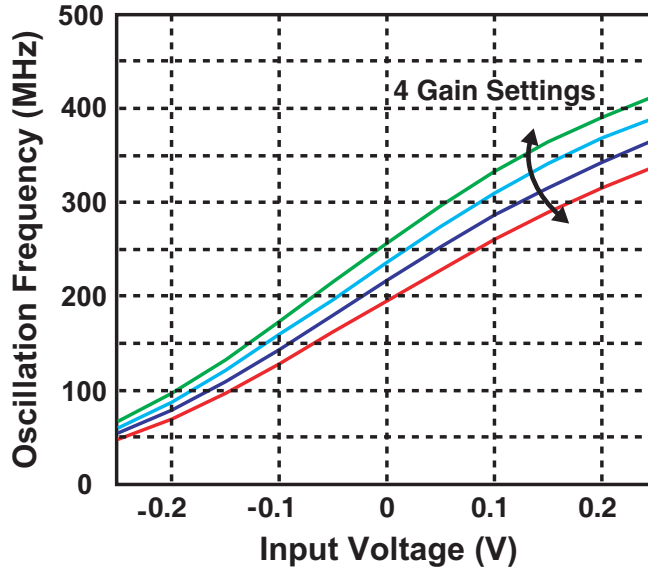


Figure 9-3 Tuning characteristic for the proposed VCO-quantizer

process. In the prototype, the choice of  $N = 31$  elements and  $F_{clk} = 950$  MHz requires a *nominal* delay of 70ps, and, therefore, a *minimum* delay of around 35ps.

In designing the variable delay cell for the VCO-based ADC, care must be taken to avoid a large gain variation in the tuning characteristic of the VCO. Such gain variation would directly alter the open loop gain of the overall ADC, which could impact its performance and cause stability problems. Fortunately, with an input common-mode set to mid-supply, the chosen delay cell has relatively smooth odd-order non-linearity at both the bottom and top of the tuning curve, which can be seen clearly in Figure 9-3. Of course, the quantizer does impose a limited range for its operation, as seen by the fact that at -300mV differential input voltage, the oscillator has slowed to a level near zero frequency, and above 300mV the oscillator starts to reach limits in the high end of its frequency range. For the implemented structure, a useful operating range for the VCO-quantizer is up to -2dBFS for 5-bit operation at 950MS/s.

To account for process variation in the center frequency of the oscillator, four gain settings control the level of current drive in the delay cell. As shown in Figure 9-3, the 2 bits of tuning can account for approximately  $\pm 20\%$  of center frequency variation, and are hand-adjusted in this prototype. This constitutes a relatively

coarse adjustment of the frequency offset of the VCO tuning characteristic, which is acceptable since any remaining offset simply translates into a differential offset voltage at the input of the VCO tuning port. Of course, in the case of a severe offset, linearity performance will suffer and, ultimately, the open loop gain of the ADC will significantly drop if frequency saturation occurs in the VCO. Note that the impact of power supply and thermal variations on the oscillator center frequency are mitigated by the feedback having large gain at low frequency, as will be seen in Chapter 10.

Finally, since excess delay introduced by the quantizer degrades the phase margin of the ADC structure, it is worthwhile to estimate its value in the proposed VCO-based quantizer structure. To do so, note that  $V_{tune}$  is integrated over the previous sampling period which can be seen as a  $1/2$  clock delay, and the  $DAC_1$  pulse logic begins  $1/2$  period after the quantizer positive sampling edge. Additionally, there is an estimate of  $1/4$  clock delay for generating the RZ DAC pulses. The combination of these effects leads to an excess loop delay of approximately 1.25 clock periods.

### 9.2.2 DAC

An RZ topology was chosen for the primary DAC in the prototype ADC (i.e.,  $DAC_1$  in Figure 9-1) in order to minimize the impact of inter-symbol interference at the high sample frequency of 950MHz and to provide additional compensation of excess loop delay introduced by the VCO-based quantizer. The penalties for choosing an RZ topology are larger current variation at the output summing node, increased sensitivity to clock jitter, and increased power [80]. As mentioned earlier, the issue of current variation was addressed through the use of passive filtering in the prototype. The issue of clock jitter, which strongly impacts the SNR of any high-speed continuous-time  $\Sigma\Delta$  ADC structure, was addressed by using a low noise, off-chip clocking source. The issue of power consumption was partially mitigated through circuit design efforts, the details of which are described below.

The schematic for the primary RZ DAC element core is shown in part (a) of Figure 9-4, and the overall DAC structure comprises of 31 unit elements, each connected bit-wise to the VCO-quantizer outputs. Degenerated transistors with moderate chan-

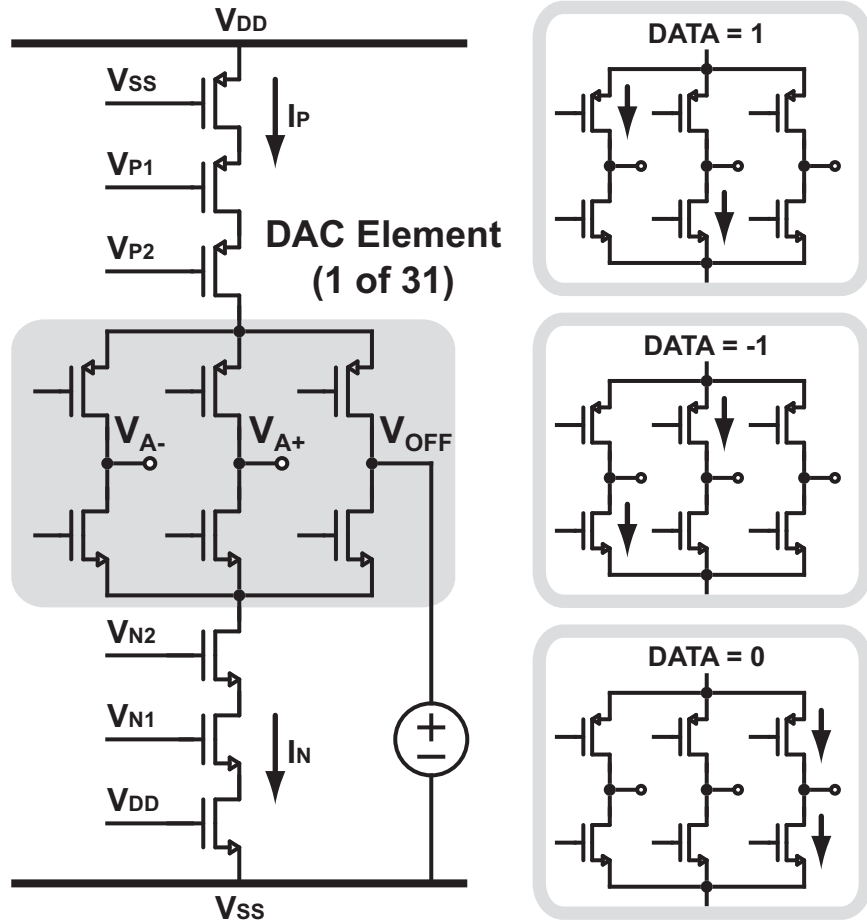


Figure 9-4 Schematic and operation of (a)  $DAC_1$  and (b)  $DAC_2$

nel lengths (and accompanying cascode devices) are used on both the top and bottom current sources to minimize thermal and  $1/f$  noise. The output common mode range of the DAC is set via the low impedance of the input signals, which have a common mode voltage of half-supply ( $V_{DD}/2$ ). Large, off-chip capacitors are used for both the NMOS and PMOS bias voltages to reduce the noise coupling from the current reference. The full-scale current of  $DAC_1$  is  $\pm 9$  mA, which corresponds to a full-scale input current of  $\pm 4.5$  mA.

As shown in Figure 9-4 (a), a triple-source configuration steers the current bias to either the positive or negative summing node during the active pulse, and to a relatively low impedance node set at  $V_{DD}/2$  during the return-to-zero time. This configuration allows the current sources to share current during the RZ time, and

therefore saves 25% of the current compared with alternative topologies. However, there is still 50% more bias current used in this design than would be for an NRZ implementation.

The RZ DAC switching waveforms are at full-level CMOS logic levels, so the switching transistors see a large overdrive. The on pulse control is output from NAND gates which retimes the data with the negative clock state. Careful attention to balancing the differential signals helps to keep source bounce low during switching events. Again, the power required in generating the switching waveforms for the RZ implementation is significantly higher than for an NRZ DAC, especially considering the 950MHz sampling rate.

In contrast to the RZ approach used for the primary DAC, the minor loop DAC (which corresponds to  $DAC_2$  in Figure 9-1) is implemented as an NRZ structure due to its less stringent performance requirements. The clocking of this DAC is done without retiming since the sensitivity to clock jitter and ISI is suppressed by the forward integration path. The 31-elements of this second DAC are scrambled with the barrel-shift DEM due to the bit-wise connection to the VCO-based quantizer, though the issue of DAC mismatch is not as important for this DAC as the primary one. The full-scale current of  $DAC_2$  is nominally  $\pm 64 \mu\text{A}$ , and can be adjusted over a wide range through an off-chip bias current such that peaking is properly controlled in the noise transfer function (NTF) of the ADC. With the minor loop disabled by removing the DAC current bias, the ADC was found to still be marginally stable.

### 9.2.3 Loop filter

The fully-differential loop filter schematic, which uses only a single opamp, is shown in Figure 9-5. As mentioned earlier, the loop filter includes a front-end passive filter composed of elements  $R_{IN}$ ,  $R_A$ , and  $C_{IN}$  in order to absorb the large current deviations of  $DAC_1$  and provide a very linear ADC front-end. Closer examination of the front-end passive filter reveals that voltage  $V_A$  is actually a virtual ground when placed in  $\Sigma\Delta$  feedback, so the ADC input current  $I_{IN}$  is defined primarily by resistor  $R_{IN}$ . The capacitor  $C_{IN}$  then filters the error signal  $I_{IN} - I_{DAC1}$  before  $I_A$

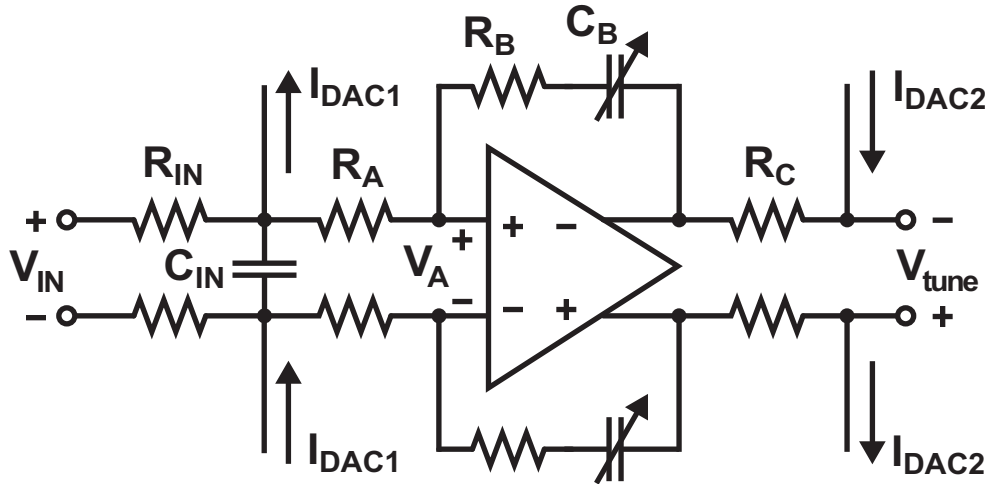


Figure 9-5 Schematic of the fully differential ADC loop filter

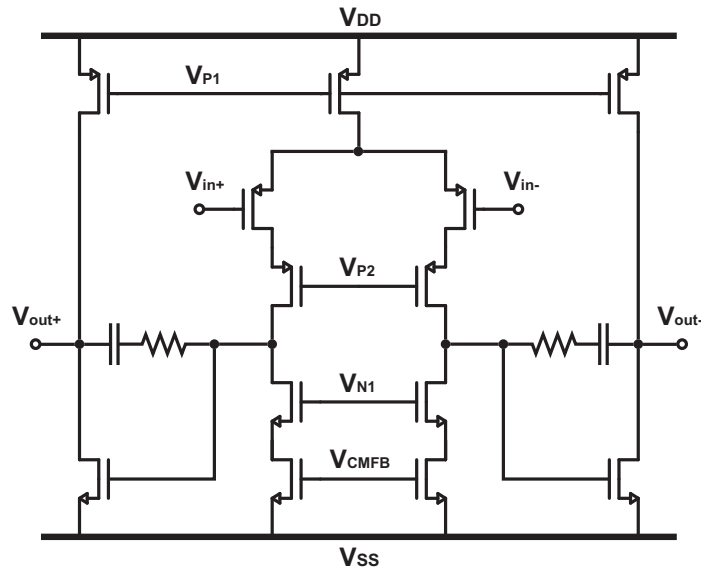


Figure 9-6 Operational amplifier schematic

is integrated onto capacitor  $C_B$ , whose value can be adjusted by  $\pm 25\%$  with an on-chip binary capacitor array. Adjustment of  $C_B$  leads to a gain change in the active integrator, which allows for better accommodation of  $K_v$  variations in the VCO-based quantizer. Of course, changes in  $C_B$  will also lead to variation in the value of the open loop zero formed by  $C_B$  and  $R_B$ .

The loop filter opamp is implemented with the two-stage Miller-compensated topology shown in Figure 9-6. Since the ADC input is assumed to have a constant

common-mode voltage at its input, the first opamp stage can be cascoded even with low supply voltage. Note that the output common-mode voltage also controls the input common-mode of the VCO, and is set according to a common-mode feedback circuit that consists of two large polysilicon resistors, a single-stage amplifier, and an off-chip reference voltage [58]. Interestingly, because the VCO-based quantizer offers relatively high SNR performance on its own, a large DC open loop gain is not required for the opamp in the proposed ADC topology. As such, the gain is designed to be over 50dB with a gain-bandwidth product in the range of 2-3GHz.

As mentioned earlier, minor loop feedback is used to compensate for excess loop delay from the quantizer and  $DAC_1$  in order to allow a more aggressive NTF. To avoid the use of another amplifier for a summation operation, current  $DAC_2$  is directed through resistor  $R_C$  such that the resulting voltage is added to the output of the opamp. Although the opamp output resistance is non-zero, it is much less than  $R_C$  in the frequencies of interest and does not need to be well-controlled since the gain and precision of this minor loop is not critical to ADC performance. The value of  $R_C$  is chosen to keep the parasitic pole, which is formed by  $R_C$  and the input capacitance of the quantizer, from affecting the loop dynamics. The full scale current of  $DAC_2$  is then set based on the value of  $R_C$  and considerations of the NTF. In addition to providing analog summation without an amplifier, another benefit to this topology is that the stability concerns of the operational amplifier are isolated from the input capacitance of the VCO-based quantizer.

# Chapter 10

## $\Sigma\Delta$ ADC results and discussion

A prototype of the ADC structure shown in Figure 9-1 is implemented in a  $0.13\mu\text{m}$  CMOS process. A microphotograph of the fabricated chip is shown in Figure 10-1. The active silicon area of the ADC is  $640\mu\text{m}\times 660\mu\text{m}$ , including power supply decoupling capacitors and guardring. Area for the 5-bit VCO-quantizer core is  $120\mu\text{m}\times 86\mu\text{m}$ , and the total chip area including 28 pads is 1.3mm x 1.3mm.

### 10.1 Measurement setup

The ADC chip is direct bonded onto an FR-4 circuit board that provides control signals, biasing, and power supplies with adequate decoupling capacitors. The output of the ADC is implemented with full-swing digital inverters on-chip, however a series resistor is included both on and off-chip, and termination is provided by a low impedance resistive network biased at mid-supply to minimize voltage swings.

To capture the 5-bits of 1Gsp/s data from the ADC, a pair of 4-channel digital oscilloscopes with a sample rate of 5Gsp/s are triggered to collect 1M samples simultaneously. Because 3-bits are sampled on the first instrument and 2-bits on the second, the data is then downloaded to MATLAB where clock and data recovery is performed digitally. For collecting parametric data measurements, a MATLAB interface controls the triggering, oscilloscopes, and data analysis.

Synchronized low-noise signal sources are used for both the input signal and sam-

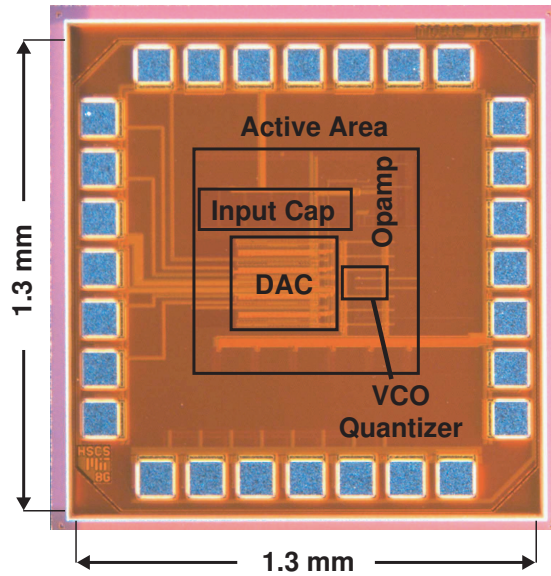


Figure 10-1 A microphotograph of the VCO-based ADC

Specification	Value
Sampling Frequency	900-1000 MHz
Input Bandwidth	10 / 20 MHz
Peak SNR	86 / 75 dB
Peak SNDR	72 / 67 dB
Analog Power	20mW (1.2V)
Digital Power	20mW (1.2V)
Peak Efficiency	0.5pJ/step
Active Area	$640\mu\text{m} \times 660\mu\text{m}$
Total Area	$1.3\text{mm} \times 1.3\text{mm}$
Technology	$0.13\mu\text{m}$ IBM CMOS

Table 10.1 Summary of VCO-based ADC measured performance

pling clock, with sharp bandpass filters for each as well. A fixed frequency bandpass filter with extremely high-Q is required for the input signal, and a tunable bandpass filter is used for the clock. All measurements are performed with the input signal AC-coupled, and the single-ended to differential conversion is performed using a transformer balun.



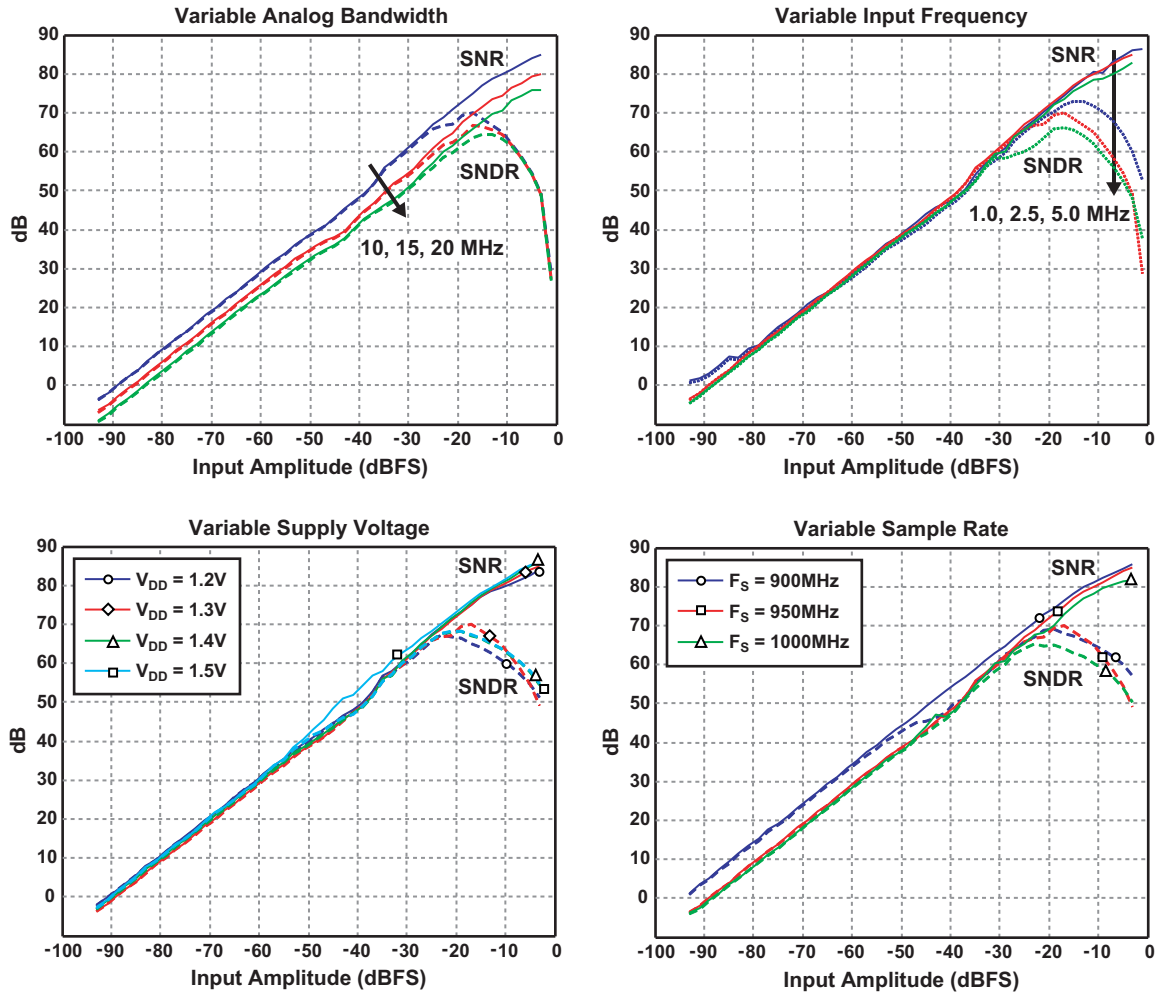


Figure 10-2 SNR/SNDR vs. input amplitude

## 10.2 Measurement results

The power consumption of the ADC is 40mW, which is evenly split between the 1.2V analog and digital supplies such that each draw roughly 16-17mA. Although there is no direct way to measure the sub-system current, bias currents indicate that the primary DAC consumes 9mA, and the operational amplifier 8mA. For the digital supply, the pulse waveform generation circuits for the RZ DAC require about 8mA, the VCO-quantizer 5mA, and the thermometer-to-binary summation circuits take the remaining 3mA. A summary of the ADC performance is found in Table 10.1, where the figure of merit is  $Power / (2 \cdot Bandwidth \cdot 2^{ENOB})$ .

The SNR and SNDR vs. input amplitude curves across a number of operating

conditions are shown in Figure 10-2. If not otherwise specified, the input frequency is 2.5MHz, the analog bandwidth is 10MHz, and the sample rate is 950MHz. At a 10MHz input bandwidth, the ADC achieves at least 81dB SNR and 65dB SNDR across all input frequencies, a power supply of 1.2-1.5V, and a sampling frequency of 900-1000MHz. While a peak SNR of 14-bits at 10MHz is achieved very efficiently with only 40mW of total power consumption, the ADC distortion performance is limited by the VCO-quantizer non-linearity to 10.5-12bits, depending on the specific test configuration.

The decline of SNDR with increasing signal frequency in Figure 10-2 is a consequence of the reduced gain of the loop filter at higher frequencies, which leads to reduced suppression of the VCO non-linearity. The degradation of SNDR by such non-linearity was about 5dB higher than predicted by simulation. This is likely due to the modeling accuracy of the VCO tuning characteristic, which can be affected by layout in addition to process and temperature variations. It may be possible to improve the SNDR somewhat with more attention given to modeling these issues, although as we will see later that other techniques offer more promise in improving VCO linearity.

It was observed that low input signal levels into the proposed ADC led to small limit-cycles which were seen in the 10-100kHz frequency range. These limit cycles are an artifact of the barrel-shift algorithm used for DEM on the DACs, which is why some demanding applications avoid the use of the barrel-shift algorithm in favor of other DEM strategies [3]. These small limit-cycles can reduce the SNR by a few dB when the input signal falls below about -35dBFS, as seen in the SNR vs. amplitude curves. As would be expected, the actual frequency of the limit-cycle depends somewhat on the input DC level.

An FFT of the ADC output with an 1.045MHz input signal at -15dBFS is shown in Figure 10-3. The third-order noise shaping is visible from 10-50MHz, and the quantization noise peaks around 60MHz. A small noise skirt centered around 1MHz was found to be from the bandpass filter used in testing. The high frequency quantization noise feature occurring in the 200-300MHz range is believed to be caused by the

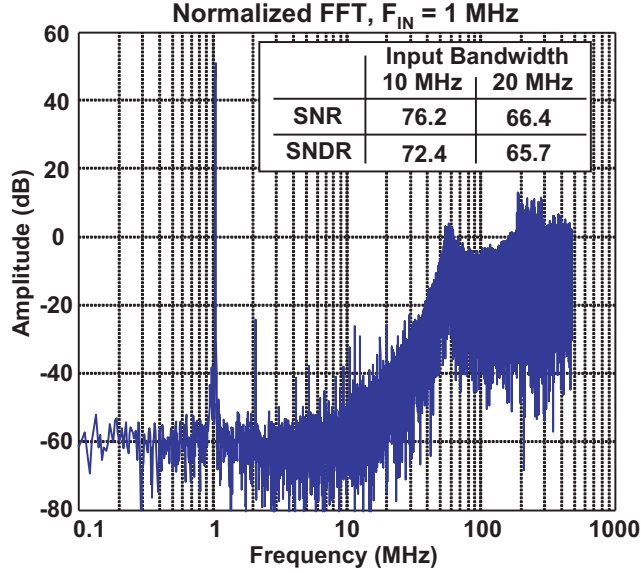


Figure 10-3 190,190 point Hanning FFT normalized to an LSB

Ref.	$F_S$ (MHz)	BW (MHz)	SNR (dB)	SNDR (dB)	Power (mW)
[79]	276	23	70	69	43
[6]	340	20	71	69	56
[49]	400	12	64	61	70
[61]	640	10	72	66	7.5
[40]	640	20	76	74	20
[60]	1000	8	63	63	10
<b>This work</b>	<b>950</b>	<b>10</b>	<b>86</b>	<b>72</b>	<b>40</b>

Table 10.2 Comparison with published high-speed CT ADC

mismatch between rising and falling edges of the VCO-quantizer, as verified with behavioral simulation. Fortunately, this artifact does not affect the functional operation of the ADC as its stability was seen to be robust across a wide variety of operating conditions.

### 10.3 Discussion

Table 10.2 compares this work with other reported CT  $\Sigma\Delta$  CMOS ADC operating at a sampling rate over 250MHz and an analog bandwidth of more than 5MHz.

The high SNR of 86dB achieved in this work points to the strength of the VCO-quantizer architecture, which allows efficient reduction of quantization noise through high-speed operation. In addition, the SNDR performance and power consumption are in line with other realizations, and as seen in Chapter 8, additional VCO non-linearity suppression is possible to improve performance further.

In combination with an optimized NTF for a 10-20MHz bandwidth, a higher-order loop filter may be expected to yield at least another 10dB or more of linearity on top of the performance reported in this work. Coupled with a more power efficient NRZ DAC design, a forecast performance of over 80dB with 20-30mW in 0.13 $\mu$ m CMOS would certainly compete well with today's state-of-the-art implementations and architectures. Because the VCO-quantizer scales well with digital process technology, there may be even more advantage in the architecture going forward.

Some ADC applications requiring more than 13-14 ENOB with low OSR may face practical limitations to the levels of linearity suppression from that can be achieved from known in-loop analog techniques reported in this work. In addition, other sources of distortion will then become significant, both in the feedback DAC and in the front-end amplifiers. Future research in the area of VCO-quantizers may find promising results from novel  $\Sigma\Delta$  linearization techniques, alternative ADC architectures with less sensitivity to VCO voltage-to-frequency distortion, or operation with a more balanced level of linearity and quantization noise performance.

# Chapter 11

## Conclusion

In this thesis, we have introduced, analyzed, and demonstrated a set of noise-shaping techniques that utilize a voltage controlled ring oscillator in a variety of ways. These techniques were applied to two distinct state-of-the-art converters, a time-to-digital converter with first-order quantization and mismatch noise-shaping, and a continuous-time  $\Sigma\Delta$  analog-to-digital converter. In both cases, the fundamental ability of the VCO to perform analog signal processing with highly digital circuitry was leveraged to efficiently achieve high-performance data conversion in advanced CMOS.

For the VCO-based time-to-digital converter, a multi-path gated ring oscillator topology was introduced that, when combined with appropriate measurement techniques as discussed, can achieve first-order noise-shaping of quantization and mismatch error. The key requirement of the architecture, to accurately preserve analog state information, was discussed in detail, and two example GRO designs were presented to highlight the important design considerations. First-order TDC noise-shaping performance was then verified in a prototype implementation fabricated in  $0.13\mu\text{m}$  CMOS technology, with measurements presented at both the component and system level.

To our knowledge, the gated ring oscillator time-to-digital converter presented in this thesis was the first TDC to demonstrate noise-shaping of analog quantization and mismatch error for non-adjacent measurement intervals. Further, compared with other reported TDC, the prototype described in this work is very competitive in

regard to important metrics such as dynamic range, power, and area.

In the case of the VCO-based analog-to-digital converter, the performance advantages and limitations of a VCO-based quantizer were presented and discussed using both theory and simulated examples. Because the non-linearity of the VCO frequency tuning presents the primary bottleneck for achieving high-performance, trade-offs for using the VCO-quantizer within a  $\Sigma\Delta$  ADC architecture were presented. To demonstrate these considerations, a high-speed continuous time  $\Sigma\Delta$  ADC operating at 950Msps was designed and fabricated in  $0.13\mu\text{m}$  CMOS. Although the architecture chosen for this work was originally disclosed in [39], measurement results were presented in this work that justifies the consideration of VCO-based quantizers in  $\Sigma\Delta$  ADC. Possible improvements are also discussed that may significantly improve these results.

Because analog device characteristics in future CMOS processes are not expected to improve, the increasing trend of replacing analog signal processing with digital signal processing is likely to continue. At the same time, analog functions cannot entirely disappear from the mixed-signal interface. Therefore, as demonstrated in this work, the ability to achieve and leverage high-performance analog functionality with highly digital circuit elements is very compelling, and is an exciting area for future research.

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